## CSC 323 Algorithm Design and Analysis <br> Spring 2017, Instructor: Dr. Natarajan Meghanathan Student Feedback Survey

## Assessment of Course Outcomes

On a scale of 1 through 4 ( 1 being Poor and 4 being Excellent), please rate your ability to perform on each of the following course outcomes before and after taking the course:

| Course Outcomes | Before | After |
| :--- | :--- | :--- |
| CO-1: Analyze the time complexity of recursive and non-recursive algorithms with <br> respect to the asymptotic order of growth |  |  |
| CO-2: Prove or justify the correctness of algorithms and their properties through <br> formal or informal analysis |  |  |
| CO-3: Design and analyze algorithms to solve optimization problems using general <br> techniques such as brute-force, divide-and-conquer, decrease-and-conquer as well <br> as transform-and-conquer |  |  |
| CO-4: Reduce one NP-complete problem to another NP-complete problem in <br> polynomial-time as well as design and analyze polynomial-time heuristics to <br> approximate solutions for NP-complete problems |  |  |
| CO-5: Discuss efficient algorithms for various graph theory problems (traversal, <br> topological sort, shortest paths and minimum spanning trees) based on different <br> design techniques |  |  |
| CO-6: Design and analyze algorithms to solve combinatorial problems using <br> advanced techniques such as dynamic programming and greedy strategies |  |  |
| CO-7: Develop and evaluate efficient implementations of algorithms, based on the <br> different design techniques, and their associated run-time complexity through <br> experimental analysis |  |  |
| Overall knowledge of the materials taught in the CSC 323 course |  |  |

In a scale of 1 through 4 ( 1 being Least Helpful and 4 being Most Helpful), please rate and comment on the usefulness of the following:

| Item | Rating [1 - Least Helpful and 4 - Most Helpful] |
| :--- | :--- |
| Question Bank and Solutions |  |
| Quizzes and Solutions |  |
| Help Videos on Selected Lecture Topics Recorded <br> by the Instructor Offline and Posted in YouTube |  |
| Video recording-based project submissions |  |
| Open Notes for exams |  |
| Individualized Take Home Exams and Quizzes |  |

Please write your comments on any aspect of the course that you rated above, as well as any other comment you want to mention about the course that will make it better [Continue on reverse side].
$\qquad$ J\#: $\qquad$

Jackson State University
CSC 323 Algorithm Design and Analysis, Spring 2017
Instructor: Dr. Natarajan Meghanathan
Exam 3 (FINAL EXAM)
Maximum Points: 150
Due on: April 25: 1 PM to 3 PM at my office, ENB 275
Submissions will NOT be accepted after 3 PM on April 25.
Print this exam and answer in the blank space/page provided after each question. You should staple your exam.

Q1:35 pts) For the graph assigned to you, find the following using the approximation heuristics discussed in class.
(a) Maximal Independent Set
(b) Minimal Vertex Cover
(c) Maximal Clique and (d) Minimum Connected Dominating Set

Show all the work for each.


Name: $\qquad$


Darren McGee


Justin McGuffee


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Q2: 30 pts ) You are assigned the edge weight matrix for a complete graph. Determine an approximation to the minimum weight tour using the (i) Nearest neighbor heuristic (ii) Twice around the tree heuristic.
Also, show one attempt of reducing the tour weight using the 2-change heuristic for the tour obtained with each of the two heuristics.

Show all the work as well as clearly indicate the tour and its weight before and after the attempt of using the 2-change heuristic in each case.

