

Module 2: List ADT

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List ADT

- A collection of entities of the same data type
- List ADT (static)
 - Functionalities (logical view)
 - Store a given number of elements of a given data type
 - Write/modify an element at a particular position
 - Read an element at a particular position
- Implementation:
 - Arrays: A contiguous block of memory of a certain size, allocated at the time of creation/initialization
 - Time complexity to read and write/modify are $\Theta(1)$ each

	A[0]		A[2]			
Array index	0	1	2	3	N-1
Array, A	10	23	13	17	21
Memory address	200	204	208	212		2xx

Code 1 (C++): Static List Implementation using Arrays

```
#include <iostream>
using namespace std;

class List{
    private:
        int *array;

    public:
        List(int size){
            array = new int[size];
        }

        void write(int index, int data){
            array[index] = data;
        }

        int read(int index){
            return array[index];
        }
};
```

```
int main(){
    int listSize;

    cout << "Enter list size: ";
    cin >> listSize;

    List integerList(listSize);

    for (int i = 0; i < listSize; i++){
        int value;
        cout << "Enter element # " << i << " : ";
        cin >> value;
        integerList.write(i, value);
    }

    return 0;
}
```

Code 1(Java): Static List Implementation using Arrays

```
class List{  
  
    private int array[];  
  
    public List(int size){  
        array = new int[size];  
    }  
  
    public void write(int index, int data){  
        array[index] = data;  
    }  
  
    public int read(int index){  
        return array[index];  
    }  
  
}
```

```
import java.util.*;

class StaticListArray{

    public static void main(String[] args){

        Scanner input = new Scanner(System.in);

        int listSize;

        System.out.print("Enter list size: ");
        listSize = input.nextInt();

        List integerList = new List(listSize);

        for (int i = 0; i < listSize; i++){

            int value;
            System.out.print("Enter element # "+ i+" : ");
            value = input.nextInt();

            integerList.write(i, value);
        }

    }
}
```

Dynamic List ADT

- **Limitations with Static List**
 - The list size is fixed (during initialization); cannot be increased or decreased.
 - With a static list, the array is filled at the time of initialization and can be later only read or modified. A new element cannot be “inserted” after the initialization phase.
- **Key Features of a Dynamic List**
 - Be able to resize (increase or decrease) the list at run time. The list size need not be decided at the time of initialization. We could even start with an empty list and populate it as elements are to be added.
 - Be able to insert or delete an element at a particular index at any time.
- **Performance Bottleneck**
 - When we increase the size of the list (i.e., increase the size of the array that stores the elements), the contents of the array need to be copied to a new memory block, element by element. → $O(n)$ time.
 - Hence, even though, we could increase the array size by one element at a time, the ‘copy’ operation is a performance bottleneck and the standard procedure is to double the size of the array (list) whenever the list gets full.
 - A delete operation also takes $O(n)$ time as elements are to be shifted one cell to the left.

Code 2: Code for Dynamic List ADT Implementation using Arrays

Variables and Constructor (C++)

```
private:
    int *array;
    int maxSize;
    int endOfArray;

public:
    List(int size){
        maxSize = size;
        array = new int[maxSize];
        endOfArray = -1;
    }
```

isEmpty (C++)

```
bool isEmpty(){
    if (endOfArray == -1)
        return true;
    return false;
}
```

Variables and Constructor (Java)

```
private int array[];
private int maxSize;
private int endOfArray;

public List(int size){
    maxSize = size;
    array = new int[maxSize];
    endOfArray = -1;
}
```

isEmpty (Java)

```
public boolean isEmpty(){
    if (endOfArray == -1)
        return true;
    return false;
}
```

Code 2: Insert Function (C++ and Java)

```
void insertAtIndex(int insertIndex, int data){
```

```
    // if the user enters an invalid insertIndex, the element is  
    // appended to the array, after the current last element  
    if (insertIndex > endOfArray+1)  
        insertIndex = endOfArray+1;
```

```
    if (endOfArray == maxSize-1) Will take O(n) time each, where  
        resize(2*maxSize); n = maxSize + 1
```

```
    for (int index = endOfArray; index >= insertIndex; index--)  
        array[index+1] = array[index];
```

```
    array[insertIndex] = data;  
    endOfArray++;
```

```
}
```

```
void insert(int data){  
    if (endOfArray == maxSize-1)  
        resize(2*maxSize);  
    array[++endOfArray] = data;  
}
```


Code 2: Resize Function (C++)

```
void resize(int s){  
    // in addition to increasing, the resize function  
    // also provides the flexibility to reduce the size  
    // of the array  
    int *tempArray = array;  
    array = new int[s];  
    for (int index = 0; index < min(s, endOfArray+1); index++){  
        array[index] = tempArray[index];  
    }  
    maxSize = s;  
}
```


Have another pointer (a temporary ptr) to refer to the starting address of the memory represented by the original array

Allocating a new set of memory blocks to the 'array' variable

Copying back the contents pointed to by the temporary array pointer to the original array

If the array size is reduced from maxSize to s, only the first 's' elements are copied. Otherwise, all the maxElements are copied

new value of maxSize



Code 2: Resize Function (Java)

```
public void resize(int s){
```

Have another reference (a temporary ref) to refer to the starting address of the memory represented by the original array

```
    int tempArray[] = array;
```

```
    array = new int[s];
```

Allocating a new set of memory blocks to the 'array' variable

```
    for (int index = 0; index < Math.min(s, endOfArray+1); index++){  
        array[index] = tempArray[index];  
    }
```

Copying back the contents pointed to by the temporary array reference to the original array

```
    maxSize = s;
```

If the array size is reduced from maxSize to s, only the first 's' elements are copied. Otherwise, all the maxElements are copied

```
}
```

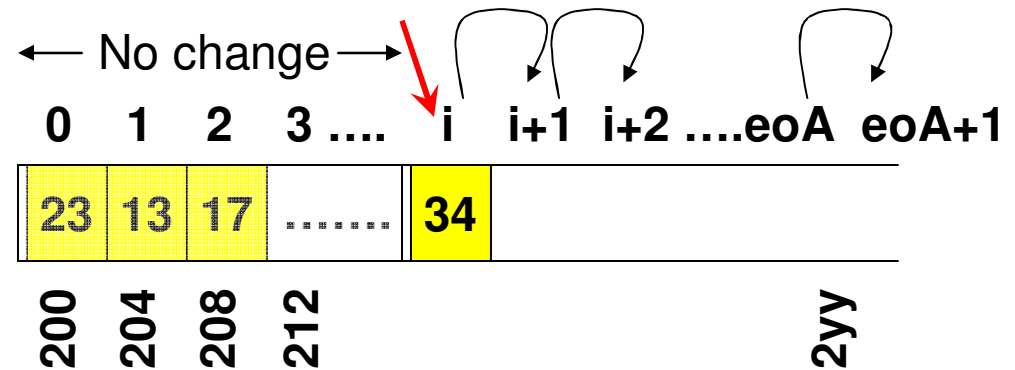
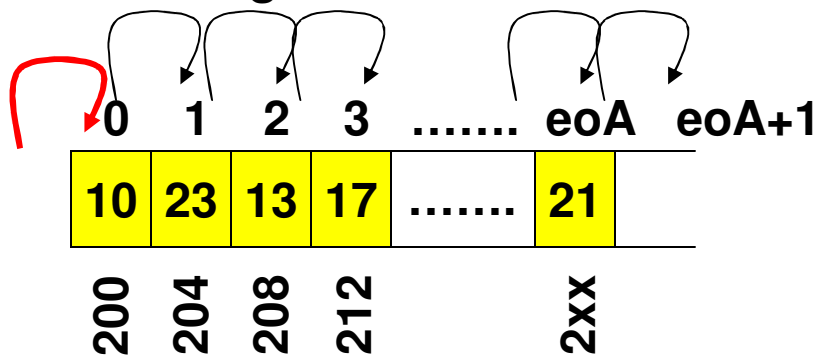
new value of maxSize



Time complexity analysis for 'Insert': Dynamic List ADT as an Array

Insert operation

- (i) Worst case: If the element is to be inserted as the first element in the array, then elements from index `endOfArray(eoA)` to index '0' have to be shifted one position to the right. If $eoA = n-1$, then 'n' (indexes 0 to n-1) such shifting need to be done.



