## Module 5: Hash table

1) Given an array $A=\{45,22,11,47,44,33,23,65\}$ and a hash function $H(v)=v \bmod 7$, construct a hash table and determine the average number of comparisons for a successful search and unsuccessful search.

## Module 6: Binary Tree

1) Consider a binary tree with 89 nodes. Determine the minimum possible height of the tree.
2) Given a tree, find the depth of all the leaf nodes and the height of all the internal nodes in the tree.

3) A binary tree is called a complete binary tree if each internal node has exactly two child nodes. Determine the number of leaf nodes and the number of internal nodes in a complete binary tree of height 5.
4) Given a binary tree, find the height of the internal nodes of the tree and determine whether the tree is height-balanced or not.
a)

b)

5) Given a binary tree, write down the preorder, inorder and postorder traversal of the vertices.

6) Given the inorder and postorder (or preorder) traversal of the vertices in a binary tree, construct the binary tree. Write down the preorder (or postorder) traversal of the vertices of the constructed binary tree.

Postorder: 3, 6, 9, 4, 1, 7, 8, 5, 2, 0
Inorder: 3, 1, 6, 4, 9, 0, 7, 2, 5, 8

## Module 7: Binary Search Tree

1) Given an array of integers below:
$\begin{array}{llllllll}12 & 5 & 1 & 4 & 18 & 9 & 9 & 15\end{array}$
(a) Sort the array using the Selection sort algorithm. Show the contents of the array after each iteration.
(b) Using the sorted array of integers, construct a binary search tree using the algorithm discussed in class.
(c) Determine the average number of comparisons for a successful search. Show all the work.
(d) Determine the average number of comparisons for an unsuccessful search. Show all the work.
2) Convert a given binary tree to a binary search tree without changing the structure.