| Alexander Arrington |  |  |  |  |  | Jaylen Boykin |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V1 | V2 | V3 | V4 | V5 | V6 | V1 | V2 | V3 | V4 | V5 | V6 |
| V1 0 | 9 | 15 | 1 | 8 | 6 | V1 |  | 10 | 4 |  |  |
| V2 9 | 0 | 15 | 10 | 4 | 6 | V2 9 | 0 | 10 | 1 | 7 | 15 |
| V3 15 | 15 | 0 | 9 | 13 | 4 | V3 10 | 3 | 0 | 1 | 11 | 14 |
| V4 1 | 10 | 9 | 0 | 13 | 5 | V4 4 | 1 | 8 | 0 |  |  |
| v5 8 | 4 | 13 | 13 | 0 | 13 | V5 6 | 7 | 11 | 11 | 0 | 5 |
| V6 6 | 6 | 4 | 5 | 13 | 0 | V6 15 | 2 | 14 | 15 | 5 | 0 |
| Jason Bruno |  |  |  |  |  |  |  | Elbert Buchanan |  |  |  |
| V1 | V2 | V3 | V4 | V5 | V6 | V1 | V2 | V3 | V4 | V5 | V6 |
| V1 0 | 8 | 6 | 2 | 9 | 14 |  | 10 | 2 | 14 | 12 | 14 |
| V2 8 | 0 | 4 | 14 | 5 | 9 | V2 10 | 0 | 7 | 8 | 15 | 7 |
| V3 6 | 4 | 0 | 5 | 15 | 10 | V3 2 | 7 | 0 | 7 | 14 | 12 |
| V4 2 | 14 | 5 | 0 | 12 | 10 | V4 14 | 8 | 7 | 0 | 2 | 14 |
| V5 9 | 5 | 15 | 12 | 0 | 3 | V5 12 | 15 | 14 | 2 | 0 | 14 |
| V6 14 | 9 | 10 | 10 | 3 | 0 | V6 14 | 7 | 12 | 14 | 14 | 0 |
| Daniel Epps |  |  |  |  |  |  | Jordan Hubbard |  |  |  |  |
| V1 | V2 | V3 | V4 | V5 | V6 | V1 | V2 | V3 | V4 | V5 | V6 |
| V1 0 | 2 | 10 | 15 | 14 | 6 |  |  | 8 | 14 | 1 | 12 |
| V2 2 | 0 | 7 | 3 | 14 | 8 | V2 4 | 0 | 4 | 7 | 14 | 15 |
| V3 10 | 7 | 0 | 12 | 3 | 15 | V3 8 | 4 | 0 | 13 | 11 | 9 |
| V4 15 | 3 | 12 | 0 | 5 | 10 | V4 14 | 7 | 13 | 0 | 5 | 6 |
| v5 14 | 14 | 3 | 5 | 0 | 8 | V5 1 | 14 |  | 5 | 0 | 13 |
| V6 6 | 8 | 15 | 10 | 8 | 0 | V6 12 | 15 | 9 | 5 | 13 | 0 |

Kayla Johnson

|  | V1 | V2 | V3 | V4 | V5 | V6 |  | V1 | V2 | V3 | V4 | V5 | V6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V1 | 0 | 14 | 10 | 2 | 9 | 7 | V1 | 0 | 11 | 5 | 5 | 6 | 14 |
| V2 | 14 | 0 | 1 | 2 | 13 | 12 | V2 | 11 | 0 | 5 | 9 | 10 | 9 |
| V3 | 10 | 1 | 0 | 13 | 2 | 5 | V3 | 5 | 5 | 0 | 2 | 6 | 12 |
| V4 | 2 | 2 | 13 | 0 | 15 | 3 | V4 | 5 | 9 | 2 | 0 | 6 | 13 |
| V5 | 9 | 13 | 2 | 15 | 0 | 2 | V5 | 6 | 10 | 6 | 6 | 0 | 2 |
| V6 | 7 | 12 | 5 | 3 | 2 | 0 | V6 | 14 | 9 | 12 | 13 | 2 | 0 |

Darren McGee

|  | V1 | V2 | V3 | V4 | V5 | V6 |  | V1 | V2 | V3 | V4 | V5 | V6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V1 | 0 | 6 | 12 | 15 | 15 | 12 | V1 | 0 | 2 | 1 | 12 | 11 | 13 |
| V2 | 6 | 0 | 11 | 4 | 6 | 3 | V2 | 2 | 0 | 7 | 12 | 8 | 6 |
|  | 12 | 11 | 0 | 3 | 5 | 12 | V3 | 1 | 7 | 0 | 11 | 8 | 8 |
|  | 15 | 4 | 3 | 0 | 13 | 3 | V4 | 12 | 12 | 11 | 0 | 6 | 12 |
|  | 15 | 6 | 5 | 13 | 0 | 3 | V5 | 11 | 8 | 8 | 6 | 0 | 8 |
| V6 | 12 | 3 | 12 | 3 | 3 | 0 | V6 | 13 | 6 | 8 | 12 | 8 | 0 |