- (ii) Best case: If the element is to be inserted at the end of the array, no shifting is needed.
- (iii) In general, if the element is to be inserted at index i , then the elements from index `endOfArray(eoA)` to index 'i' need to be shifted one cell to the right.

Time complexity for insert operation: $O(n)$

Code 2: Other Auxiliary Functions

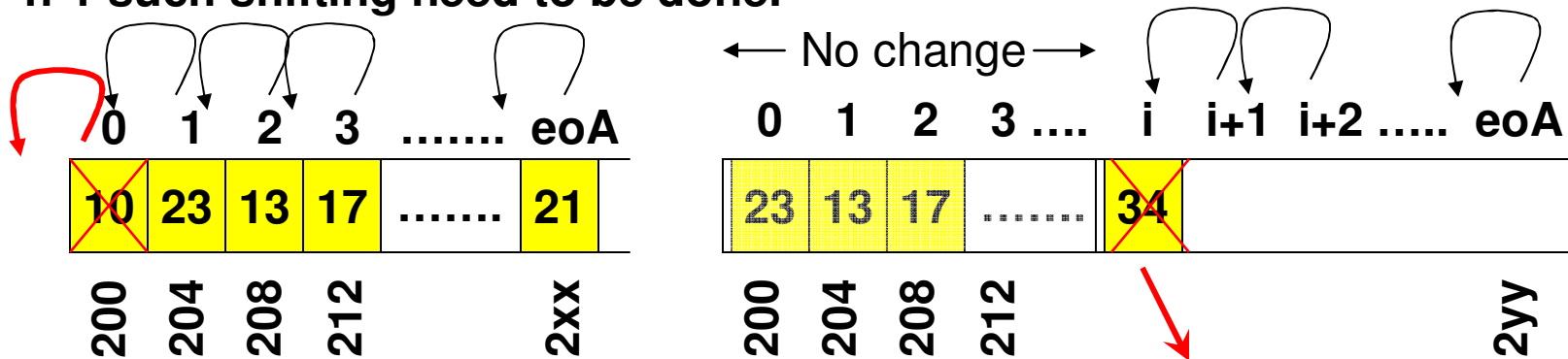
```
int read(int index){  
    return array[index];  
}  
  
void modifyElement(int index, int data){  
    array[index] = data;  
}  
  
void deleteElement(int deleteIndex){  
    // shift elements one cell to the left starting from  
    // deleteIndex+1 to endOfArray-1  
    // i.e., move element at deleteIndex + 1 to deleteIndex and so on  
  
    for (int index = deleteIndex; index < endOfArray; index++)  
        array[index] = array[index+1];  
  
    endOfArray--;  
}  
  
int countList(){  
    int count = 0;  
    for (int index = 0; index <= endOfArray; index++)  
        count++;  
  
    return count;  
}
```

(for both C++ and Java)

Time complexity analysis for 'Delete': Dynamic List ADT as an Array

Delete operation

(i) Worst case: If the element to be deleted is the first element (at index 0) in the array, then the subsequent elements have to be shifted one position to the left, starting from index 1 to endOfArray (eoA). If $eoA = n-1$, then $n-1$ such shifting need to be done.



(ii) Best case: If the element to be deleted is at the end of the array, no shifting is needed.

(iii) In general, if the element to be deleted is at index i , then the elements from index $i+1$ to endOfArray need to be shifted one cell to the left.

Time complexity for delete operation: $O(n)$

Code 2: C++ main function

```
int main(){  
  
    int listSize;  
  
    cout << "Enter list size: ";  
    cin >> listSize;  
  
    List integerList(1);  
  
    for (int i = 0; i < listSize; i++){  
  
        int value;  
        cout << "Enter element # " << i << " : ";  
        cin >> value;  
  
        integerList.insert(i, value);  
  
    }  
}
```

We will set the maximum size of the list to 1
and double it as and when needed

Code 2: Java main function

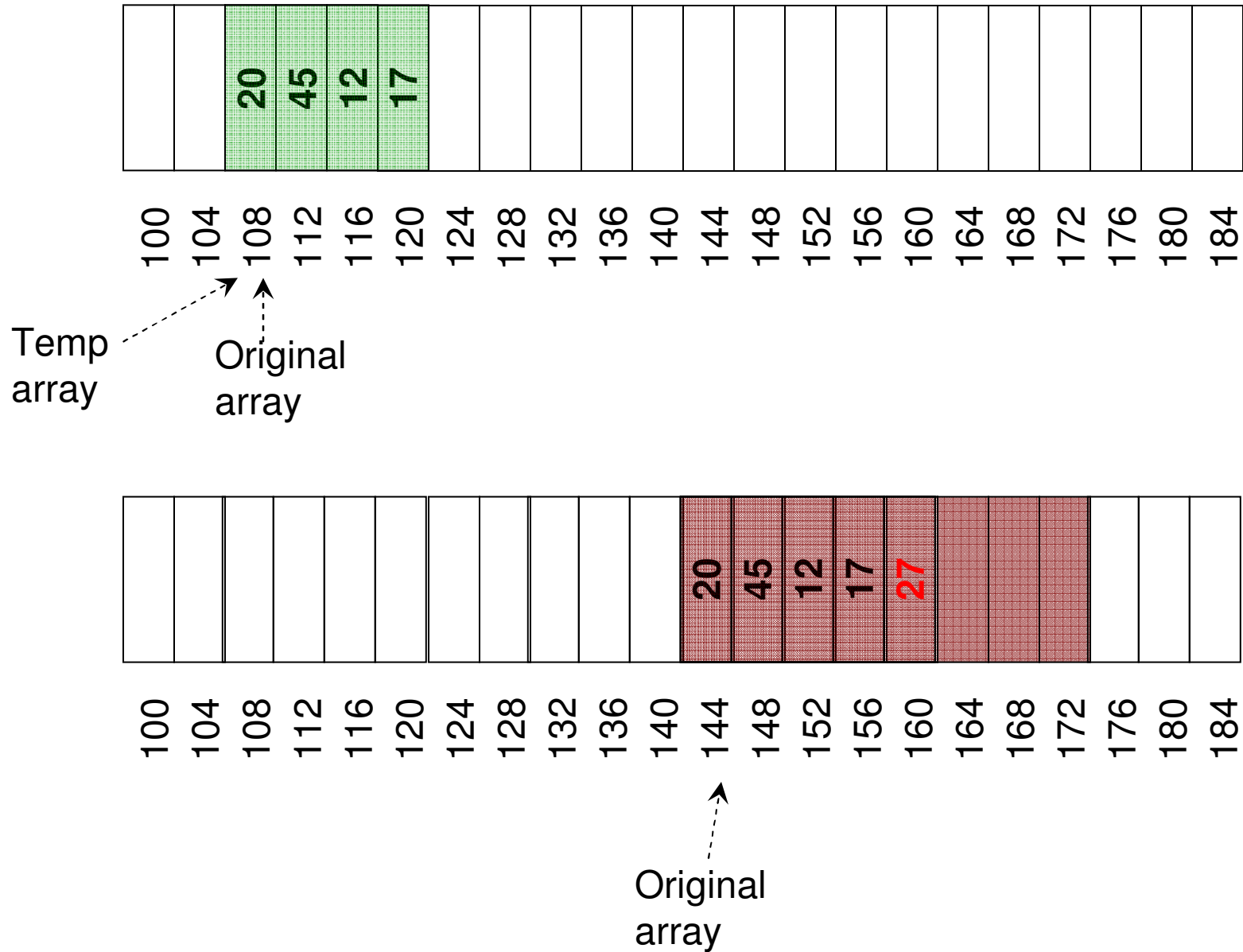
```
class DynamicListArray{  
    public static void main(String[] args){  
        int listSize;  
        Scanner input = new Scanner(System.in);  
        System.out.print("Enter list size: ");  
        listSize = input.nextInt();  
        List integerList = new List(1);  
        for (int i = 0; i < listSize; i++){  
            int value;  
            System.out.print("Enter element # " + i + " : ");  
            value = input.nextInt();  
            integerList.insert(i, value);  
        }  
    }  
}
```

