

Module 2: List ADT

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List ADT

- A collection of entities of the same data type
- List ADT (static)
 - Functionalities (logical view)
 - Store a given number of elements of a given data type
 - Write/modify an element at a particular position
 - Read an element at a particular position
- Implementation:
 - Arrays: A contiguous block of memory of a certain size, allocated at the time of creation/initialization
 - Time complexity to read and write/modify are $\Theta(1)$ each

	A[0]		A[2]			
Array index	0	1	2	3	N-1
Array, A	10	23	13	17	21
Memory address	200	204	208	212		2XX

Code 1 (C++): Static List Implementation using Arrays

```
#include <iostream>
using namespace std;

class List{
private:
    int *array;

public:
    List(int size){
        array = new int[size];
    }

    void write(int index, int data){
        array[index] = data;
    }

    int read(int index){
        return array[index];
    }
};
```

```
int main(){
    int listSize;

    cout << "Enter list size: ";
    cin >> listSize;

    List integerList(listSize);

    for (int i = 0; i < listSize; i++){
        int value;
        cout << "Enter element # " << i << " : ";
        cin >> value;
        integerList.write(i, value);
    }

    return 0;
}
```

Dynamic List ADT

- **Limitations with Static List**
 - The list size is fixed (during initialization); cannot be increased or decreased.
 - With a static list, the array is filled at the time of initialization and can be later only read or modified. A new element cannot be “inserted” after the initialization phase.
- **Key Features of a Dynamic List**
 - Be able to resize (increase or decrease) the list at run time. The list size need not be decided at the time of initialization. We could start with a list of size one and populate it as elements are to be added.
 - Be able to insert or delete an element at a particular index at any time.
- **Performance Bottleneck**
 - When we increase the size of the list (i.e., increase the size of the array that stores the elements), the contents of the array need to be copied to a new memory block, element by element. → $O(n)$ time.
 - Hence, even though, we could increase the array size by one element at a time, the ‘copy’ operation is a performance bottleneck and the standard procedure is to double the size of the array (list) whenever the list gets full.
 - A delete operation also takes $O(n)$ time as elements are to be shifted one cell to the left.

Code 2: Code for Dynamic List ADT Implementation using Arrays

Variables and Constructor (C++)

```
private:  
    int *array;  
    int maxSize;  
    int endOfArray;  
  
public:  
    List(int size){  
        maxSize = size;  
        array = new int[maxSize];  
        endOfArray = -1;  
    }
```

isEmpty (C++)

```
bool isEmpty(){  
    if (endOfArray == -1)  
        return true;  
    return false;  
}
```

Code 2: Insert Function (C++)

```
void insertAtIndex(int insertIndex, int data){
```

```
    // if the user enters an invalid insertIndex, the element is  
    // appended to the array, after the current last element
```

```
    if (insertIndex > endOfArray+1)  
        insertIndex = endOfArray+1;
```

```
    if (endOfArray == maxSize-1) Will take O(n) time each, where  
        resize(2*maxSize); n = maxSize + 1
```

```
    for (int index = endOfArray; index >= insertIndex; index--)  
        array[index+1] = array[index];
```

```
    array[insertIndex] = data;  
    endOfArray++;
```

```
}
```

```
void insert(int data){  
    if (endOfArray == maxSize-1)  
        resize(2*maxSize);  
    array[++endOfArray] = data;  
}
```

Code 2: Resize Function (C++)

```
void resize(int s){  
    // in addition to increasing, the resize function  
    // also provides the flexibility to reduce the size  
    // of the array  
    int *tempArray = array;  
    array = new int[s];  
    for (int index = 0; index < min(s, endOfArray+1); index++){  
        array[index] = tempArray[index];  
    }  
    maxSize = s;  
}
```


Have another pointer (a temporary ptr) to refer to the starting address of the memory represented by the original array

