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## CSC 228-60 Data Structures and Algorithms, Spring 2018

Instructor: Dr. Natarajan Meghanathan

Exam 3 (Take Home Part)
Max. Points: 100
Due on: April 25th @ 9 AM, in-class for the 12 PM section CSC 228-60
Print this exam and answer in the space provided. Staple and submit in class at the above time.
Given an array of integers, do the following (SHOW ALL THE STEPS; just writing the final answer will get only ZERO):
(a-15 pts) Construct a max heap of the array. Show the initial essentially complete binary tree and the transformation of the binary tree to a max heap via the reheapify operations at the indices of the internal nodes (as shown in the slides).
(b-15 pts) Sort the max heap version of the array obtained from (a) to obtain a sorted array of integers. Show the structural changes in the max heap in each iteration.
(c-7 pts) Transform the max heap of (a) to a binary search tree.
(d - 8 pts ) For the binary search tree obtained in (c), determine the average number of comparisons for a successful search and the average number of comparisons for an unsuccessful search.
(e-8 pts) Use the sorted array of (b) to construct a binary search tree.
(f - 7 pts) For the binary search tree obtained in (e), determine the average number of comparisons for a successful search and the average number of comparisons for an unsuccessful search.
(g-7 pts) Construct a hash table of the given array using a hash function $\mathrm{H}(\mathrm{K})=\mathrm{K} \bmod 5$.
( $\mathrm{h}-8 \mathrm{pts}$ ) For the hash table of (g), determine the average number of comparisons for a successful search and the worst case number of comparisons for an unsuccessful search.
(i - 25 pts ) Consider the elements of the array assigned to you are known only one at a time. Construct a sequence of priority queues (as max heaps) with the insertion (enqueue) of one element at a time, as shown in the slides.

| 1 | Biruk Abate | $[6$, | 22, | 1, | 12, | 19, | 10, | 1, | 17, | 17, | 19, | 15, | $27]$ |
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| 2 | Dakarai Armstead | $[14$, | 6, | 19, | 16, | 23, | 2, | 18, | 4, | 26, | 23, | 7, | $1]$ |
| 3 | Deonte Buckner | $[30$, | 20, | 26, | 6, | 29, | 3, | 7, | 25, | 4, | 1, | 29, | $27]$ |
| 4 | Nzefili Chukwuma | $[11$, | 4, | 18, | 24, | 18, | 28, | 12, | 2, | 14, | 7, | 27, | $11]$ |
| 5 | Brunti Givens | $[14$, | 3, | 16, | 22, | 23, | 24, | 28, | 17, | 19, | 15, | 2, | $16]$ |
| 6 | Kamera Gorden | $[14$, | 18, | 18, | 11, | 9, | 12, | 15, | 28, | 1, | 26, | 18, | $11]$ |
| 7 | Damon Kirk | $[3$, | 14, | 21, | 19, | 27, | 28, | 4, | 4, | 28, | 6, | 29, | $24]$ |
| 8 | Blair McIntosh | $[25$, | 10, | 7, | 18, | 11, | 5, | 15, | 7, | 17, | 15, | 30, | $5]$ |
| 9 | Donald Parker | $[20$, | 4, | 7, | 3, | 3, | 20, | 12, | 23, | 10, | 9, | 26, | $15]$ |
| 10 | Tavarez Stewart | $[24$, | 2, | 26, | 9, | 17, | 25, | 18, | 13, | 8, | 4, | 29, | $30]$ |
| 11 | Tanisha Thompson | $[2$, | 6, | 14, | 22, | 1, | 10, | 18, | 10, | 15, | 1, | 21, | $27]$ |
| 12 | Bryan Williams | $[5$, | 29, | 24, | 16, | 20, | 3, | 8, | 20, | 15, | 12, | 8, | $5]$ |

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