We will set the maximum size
of the list to 1
and double it as and when needed

Pros and Cons of Implementing Dynamic List using Array

- Pros: $\Theta(1)$ time to read or modify an element at a particular index
- Cons: $O(n)$ time to insert or delete an element (at any arbitrary position)
- Note: Array is a contiguous block of memory
- When we double the array size (to handle the need for more space), the memory management system of the OS needs to search for contiguous blocks of memory that is double the previous array size.
 - Sometimes, it becomes difficult to allocate a contiguous block of memory, if the requested array size is larger.
- After we double the size (say from 50,000 to 100,000 to insert just one more element), the rest of the array remains unused. However, increasing the size of the array one element at a time is time consuming too.
 - The copy operation involved during resizing the array is also time consuming

Insert Operation (incl. Relocation and Doubling the Size of the Array)



Linked List

- A Linked List stores the elements of the 'List' in separate memory locations and we keep track of the memory locations as part of the information stored with an element (called a node).
 - A 'node' in a Linked List contains the data value as well as the address of the next node.
- Singly Linked List: Each node contains the address of the node with the subsequent value in the list. There is also a head node that points to the first node in the list.

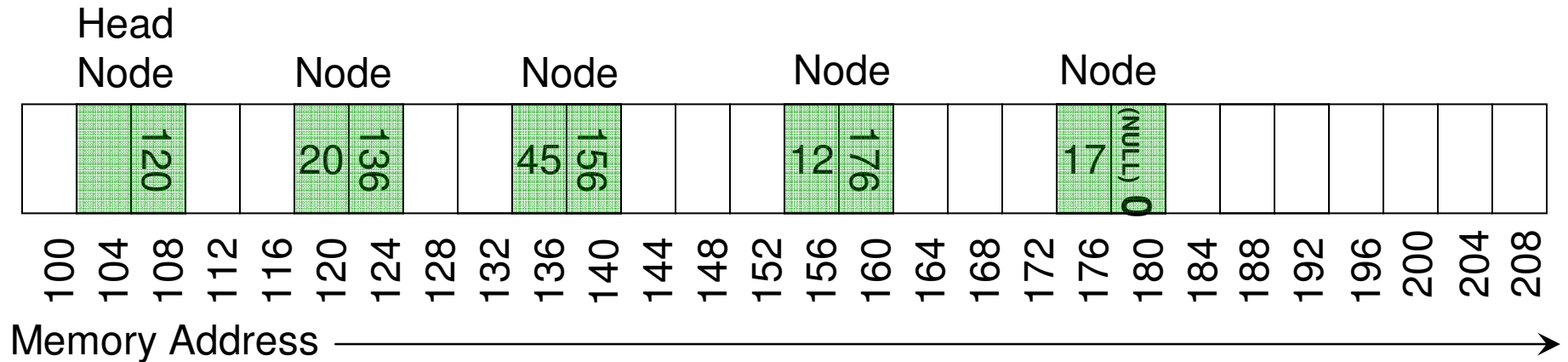
Data **With singly linked list – we can traverse only in one direction**
nextNodePtr

- Doubly Linked List: Each node contains the address of the node with the subsequent value as well as the address of the node with the preceding value. There is also a head node pointing to the first node in the list and a tail node pointing to the last node in the list.

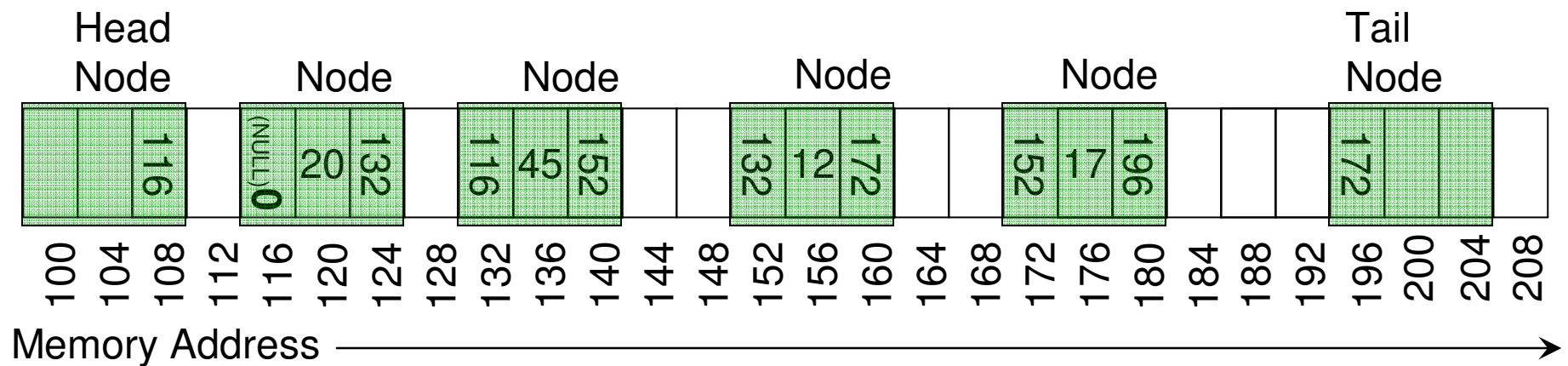
prevNodePtr
Data **With doubly linked list – we can traverse in both directions**
nextNodePtr

- Note: Memory address can be represented in 4 bytes. Hence, each pointer or reference to a memory will take 4 bytes of space.

Singly Linked List



Doubly Linked List



Linked List vs. Arrays: Memory Usage

	Data size	Next Node Ptr	Prev Node Ptr	Node Size
Singly Linked List	4 (int)	4	N/A	8 bytes
Singly Linked List	32	4	N/A	36 bytes
Doubly Linked List	4 (int)	4	4	12 bytes
Doubly Linked List	32	4	4	40 bytes

An array is usually considered to take space that is half the number of elements in it. Still, it looks like the Linked Lists will take a larger memory compared to an array. But, it is not always the case.

Consider a scenario wherein we had an array of size 64,000 objects (each of size 32 bytes) and we doubled it to 128,000 objects to insert a new object.

There a total of 64,001 objects in the List.

Array-based implementation will now hold up $128,000 * 32 \text{ bytes} = 40,96,000 \text{ bytes}$ in memory.

A singly linked list based implementation will hold $(64,001 + 1 \text{ head node}) * 36 \text{ bytes} = 23,04,072 \text{ bytes}$ in memory.

A doubly linked list based implementation will hold $(64,001 + 1 \text{ head node} + 1 \text{ tail node}) * 40 \text{ bytes} = 25,60,120 \text{ bytes}$ in memory.

Linked List vs. Arrays: Memory Usage

	Data size	Next Ptr/Ref	Prev/Ptr	Node Size
Singly Linked List	4 (int)	4	N/A	8 bytes
Singly Linked List	32	4	N/A	36 bytes
Doubly Linked List	4 (int)	4	4	12 bytes
Doubly Linked List	32	4	4	40 bytes

On the other hand, consider a scenario wherein we had an array of size 4,000 integers doubled to 8,000 integers to insert the 4,001th integer in the List.

There are a total of 4,001 integers in the List.

An array-based implementation will now hold $8,000 * 4 = 32,000$ bytes in memory.

A singly linked list-based implementation will now hold $(4,001 + 1 \text{ head node}) * 8 = 32,016$ bytes in memory.