Allocating a new set of memory blocks to the 'array' variable

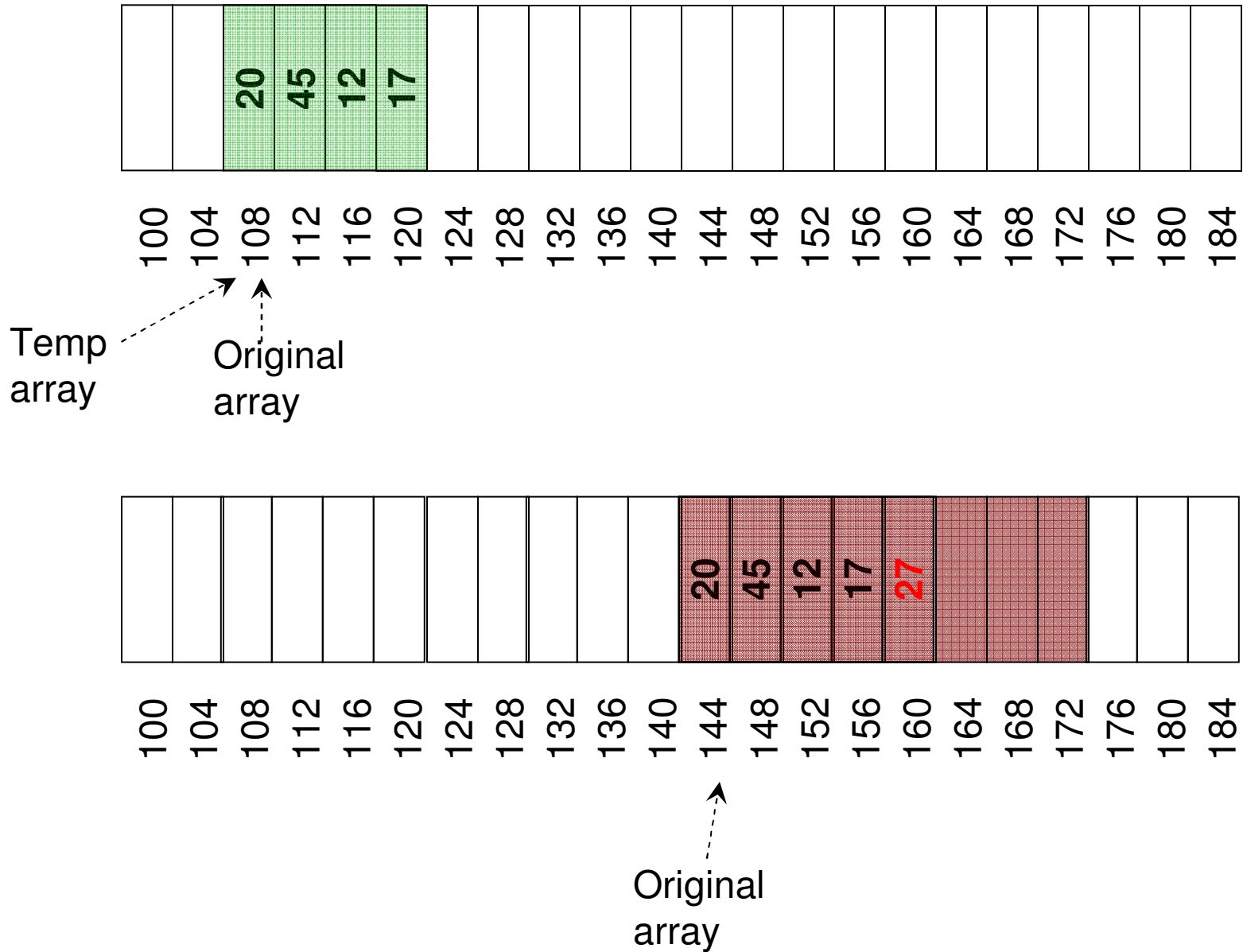
Copying back the contents pointed to by the temporary array pointer to the original array

