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# CSC 228 Data Structures and Algorithms, Fall 2017 

Instructor: Dr. Natarajan Meghanathan
Exam 2 (Take Home: Nov. 13, 2017 @ 1 PM) Max. Points: 75
Print this exam and answer in the space provided. Staple and submit in class.
Given an array of integers, do the following:

| 1 | Toni Barnes | [14, | 14, | 2, | 10, | 18, | 7, | 3, | 3, | 15, | 10, | 27, | 23] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | Ujjwal Baskota | [17, | 13, | 16, | 7, | 25, | 11, | 4, | 22, | 10, | 21, | 28, | 29] |
| 3 | Albert Boateng | [16, | 12, | 11. | 29, | 21, | 17, | 8 , | 19, | 18, | 10, | 10, |  |
| 4 | Ronnal Boyd | [18, | 28, | 2, | 27, | 18, | 16, | 29, | 2, | 0 , | 6, | 8 , |  |
| 5 | Deonte Buckner | [20, | 13, | 12, | 6 , | 13, | 14, | 10, | 9, | 9, | 14, | 12, | 20] |
| 6 | Nissi Campbell | [11, | 27, | 27, | 5 , | 29, | 6, | 22, | 22, | 16, | 7, | 27, | 19] |
| 7 | Samuel Ayalew Dagne | [26, | 9 , | 29, | 9, | 0 , | 23, | 5 , | 23, | 23, | 24, | 2, | 18] |
| 8 | Zakeia Davis | [10, | 18, | 22, | 28, | 5 , | 2, | 12, | 4, | 7, | 19, | 2, | 26] |
| 9 | Joshua Everett | [11, | 0 , | 20, | 26, | 22, | 0 , | 13, | 14, | 28, | 26, | 3 , | 27] |
| 10 | Amanuel E. Gebre | [2, | 8 , | 9, | 3 , | 28, | 26, | 8 , | 19, | 1, | 10, | 19, | 10] |
| 11 | James Harris | [22, | 24, | 24, | 18, | 15, | 5, | 7, | 0 , | 3 , | 20, | 20, |  |
| 12 | Jillian Hart | [12, | 27, | 0 , | 16, | 6 , | 23, | 28, | 16, | 3 , | 13, | 29, | $26]$ |
| 13 | Ellis Hill | [3, | $14,$ | 14, | 29, | 26, | 19, | 20, | 27, | 26, | 0 , | 17, | 27] |
| 14 | Demarcus Johnson | [25, | 13, | 14, | 21, | 25, | 3 , | 10, | 27, | 18, | 25, | 15, | 25] |
| 15 | Demarius Jones | [15, | 3 , | 18, | 16, | 8 , | 6 , | 14, | 15, | 28, | 12, | 23, |  |
| 16 | Ning Kang | [17, | 3 , | 18, | 27, | 0 , | 5, | 19, | 19, | 9, | 4, | 8 , |  |
| 17 | Ji Mack | [6, | $15,$ | 16, | 20, | 23, | 6 , | $11,$ | 18, | 17, | 1, | 18, |  |
| 18 | DeOnica Mitchell | [2, | 1 , | 23, | 28, | 27, | 5, | 11, | 25, | 19, | 14, | 29, |  |
| 19 | Cortland Moten | [25, | 20, | 17, | 28, | 28, | 11, | 23, | 6 , | 1, | 14, | 27, | 27] |
| 20 | Dakota Nichols | [21, | 15, | 1, | 16, | 11, | 2, | 29, | 11, | 8 , | 16, | 23, |  |
| 21 | Sherrod Perry | [29, | 12, | 3 , | 10, | 19. | 20, | 10, | 24, | 6, | 18, | 25, |  |
| 22 | Jontay Reynolds | [8, | 22, | 28, | 11, | 22, | 11, | 23, | 3 , | 0 , | 12, | 8 , |  |
| 23 | Christopher Robinson | [24, | 24, | 14, | 17, | 7, | 25, | 27, | 17, | 22, | 4, | 0, | 11] |
| 24 | Keara Rogers | [3, | 27, | 18, | 25, | 23, | 14, | 3 , | 24, | 3, | 17. | 10, |  |
| 25 | Ancornelius Sandifer | [9, | 10, | 28, | 2, | 5, | 21, | 8 , | 10, | 4, | 4, | 10, |  |
| 26 | Varlin Sheffey | [24, | 22, | 18, | 9, | 20, | 10, | 25, | 21, | 3, | 3, | 14, |  |
| 27 | Timothy Stewart | [5, | 11, | 20, | 1, | 18, | 6 , | 8 , | 16, | 12, | 24, | 4, | 24] |
| 28 | Nebiyou Tadesse | [13, | 0 , | 8 , | 6 , | 21, | 21, | 9, | 7 , | 22, | 20, | 0 , |  |
| 29 | Astride Tchakoua | [8, | 12, | 9, | 25, | 11. | 2, | 15, | 6 , | 15. | 22, | 24, |  |
| 30 | Ingrid Tchakoua | [15, | 14, | 21, | 28, | 3, | 4, | 24, | 26, | 25, | 6, | 17, |  |
| 31 | Alexander Thomas | [19, | 20, | 8, | 14, | 7, | 7, | 4, | 18, | 5, | 29, | 28, |  |
| 32 | Eriana Thomas | [19, | 24, | 26, | 18, | 25, | 3, | 15, | 27, | 29, | 9, | 20, |  |
| 33 | Nia Whavers | [25, | 9, | 20, | 18, | 7, | 15, | 26, | 23, | 28, | 5, | 9, |  |
| 34 | Semenbari Yakubu | [29, | 26, | 9, | 23, | 28, | 27, | 23, | 11, | 20, | 7 , | 9, | 23] |
| 35 | Taba Zimmerman | [8, | 6 , | 1, | 29, | 2, | 4, | 5, | 11, | 1 , | 24, | 15 , | 12] |

$\qquad$ J\#: $\qquad$
(Q1-15 pts) Construct a max heap of the array. Show the initial essentially complete binary tree and the transformation of the binary tree to a max heap via the reheapify operations at the indices of the internal nodes (as shown in the slides).

Student Name:
J\#: $\qquad$
(Q2-10 pts) Transform the max heap to a min heap (via direct transformation) using a sequence of reheapify operations.
$\qquad$ J\#: $\qquad$
(Q3-15 pts) Sort the min heap version (obtained from Q2) of the array (step by step) in order to obtain an array of reversely sorted integers.

Student Name: __ J\#:

Student Name:
J\#: $\qquad$
(Q4-10 pts) Transform the max heap (obtained from Q1) to a binary search tree. Show all the steps.

Student Name:
J\#: $\qquad$
(Q5-10 pts) Transform the binary search tree of (Q4) to a min heap. Show all the steps.
$\qquad$ J\#: $\qquad$
(Q6-5 pts) Differentiate between the binary trees/min heaps of (Q2) and (Q5) with respect to the nature of data distribution in the left sub tree and right sub tree of each internal node.
(Q7-10 pts) Consider the binary search tree of (Q4). Delete the root node of this binary search tree and do the necessary transformation (as discussed in the slides of Module 7) to get a new binary search tree.