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| Kayshaunna Williams |  |  |  |  |  |  |  |  |  | Michael Wilson |  |  |  |
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|  | V1 | V2 | V3 | V4 | V5 | V6 |  | V1 | V2 | V3 | V4 | V5 | V6 |
| V1 | 0 | 3 | 7 | 2 | 2 | 3 | V1 | 0 | 8 | 14 | 4 | 10 | 15 |
| V2 | 3 | 0 | 9 | 13 | 6 | 4 | V2 | 8 | 0 | 7 | 4 | 9 | 8 |
| V3 | 7 | 9 | 0 | 12 | 7 | 9 | V3 | 14 | 7 | 0 | 5 | 12 | 14 |
| V4 | 2 | 13 | 12 | 0 | 9 | 9 | V4 | 4 | 4 | 5 | 0 | 4 | 10 |
| v5 | 2 | 6 | 7 | 9 | 0 | 9 | V5 | 10 | 9 | 12 | 4 | 0 | 2 |
| V6 | 3 | 4 | 9 | 9 | 9 | 0 | V6 | 15 | 8 | 14 | 10 | 2 | 0 |

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Q3: 30 pts ) For the edge weight matrix assigned to you for a directed graph, determine the shortest path weights between any two vertices of the graph using the Floyd-Warshall algorithm.

Show clearly the distance matrix and the predecessor matrix for each iteration.
Also, extract a path of length two or above between any two vertices of your choice. Clearly show the path extraction steps, as shown in the slides.


Jason Bruno

|  | V1 | V2 | V3 | V4 | V5 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| V1 | 0 | $\infty$ | $\mathbf{2}$ | $\mathbf{4}$ | $\mathbf{1 1}$ |
| V2 | 1 | 0 | 8 | $\infty$ | 1 |
| V3 | $\mathbf{4}$ | $\infty$ | 0 | 8 | 3 |
| V4 | $\mathbf{1 0}$ | $\mathbf{7}$ | 5 | 0 | $\infty$ |
| V5 | $\infty$ | $\mathbf{1 5}$ | $\mathbf{1 0}$ | 9 | 0 |

Daniel Epp

| V1 | V2 | V3 | V4 | V5 |  | V1 | V2 | V3 | V4 | V5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V1 0 | $\infty$ | 8 | 4 | 10 | V1 | 0 | $\infty$ | 13 | 2 | 13 |
| V2 8 | 0 | 14 | 4 | $\infty$ | V2 | 8 | 0 | 15 | 12 | 0 |
| V3 14 | 12 | 0 | 5 | $\infty$ | V3 | 9 | $\infty$ | 0 | 2 | 5 |
| V4 2 | $\infty$ | 13 | 0 | 2 | V4 1 | 4 | $\infty$ | 10 | 0 | 4 |
| V5 3 | $\infty$ | 12 | 13 | 0 | V5 | 3 | 6 | 12 | $\infty$ | 0 |

Kayla Johnson

|  | V1 | V2 | V3 | V4 | V5 |  | V1 | V2 | V3 | V4 | V5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V1 | 0 | $\infty$ | 7 | 10 | 7 | V1 | 0 | 1 | 14 | 12 | $\infty$ |
| V2 | 2 | 0 | 15 | 15 | $\infty$ | V2 | 6 | 0 | $\infty$ | 11 | 1 |
| V3 | $\infty$ | 2 | 0 | 7 | 8 | V3 | $\infty$ | 10 | 0 | 9 | 5 |
| V4 | 4 | 15 | 2 | 0 | $\infty$ | V4 | $\infty$ | 9 | 15 | 0 | 4 |
| 5 | 9 | 15 | $\infty$ | 5 | 0 |  | 10 |  | 7 | $\infty$ | E |