If the array size is reduced from maxSize to s, only the first 's' elements are copied. Otherwise, all the maxElements are copied

new value of maxSize



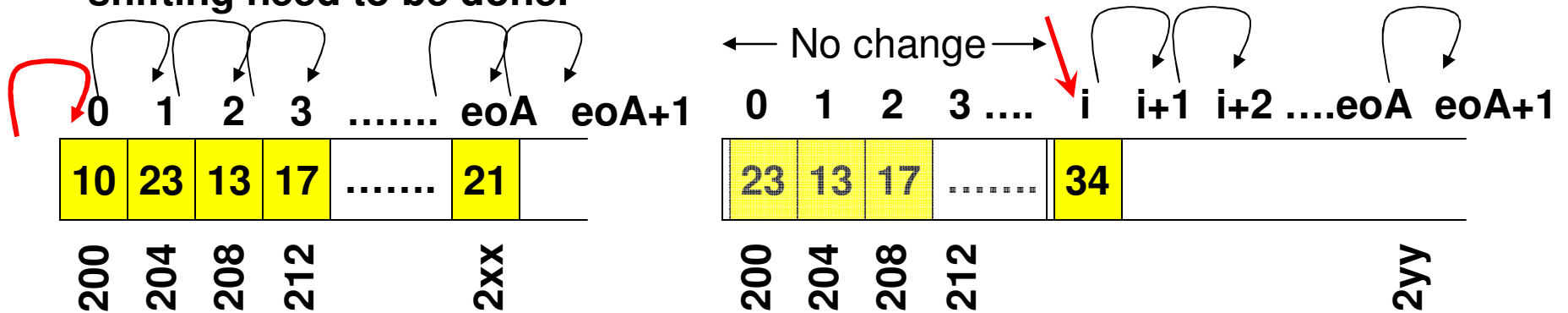
Insert Operation (incl. Relocation and Doubling the Size of the Array)



Time complexity analysis for 'Insert': Dynamic List ADT as an Array

Insert operation

(i) Worst case: If the element is to be inserted as the first element in the array, then elements from index $\text{endOfArray}(\text{eoA})$ to index '0' have to be shifted one position to the right. If $\text{eoA} = n-1$, then 'n' (indexes 0 to n-1) such shifting need to be done.



(ii) Best case: If the element is to be inserted at the end of the array, no shifting is needed.

(iii) In general, if the element is to be inserted at index i , then the elements from index $\text{endOfArray}(\text{eoA})$ to index 'i' need to be shifted one cell to the right.

Time complexity for insert operation: $O(n)$

Code 2: Other Auxiliary Functions

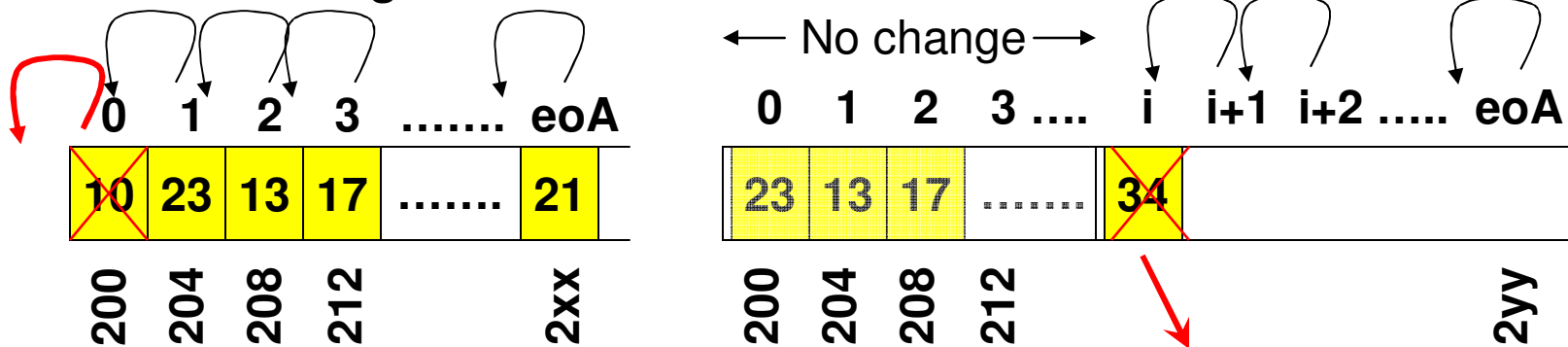
```
int read(int index){  
    return array[index];  
}  
  
void modifyElement(int index, int data){  
    array[index] = data;  
}  
  
void deleteElement(int deleteIndex){  
    // shift elements one cell to the left starting from  
    // deleteIndex+1 to endOfArray-1  
    // i.e., move element at deleteIndex + 1 to deleteIndex and so on  
  
    for (int index = deleteIndex; index < endOfArray; index++)  
        array[index] = array[index+1];  
  
    endOfArray--;  
}  
  
int countList(){  
    int count = 0;  
    for (int index = 0; index <= endOfArray; index++)  
        count++;  
  
    return count;  
}
```