A doubly linked list-based implementation will now hold $(4,001 + 1 \text{ head node} + 1 \text{ tail node}) * 12 = 48,036$ bytes in memory.

Linked List vs. Arrays: Time Complexity

	Array	Singly Linked List	Doubly Linked List
Read/Modify	$\Theta(1)$	$O(n)$	$O(n)$
Insert	$O(n)$	$O(n)$	$O(n)$
Delete	$O(n)$	$O(n)$	$O(n)$
isEmpty	$\Theta(1)$	$\Theta(1)$	$\Theta(1)$
Count	$O(n)$	$O(n)$	$O(n)$

We typically use arrays if there are more frequent read/modify operations compared to Insert/Delete

We typically use Linked Lists if there are more frequent insert/delete operations compared to read/modify

Note: With arrays, Insert operations are more time consuming if need to be done at the smaller indices. With singly linked lists, insert operations are more time consuming if done towards the end of the list. A doubly linked list could be traversed either from the head or the tail, and hence if a priori information is know about the sequence of elements in the list, traversal could be initiated from the head or tail, and the traversal time could be lower than a singly linked list. Still $O(n)$ time though!

Singly Linked List Implementation (Code 3)

Class Node

C++

```
private:  
    int data;  
    Node* nextNodePtr;
```

```
public:  
    Node(){  
  
    void setData(int d){  
        data = d;  
    }  
  
    int getData(){  
        return data;  
    }  
}
```

Java

```
private int data;  
private Node nextNodePtr;
```

```
public Node(){  
  
    public void setData(int d){  
        data = d;  
    }  
  
    public int getData(){  
        return data;  
    }  
}
```

Singly Linked List Implementation

Class Node

C++

```
public:
    void setNextNodePtr(Node* nodePtr){
        nextNodePtr = nodePtr;
    }

    Node* getNextNodePtr(){
        return nextNodePtr;
    }
```

Java

```
public void setNextNodePtr(Node nodePtr){
    nextNodePtr = nodePtr;
}

public Node getNextNodePtr(){
    return nextNodePtr;
}
```


Singly Linked List: Class List

Class Node (C++) Overview

```
private:
    int data;
    Node* nextNodePtr;

public:
    Node( )
    void setData(int)
    int getData()
    void setNextNodePtr(Node* )
    Node* getNextNodePtr( )
```

Class Node (Java) Overview

```
private int data;
private Node nextNodePtr;

public Node( )
public void setData(int)
public int getData()
public void setNextNodePtr(Node* )
public Node getNextNodePtr( )
```

Class List (C++)

```
private:
    Node *headPtr;

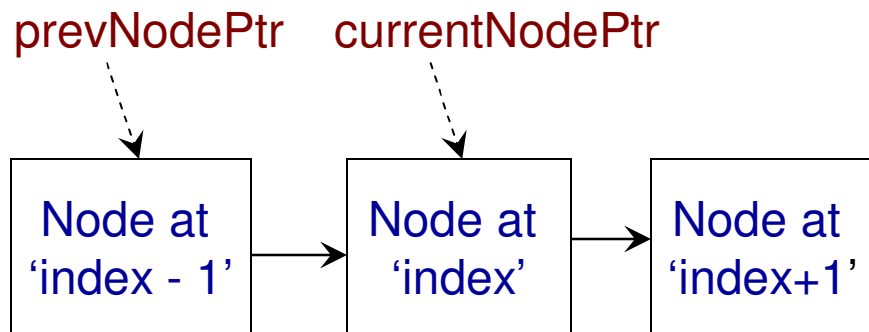
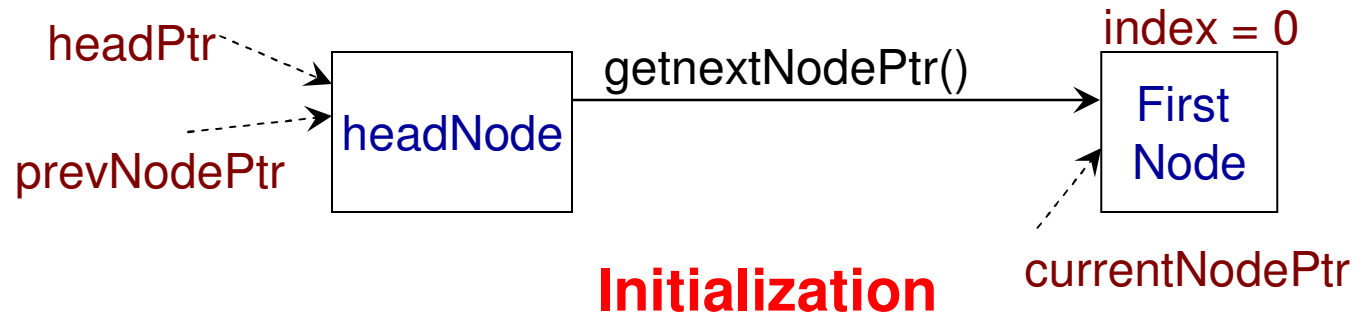
public:
    List(){
        headPtr = new Node();
        headPtr->setNextNodePtr(0);
    }
```

Class List (Java)

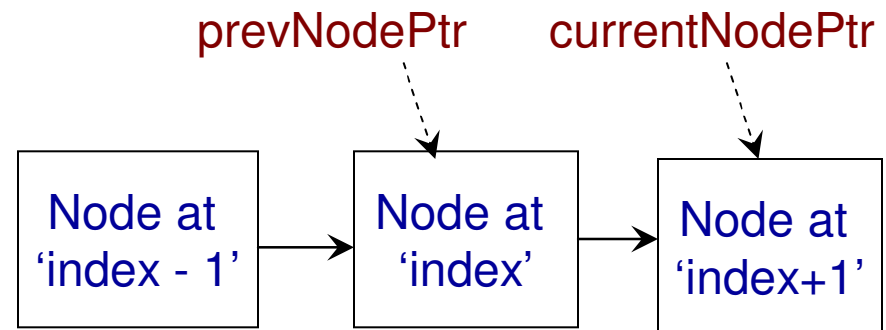
```
private Node headPtr;

public List(){
    headPtr = new Node();
    headPtr.setNextNodePtr(null);
}
```