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Darren McGee

|  | V1 | V2 | V3 | V4 | V5 |
| :--- | :--- | ---: | ---: | ---: | ---: |
| V1 | 0 | $\mathbf{5}$ | $\mathbf{4}$ | $\infty$ | $\mathbf{1 5}$ |
| V2 | $\infty$ | 0 | 12 | $\mathbf{8}$ | $\mathbf{7}$ |
| V3 | $\mathbf{3}$ | $\mathbf{1 0}$ | 0 | $\mathbf{1}$ | $\infty$ |
| V4 | 6 | 6 | $\infty$ | 0 | $\mathbf{4}$ |
| V5 | $\mathbf{8}$ | $\infty$ | $\mathbf{3}$ | $\mathbf{1 3}$ | 0 |


| Kayshaunna Williams |  |  |  |  | Michael Wilson |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | V1 | V2 | V3 | V4 | V5 | V1 |  | V2 | V3 | V4 | V5 |
| V1 | 0 | 3 | 2 | $\infty$ | 9 | V1 | 0 | 1 | 11 | 6 | $\infty$ |
| V2 | $\infty$ | 0 | 5 | 8 | 6 |  | 1 | 0 | 10 | $\infty$ | 12 |
| V3 | 9 | 6 | 0 | $\infty$ | 7 | V3 | 4 | $\infty$ | 0 | 10 | 6 |
| V4 | $\infty$ | 13 | 14 | 0 | 8 | V4 | 2 | 2 | 1 | 0 | $\infty$ |
| V5 | 3 | 2 | $\infty$ | 6 | 0 | V5 |  | $\infty$ | 3 | 15 | 0 |

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Q4: 25 pts) Run the Dijkstra's shortest path algorithm on the graph assigned to you, starting from Vertex 1 , and determine the shortest path tree rooted from Vertex 1 to the rest of the vertices. If any edge does not have weight assigned, assume the weight of that edge to be 5 . Show your work for each iteration in the skeletal graphs (see next page). For each skeletal graph, indicate the vertices and all the edges that are selected as part of the particular iteration as well as carried over from the previous iterations. Show all the steps.

Alexander Arrington


Elbert Buchanan


Kayla Johnson


Kayshaunna Williams



Daniel Epps


Bria McCutcheon


Michael Wilson


Jason Bruno


Jordan Hubbard


Darren McGee


Justin McGuffee

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Skeletal Graphs (Iterations)


Given Graph


Iteration 1


Iteration 3


Iteration 5


Iteration 7


Initialization


Iteration 2


Iteration 4


Iteration 6


Shortest Path Tree

Sum of the Weights of the Shortest Path Tree: $\qquad$
$\qquad$
$\qquad$

Q5: 15 pts ) Run the Kruskal's algorithm for minimum weight spanning tree on the graph assigned to you. If any edge does not have weight assigned, assume the weight of that edge to be 5 . Show your work for each iteration in the skeletal graphs (see next page). For each skeletal graph, indicate the vertices and all the edges that are selected as part of the particular iteration as well as carried over from the previous iterations. Show all the steps.

Alexander Arrington


Elbert Buchanan


Kayla Johnson


Kayshaunna Williams



Daniel Epps


Bria McCutcheon


Michael Wilson


Jason Bruno


Jordan Hubbard


Justin McGuffee

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## Skeletal Graphs (Iterations)




Iteration 1


Iteration 3


Iteration 5


Iteration 7


Iteration 2


Iteration 4


Iteration 6


Minimum Weight Spanning Tree

Sum of the weights of the Minimum Weight Spanning Tree: $\qquad$
$\qquad$
$\qquad$

Q6: 15 pts ) Run a Breadth First Search (BFS) on the graph and find the level numbers of the vertices as well as identify the tree edges and cross edges.

Use the results to determine whether the graph is bipartite (2-colorable) or not. If the graph is bipartite, identify the two partitions of the graph. If the graph is not bipartite, identify the edges that prevent the graph from being bipartite.

Alexander Arrington



Elbert Buchanan


Jordan Hubbard


Daniel Epps


Justin McGuffee


Michael Wilson


Name:
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