(C++)

Time complexity analysis for 'Delete': Dynamic List ADT as an Array

Delete operation

(i) Worst case: If the element to be deleted is the first element (at index 0) in the array, then the subsequent elements have to be shifted one position to the left, starting from index 1 to endOfArray (eoA). If $eoA = n-1$, then $n-1$ such shifting need to be done.



(ii) Best case: If the element to be deleted is at the end of the array, no shifting is needed.

(iii) In general, if the element to be deleted is at index i , then the elements from index $i+1$ to endOfArray need to be shifted one cell to the left.

Time complexity for delete operation: $O(n)$

Code 2: C++ main function

```
int main(){
```

```
    int listSize;
```

```
    cout << "Enter list size: ";
```

```
    cin >> listSize;
```

```
    List integerList(1);
```

We will set the maximum size of the list to 1
and double it as and when needed

```
    for (int i = 0; i < listSize; i++){
```

```
        int value;
```

```
        cout << "Enter element # " << i << " : ";
```

```
        cin >> value;
```

```
        integerList.insert(i, value);
```

```
    }
```

Pros and Cons of Implementing Dynamic List using Array

- Pros: $\Theta(1)$ time to read or modify an element at a particular index
- Cons: $O(n)$ time to insert or delete an element (at any arbitrary position)
- Note: Array is a contiguous block of memory
- When we double the array size (to handle the need for more space), the memory management system of the OS needs to search for contiguous blocks of memory that is double the previous array size.
 - Sometimes, it becomes difficult to allocate a contiguous block of memory, if the requested array size is larger.
- After we double the size (say from 50,000 to 100,000 to insert just one more element), the rest of the array remains unused. However, increasing the size of the array one element at a time is time consuming too.
 - The copy operation involved during resizing the array is also time consuming

```

int main(){
    int arraySize;
    cout << "Enter an array size: ";
    cin >> arraySize;

    int maxValue;
    cout << "Enter the max. value of an element: ";
    cin >> maxValue;

    int array[arraySize];

    for (int i = 0; i < arraySize; i++){
        array[i] = rand() % maxValue;
    }

    cout << "IterativePrint: ";
    IterativePrint(array, arraySize);

    return 0;
}

```

C++

```

void IterativePrint(int* arrayPtr, int size){
    for (int index = 0; index < size; index++){
        cout << arrayPtr[index] << " ";
    }

    cout << endl;
}

```

**Example Code 4:
Random Number Generation**

Initialize the random number generator with a seed that corresponds to the current system time

The random numbers are generated from 0 to maxValue - 1

Headers to be included

```

#include <iostream>
#include <stdlib.h> // random number
#include <time.h> // for time
using namespace std;