Insert and InsertAtIndex Functions

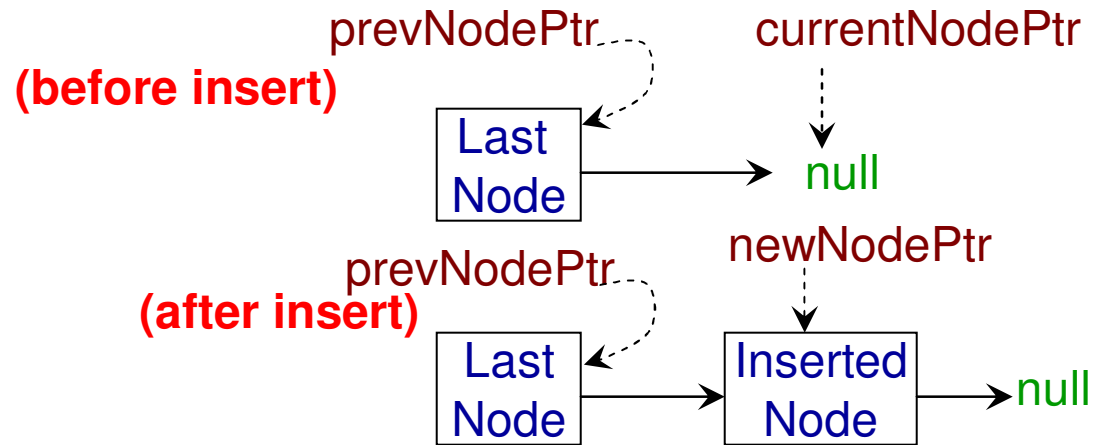


**At the beginning of
an iteration inside
the 'while' loop**

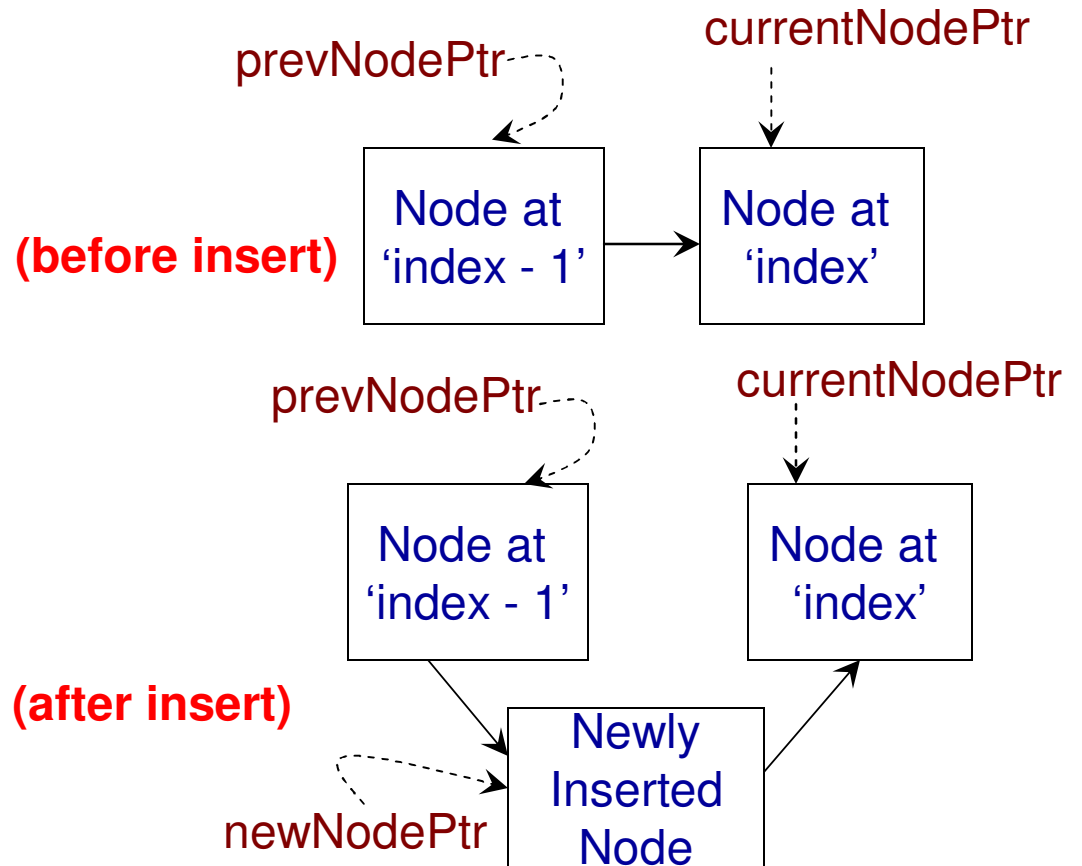


**At the end of
an iteration inside
the 'while' loop**

Insert Function (at the end of the List)



InsertAtIndex Function



Class List (C++)

```
void insert(int data){
```

```
    Node* currentNodePtr = headPtr->getNextNodePtr();
```

```
    Node* prevNodePtr = headPtr;
```

```
    while (currentNodePtr != 0){
```

```
        prevNodePtr = currentNodePtr;
```

```
        currentNodePtr = currentNodePtr->getNextNodePtr();
```

```
    }
```

```
    Node* newNodePtr = new Node();
```

```
    newNodePtr->setData(data);
```

```
    newNodePtr->setNextNodePtr(0);
```

```
    prevNodePtr->setNextNodePtr(newNodePtr);
```

```
}
```

If the nextNodePtr for the headPtr points to null (0), then the list is empty. Otherwise, the list has at least one node.

Move the currentNode ptr from first node in the list to end of the list. When we come out of the 'while' loop, the prevNode ptr is the last node in the list and currentNode ptr points to null (0).

```
bool isEmpty(){
```

```
    if (headPtr->getNextNodePtr() == 0)
```

```
        return true;
```

```
    return false;
```

```
}
```

Class List (Java)

```
public void insert(int data){
```

```
    Node currentNodePtr = headPtr.getNextNodePtr();
```

```
    Node prevNodePtr = headPtr;
```

```
    while (currentNodePtr != null){
```

```
        prevNodePtr = currentNodePtr;
```

```
        currentNodePtr = currentNodePtr.getNextNodePtr();
```

```
    }
```

```
    Node newNodePtr = new Node();
```

```
    newNodePtr.setData(data);
```

```
    newNodePtr.setNextNodePtr(null);
```

```
    prevNodePtr.setNextNodePtr(newNodePtr);
```

```
}
```

If the nextNodePtr for the headPtr points to null (0), then the list is empty. Otherwise, the list has at least one node.

```
public boolean isEmpty(){
```

```
    if (headPtr.getNextNodePtr() == null)
```

```
        return true;
```

```
    return false;
```

```
}
```

Move the currentNode ptr from first node in the list to end of the list. When we come out of the 'while' loop, the prevNode ptr is last node in the list and currentNode ptr points to null (0).

Class List (C++)

```
void insertAtIndex(int insertIndex, int data){
```

```
    Node* currentNodePtr = headPtr->getNextNodePtr();
```

```
    Node* prevNodePtr = headPtr;
```

```
    int index = 0;
```

```
    while (currentNodePtr != 0){
```

```
        if (index == insertIndex)
            break;
```

```
        prevNodePtr = currentNodePtr;
```

```
        currentNodePtr = currentNodePtr->getNextNodePtr();
```

```
        index++;
```

```
    }
```

```
    Node* newNodePtr = new Node();
```

```
    newNodePtr->setData(data);
```

```
    newNodePtr->setNextNodePtr(currentNodePtr);
```

```
    prevNodePtr->setNextNodePtr(newNodePtr);
```

```
}
```

During the beginning and end of the while loop,
the value for 'index' corresponds to the

Position of the currentNode ptr and prevNode ptr
corresponds to index-1.

If index equals insertIndex, we break from
the while loop and insert the new node
at the index in between prevNode and
currentNode.

Class List (Java)

```
public void insertAtIndex(int insertIndex, int data){
```

```
    Node currentNodePtr = headPtr.getNextNodePtr();
```

```
    Node prevNodePtr = headPtr;
```

```
    int index = 0;
```

```
    while (currentNodePtr != null){
```

```
        if (index == insertIndex)
            break;
```

```
        prevNodePtr = currentNodePtr;
```

```
        currentNodePtr = currentNodePtr.getNextNodePtr();
```

```
        index++;
```

```
    }
```

```
    Node newNodePtr = new Node();
```

```
    newNodePtr.setData(data);
```

```
    newNodePtr.setNextNodePtr(currentNodePtr);
```

```
    prevNodePtr.setNextNodePtr(newNodePtr);
```

```
}
```

During the beginning and end of the while loop,
the value for 'index' corresponds to the
Position of the currentNode ptr and prevNode ptr
corresponds to index-1.

If index equals insertIndex, we break from
the while loop and insert the new node
at the index in between prevNode and
currentNode.