```

Code 6: Run Time Complexity Analysis

```
#include <iostream>
#include <ctime>
#include <ratio>
#include <chrono>
using namespace std;

int main ()
{
    using namespace std::chrono;

    high_resolution_clock::time_point t1 = high_resolution_clock::now();

    cout << "printing out 1000 stars...\n";
    for (int i=0; i<1000; ++i) cout << "*";
    cout << endl;

    high_resolution_clock::time_point t2 = high_resolution_clock::now();

    duration<double, std::nano> time_span_nano = t2 - t1;
    duration<double, std::micro> time_span_micro = t2 - t1;
    duration<double, std::milli> time_span_milli = t2 - t1;

    cout << "It took me " << time_span_nano.count() << " nanoseconds." << endl;
    cout << "It took me " << time_span_micro.count() << " microseconds." << endl;
    cout << "It took me " << time_span_milli.count() << " milliseconds." << endl;
    cout << endl;

    return 0;
}
```

Linked List

- A Linked List stores the elements of the 'List' in separate memory locations and we keep track of the memory locations as part of the information stored with an element (called a node).
 - A 'node' in a Linked List contains the data value as well as the address of the next node.
- Singly Linked List: Each node contains the address of the node with the subsequent value in the list. There is also a head node that points to the first node in the list.

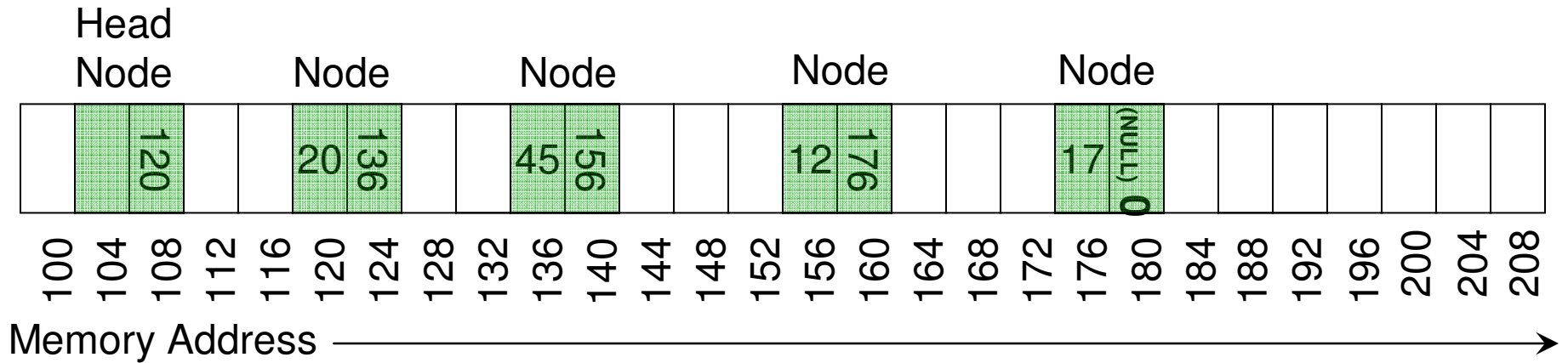
Data **With singly linked list – we can traverse only in one direction**
nextNodePtr

- Doubly Linked List: Each node contains the address of the node with the subsequent value as well as the address of the node with the preceding value. There is also a head node pointing to the first node in the list and a tail node pointing to the last node in the list.