Class List (C++)

```
int read(int readIndex){  
    Node* currentNodePtr = headPtr->getNextNodePtr();  
    Node* prevNodePtr = headPtr;  
    int index = 0;  
  
    while (currentNodePtr != 0){  
        if (index == readIndex)  
            return currentNodePtr->getData();  
  
        prevNodePtr = currentNodePtr;  
        currentNodePtr = currentNodePtr->getNextNodePtr();  
  
        index++;  
    }  
    return -1; // an invalid value indicating index is out of range  
}
```

The 'index' value corresponds to the Position of the currentNode ptr and index-1 corresponds to prevNode ptr

Class List (Java)

```
public int read(int readIndex){  
    Node currentNodePtr = headPtr.getNextNodePtr();  
    Node prevNodePtr = headPtr;  
    int index = 0;  
  
    while (currentNodePtr != null){  
        if (index == readIndex)  
            return currentNodePtr.getData();  
  
        prevNodePtr = currentNodePtr;  
        currentNodePtr = currentNodePtr.getNextNodePtr();  
  
        index++;  
    }  
    return -1;  
}
```

The 'index' value corresponds to the Position of the currentNode ptr and index-1 corresponds to prevNode ptr

Class List (C++)

```
void modifyElement(int modifyIndex, int data){  
    Node* currentNodePtr = headPtr->getNextNodePtr();  
    Node* prevNodePtr = headPtr;  
    int index = 0;  
  
    while (currentNodePtr != 0){  
  
        if (index == modifyIndex){  
            currentNodePtr->setData(data);  
            return;  
        }  
  
        prevNodePtr = currentNodePtr;  
        currentNodePtr = currentNodePtr->getNextNodePtr();  
  
        index++;  
    }  
}
```

Class List (Java)

```
public void modifyElement(int modifyIndex, int data){
    Node currentNodePtr = headPtr.getNextNodePtr();
    Node prevNodePtr = headPtr;
    int index = 0;

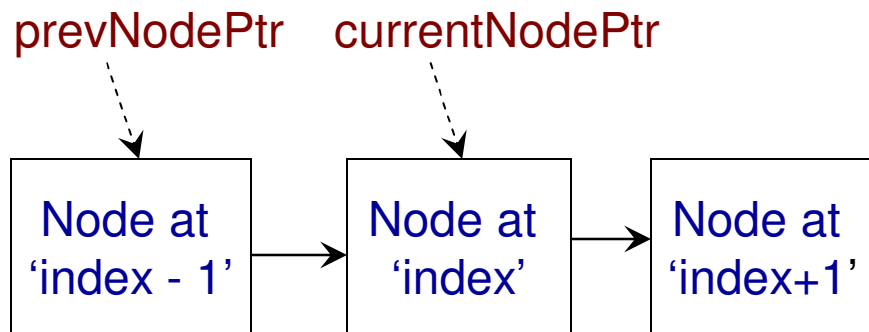
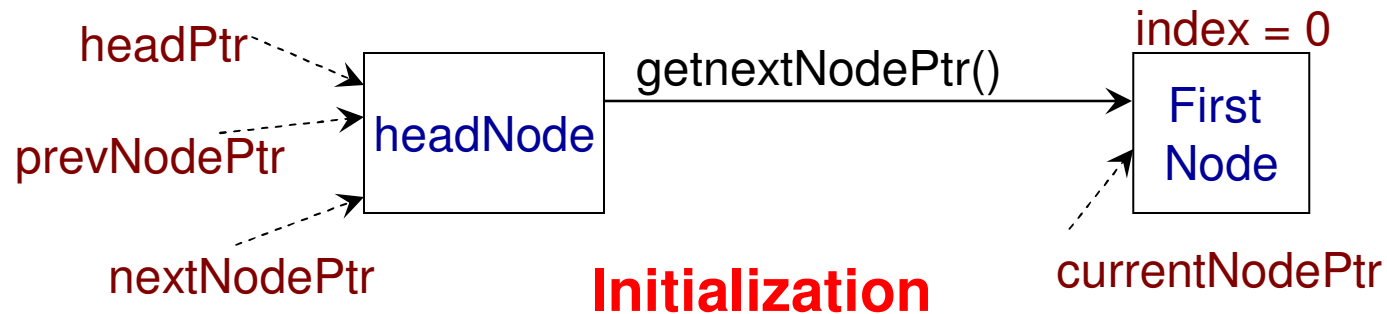
    while (currentNodePtr != null){

        if (index == modifyIndex){
            currentNodePtr.setData(data);
            return;
        }

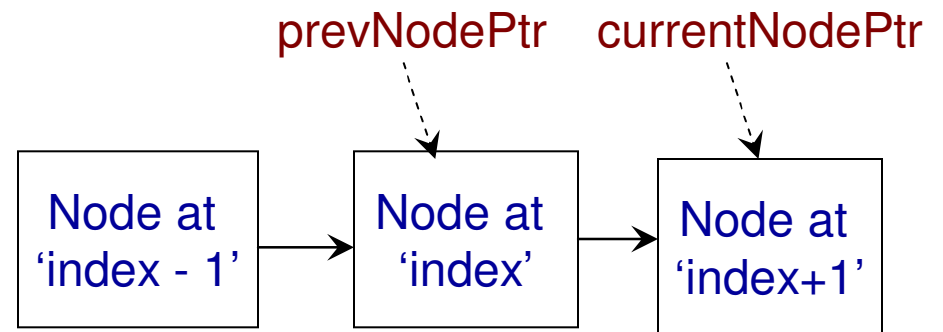
        prevNodePtr = currentNodePtr;
        currentNodePtr = currentNodePtr.getNextNodePtr();

        index++;
    }
}
```

Delete (deleteIndex) Function



**At the beginning of
an iteration inside
the 'while' loop**

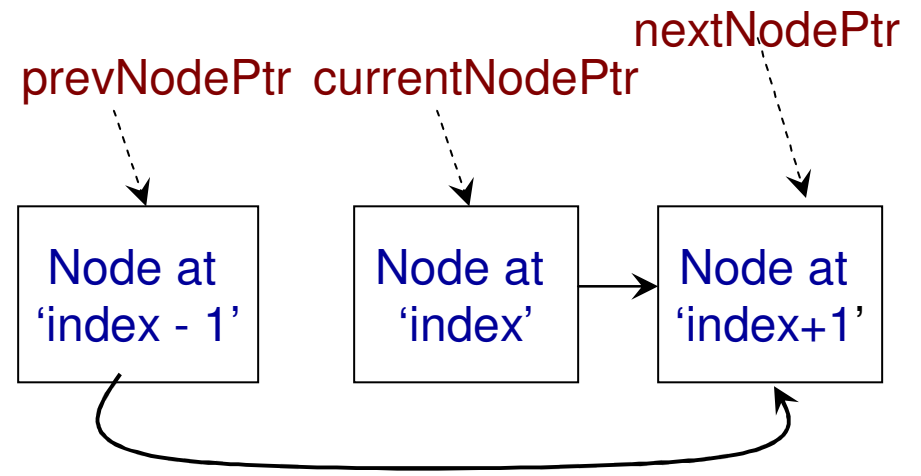
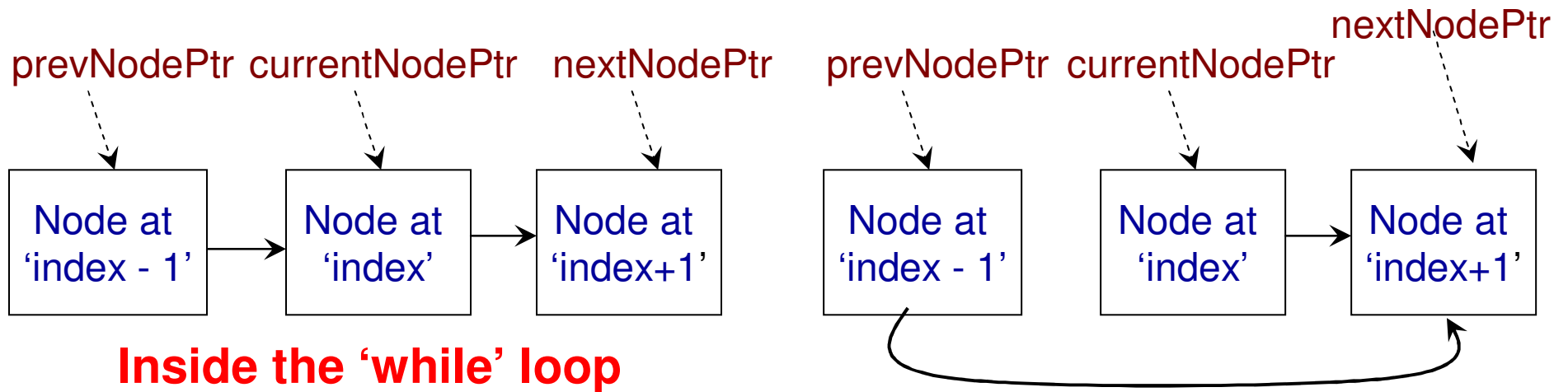


**At the end of
an iteration inside
the 'while' loop**

When $\text{index} \neq \text{deleteIndex}$

Delete (deleteIndex) Function

When $\text{index} == \text{deleteIndex}$



**currentNode at index = deleteIndex
is disconnected from the Linked List**

Class List (C++)

```
void deleteElement(int deleteIndex){
    Node* currentNodePtr = headPtr->getNextNodePtr();
    Node* prevNodePtr = headPtr;
    Node* nextNodePtr = headPtr;
    int index = 0;

    while (currentNodePtr != 0){

        if (index == deleteIndex){
            nextNodePtr = currentNodePtr->getNextNodePtr();
            break;
        }

        prevNodePtr = currentNodePtr;
        currentNodePtr = currentNodePtr->getNextNodePtr();

        index++;
    }

    prevNodePtr->setNextNodePtr(nextNodePtr);
}
```

The next node for 'prevNode' ptr
is now 'next node' and not
'current node'

Class List (Java)

```
public void deleteElement(int deleteIndex){  
    Node currentNodePtr = headPtr.getNextNodePtr();  
    Node prevNodePtr = headPtr;  
    Node nextNodePtr = headPtr;  
    int index = 0;  
  
    while (currentNodePtr != null){  
        if (index == deleteIndex){  
            nextNodePtr = currentNodePtr.getNextNodePtr();  
            break;  
        }  
  
        prevNodePtr = currentNodePtr;  
        currentNodePtr = currentNodePtr.getNextNodePtr();  
  
        index++;  
    }  
    prevNodePtr.setNextNodePtr(nextNodePtr);  
}
```

The next node for 'prevNode' ref
is now 'next node' and not
'current node'

Iterative Print

```
void IterativePrint(){           Class List (C++)  
    Node* currentNodePtr = headPtr->getNextNodePtr();  
  
    while (currentNodePtr != 0){  
        cout << currentNodePtr->getData() << " ";  
        currentNodePtr = currentNodePtr->getNextNodePtr();  
    }  
    cout << endl;  
}
```

```
public void IterativePrint(){ Class List (Java)  
    Node currentNodePtr = headPtr.getNextNodePtr();  
  
    while (currentNodePtr != null){  
        System.out.print(currentNodePtr.getData()+" ");  
        currentNodePtr = currentNodePtr.getNextNodePtr();  
    }  
    System.out.println();  
}
```


Recursion

- Recursion: A function calling itself.
- Recursions are represented using a recurrence relation (incl. a base or terminating condition)
- Example 1
- $\text{Factorial}(n) = n * \text{Factorial}(n-1)$ for $n > 0$
- $\text{Factorial}(n) = 1$ for $n = 0$

```
Factorial(n)
  if (n == 0)
    return 1;
  else
    return n * Factorial(n-1)
```

```
Factorial(0) = 1
Factorial(1) = 1 * Factorial(0)
Factorial(2) = 2 * Factorial(1)
Factorial(3) = 3 * Factorial(2)
Factorial(4) = 4 * Factorial(3)
Factorial(5) = 5 * Factorial(4)
```

```
int main(){
```

C++

```
int arraySize;
```

```
cout << "Enter an array size: ";
```

```
cin >> arraySize;
```

```
int maxValue;
```

```
cout << "Enter the max. value of an element: ";
```

```
cin >> maxValue;
```

```
srand(time(NULL));
```

Initialize the random number generator with a seed that corresponds to the current system time

```
int array[maxValue];
```

```
for (int i = 0; i < arraySize; i++){  
    array[i] = rand() % maxValue;  
}
```

The random numbers are generated from 0 to maxValue – 1

```
cout << "IterativePrint: ";
```

```
IterativePrint(array, arraySize);
```

```
cout << "RecursivePrint: ";
```

```
RecursivePrint(array, arraySize, 0);
```

```
return 0;
```

```
}
```

Example (Code 4) to Illustrate Recursion and Random Number Generation

Headers to be included

```
#include <iostream>
```

```
#include <stdlib.h> // random number
```

```
#include <time.h> // for time
```

```
using namespace std;
```

Code 4: C++

```
void IterativePrint(int* arrayPtr, int size){  
    for (int index = 0; index < size; index++)  
        cout << arrayPtr[index] << " ";  
  
    cout << endl;  
}
```

```
void RecursivePrint(int* arrayPtr, int size, int printIndex){  
    if (printIndex == size){  
        cout << endl;  
        return;  
    }  
    cout << arrayPtr[printIndex] << " "; Printing in the forward order  
  
    RecursivePrint(arrayPtr, size, printIndex+1);  
  
    cout << arrayPtr[printIndex] << " "; Printing in the reverse order  
}
```

Recursion

Seq

	0	1	2	3
array	14	21	33	45

Seq	2	4	6	8
	14	21	33	45
	45	33	21	14

Seq	12	14	16	18
-----	----	----	----	----

10	11	if (printIndex == arraySize){ // 4 == 4 cout << endl; return; }
8	9	cout << arrayPtr[3] << " "; RecursivePrint(arrayPtr, arraySize = 4, printIndex = 4)
12		cout << arrayPtr[3] << " ";
6	7	cout << arrayPtr[2] << " "; RecursivePrint(arrayPtr, arraySize = 4, printIndex = 3)
13		cout << arrayPtr[2] << " ";
4	5	cout << arrayPtr[1] << " "; RecursivePrint(arrayPtr, arraySize = 4, printIndex = 2)
14		cout << arrayPtr[1] << " ";
2	3	cout << arrayPtr[0] << " "; RecursivePrint(arrayPtr, arraySize = 4, printIndex = 1)
15		cout << arrayPtr[0] << " ";
		@main
1		RecursivePrint(array, arraySize = 4, printIndex = 0)

`import java.util.*;` **Java**

`class arrayRecursive{`

`public static void IterativePrint(int arrayRef[], int size){`

`for (int index = 0; index < size; index++)
 System.out.print(arrayRef[index] + " ");`

`System.out.println();`

`}`

`public static void RecursivePrint(int arrayPtr[], int size, int printIndex){`

`if (printIndex == size){
 System.out.println();
 return;`

`}
 System.out.print(arrayPtr[printIndex] + " ");`

`RecursivePrint(arrayPtr, size, printIndex+1);`

`System.out.print(arrayPtr[printIndex] + " ");`

`}`

**Example (Code 4)
to Illustrate
Recursion and
Random Number
Generation**

Java

```
public static void main(String[] args){
```

```
    Scanner input = new Scanner(System.in);
```

```
    int arraySize;
```

```
    System.out.print("Enter an array size: ");
```

```
    arraySize = input.nextInt();
```

```
    int maxValue;
```

```
    System.out.print("Enter the max. value of an element: ");
```

```
    maxValue = input.nextInt();
```

```
    Random randGen = new Random(System.currentTimeMillis());
```

```
    int array[] = new int[arraySize];
```

```
    for (int i = 0; i < arraySize; i++){  
        array[i] = randGen.nextInt(maxValue);  
    }
```

```
    System.out.print("IterativePrint: ");
```


```
    IterativePrint(array, arraySize);
```

```
    System.out.print("RecursivePrint: ");
```

```
    RecursivePrint(array, arraySize, 0);
```

```
}
```