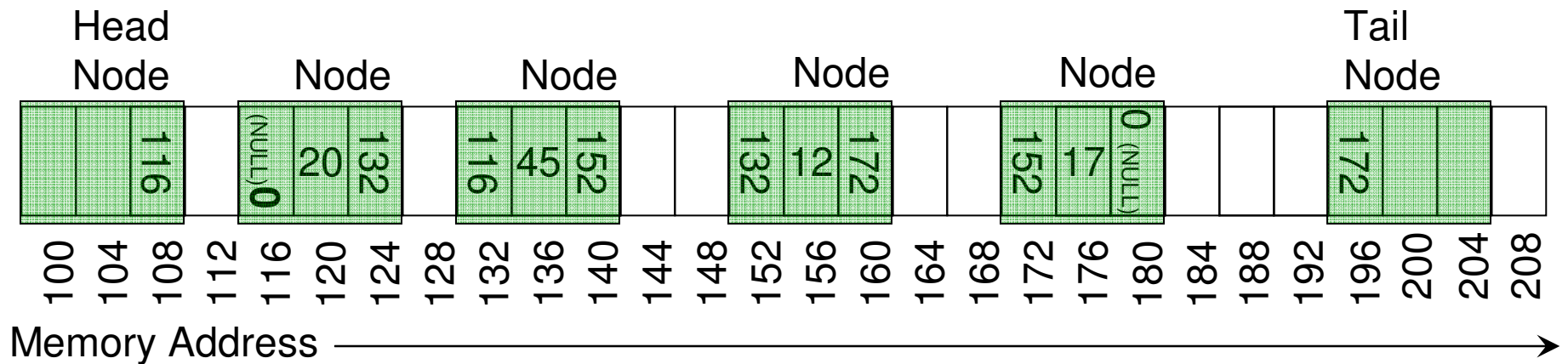
prevNodePtr
Data **With doubly linked list – we can traverse in both directions**
nextNodePtr

- Note: Memory address can be represented in 4 bytes. Hence, each pointer or reference to a memory will take 4 bytes of space.

Singly Linked List



Doubly Linked List



Linked List vs. Arrays: Memory Usage

	Data size	Next Node Ptr	Prev Node Ptr	Node Size
Singly Linked List	4 (int)	4	N/A	8 bytes
Singly Linked List	32	4	N/A	36 bytes
Doubly Linked List	4 (int)	4	4	12 bytes
Doubly Linked List	32	4	4	40 bytes

An array is usually considered to take space that is twice the number of elements in it. Still, it looks like the Linked Lists will take a larger memory compared to an array. But, it is not always the case.

Consider a scenario wherein 64,000 objects (each of size 32 bytes) are to be stored in a List.

If we were to stored the objects in an array, there would need to be space for 128,000 objects. Hence, a dynamic array-based implementation will now hold up $128,000 * 32 \text{ bytes} = 40,96,000$ bytes in memory.

A singly linked list based implementation will hold $(64,000 + 1 \text{ head node}) * 36 \text{ bytes} = 23,04,036$ bytes in memory.

A doubly linked list based implementation will hold $(64,000 + 1 \text{ head node} + 1 \text{ tail node}) * 40 \text{ bytes} = 25,60,080$ bytes in memory.

Linked List vs. Arrays: Memory Usage

On the other hand, Consider a scenario wherein 4,000 integers (each integer is 4 bytes) are to be stored in a List.

An array-based implementation will now hold $8,000 * 4 = 32,000$ bytes in memory.

A singly linked list-based implementation will now hold $(4,000 + 1 \text{ head node}) * 8 = 32,008$ bytes in memory.

A doubly linked list-based implementation will now hold $(4,000 + 1 \text{ head node} + 1 \text{ tail node}) * 12 = 48,024$ bytes in memory.

Singly Linked List Implementation (Code 3)

Class Node

C++

```
private:  
    int data;  
    Node* nextNodePtr;
```

```
public:  
    Node(){  
  
    void setData(int d){  
        data = d;  
    }  
  
    int getData(){  
        return data;  
    }  
}
```