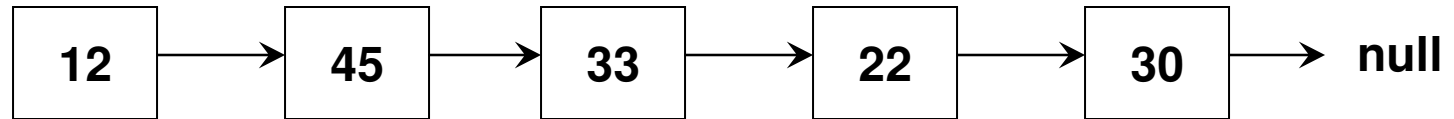
Initialize the random number generator with a seed that corresponds to the current system time



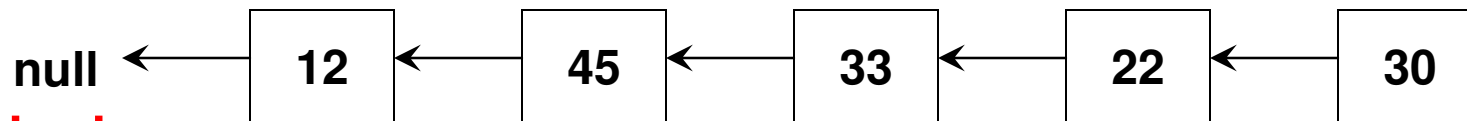
The random numbers are generated from 0 to $\text{maxValue} - 1$

Reversing a Linked List

Input



Output



Logic

Maintain three pointers

currentNode, nextNode, prevNode

Enter the loop if currentNode is not null

After entering the loop,

Step 1: set nextNode = currentNode->getNextNodePtr()

Now that there is a pointer to the next node of currentNode, reverse the direction for the next node of currentNode

Step 2: currentNode->setNextNodePtr(prevNode)

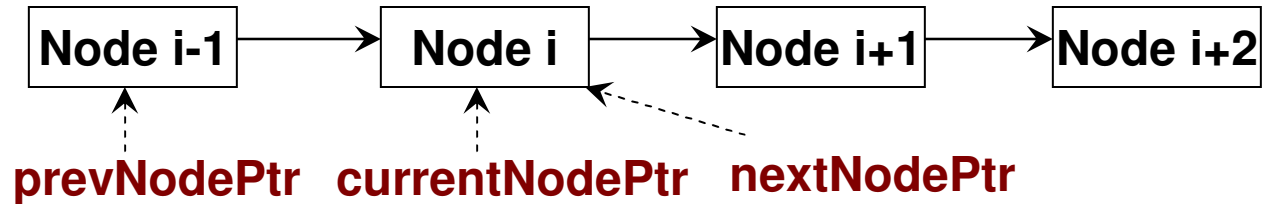
Now prepare for the next iteration,

Step 3: set prevNode = currentNode

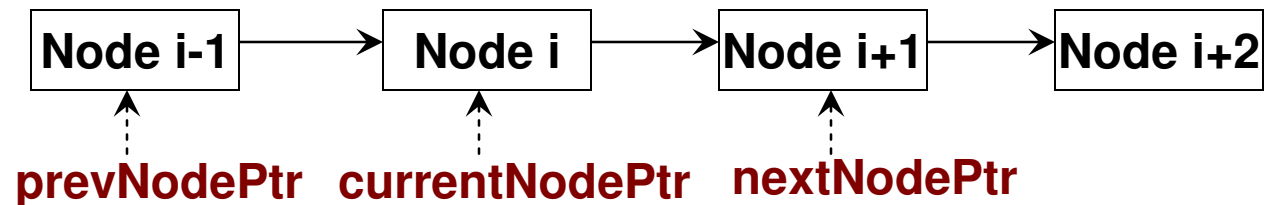
Step 4: set currentNode = nextNode

Reversing a Linked List (logic)

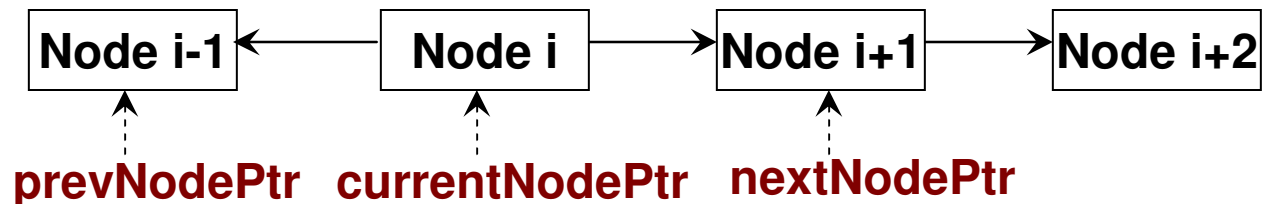
At the time of entering the loop:



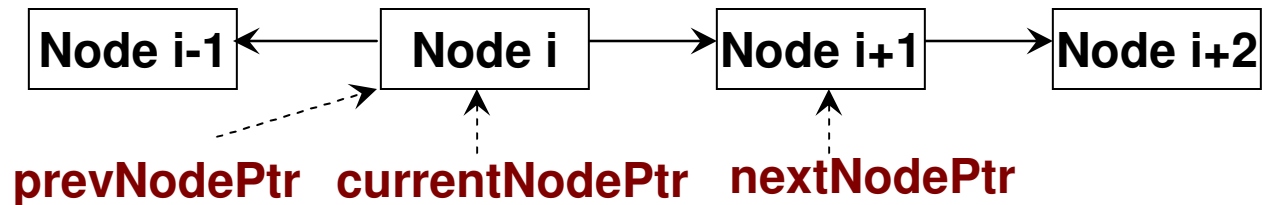
Step 1:



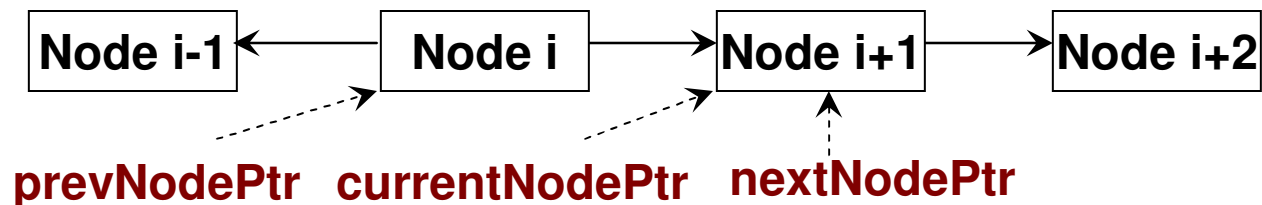
Step 2:



Step 3:



Step 4:



Reversing a Singly Linked List (Code 5): C++

```
void reverseList(){  
    Node* currentNodePtr = headPtr->getNextNodePtr();  
    Node* prevNodePtr = 0;  
    Node* nextNodePtr = currentNodePtr;  
  
    while (currentNodePtr != 0){  
        nextNodePtr = currentNodePtr->getNextNodePtr(); // Step 1  
        currentNodePtr->setNextNodePtr(prevNodePtr); // Step 2  
        prevNodePtr = currentNodePtr; // Step 3  
        currentNodePtr = nextNodePtr; // Step 4  
    }  
    headPtr->setNextNodePtr(prevNodePtr);  
}
```

Reversing a Singly Linked List (Code 5): Java

```
public void reverseList(){  
    Node currentNodePtr = headPtr.getNextNodePtr();  
    Node prevNodePtr = null;  
    Node nextNodePtr = currentNodePtr;  
  
    while (currentNodePtr != null){  
        nextNodePtr = currentNodePtr.getNextNodePtr(); // Step 1  
        currentNodePtr.setNextNodePtr(prevNodePtr); // Step 2  
        prevNodePtr = currentNodePtr; // Step 3  
        currentNodePtr = nextNodePtr; // Step 4  
    }  
  
    headPtr.setNextNodePtr(prevNodePtr);  
}
```