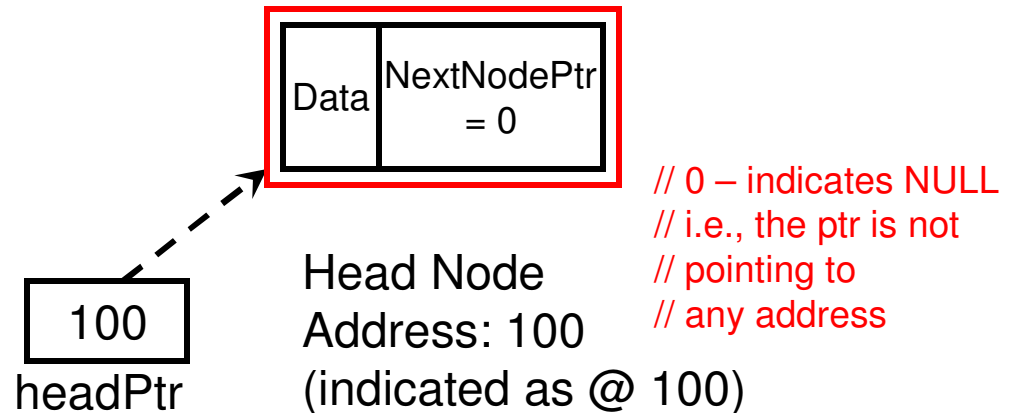
```
public:  
    void setNextNodePtr(Node* nodePtr){  
        nextNodePtr = nodePtr;  
    }  
  
    Node* getNextNodePtr(){  
        return nextNodePtr;  
    }  
}
```

Singly Linked List: Class List

Class List (C++)

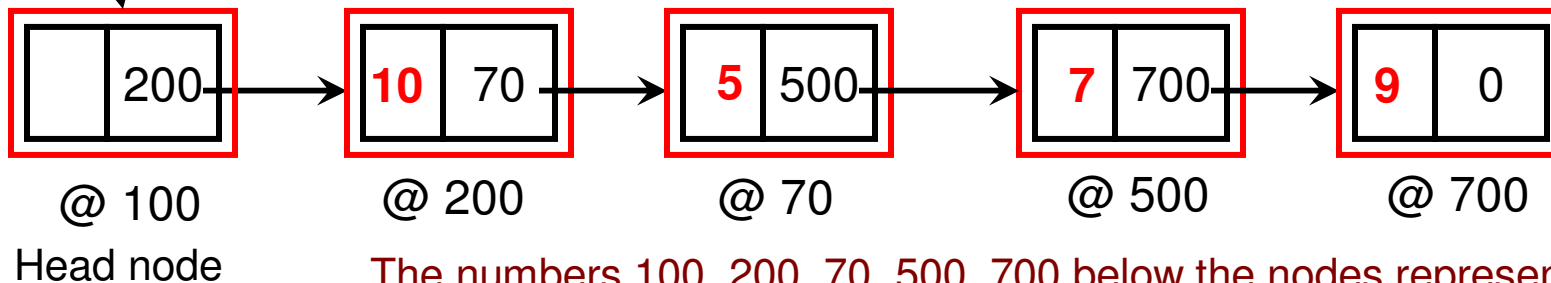
```
private:  
    Node *headPtr;  
  
public:    /* Note that the data for the  
List(){  Head node is not set */  
    headPtr = new Node();  
    headPtr->setNextNodePtr(0);  
}
```

Initialization of List Object



headPtr
100

Convention used to represent a Linked List.
Let the List be **10 5 7 9**



The numbers 100, 200, 70, 500, 700 below the nodes represent the address at which these nodes are stored, indicated with an @ symbol

Class List (C++)

```
void insert(int data){
```

```
    Node* currentNodePtr = headPtr->getNextNodePtr();
```

```
    Node* prevNodePtr = headPtr;
```

```
    while (currentNodePtr != 0){
```

```
        prevNodePtr = currentNodePtr;
```

```
        currentNodePtr = currentNodePtr->getNextNodePtr();
```

```
    }
```

```
    Node* newNodePtr = new Node();
```

```
    newNodePtr->setData(data);
```

```
    newNodePtr->setNextNodePtr(0);
```

```
    prevNodePtr->setNextNodePtr(newNodePtr);
```

```
}
```

If the nextNodePtr for the headPtr points to null (0), then the list is empty. Otherwise, the list has at least one node.

```
bool isEmpty(){
```

```
    if (headPtr->getNextNodePtr() == 0)
```

```
        return true;
```

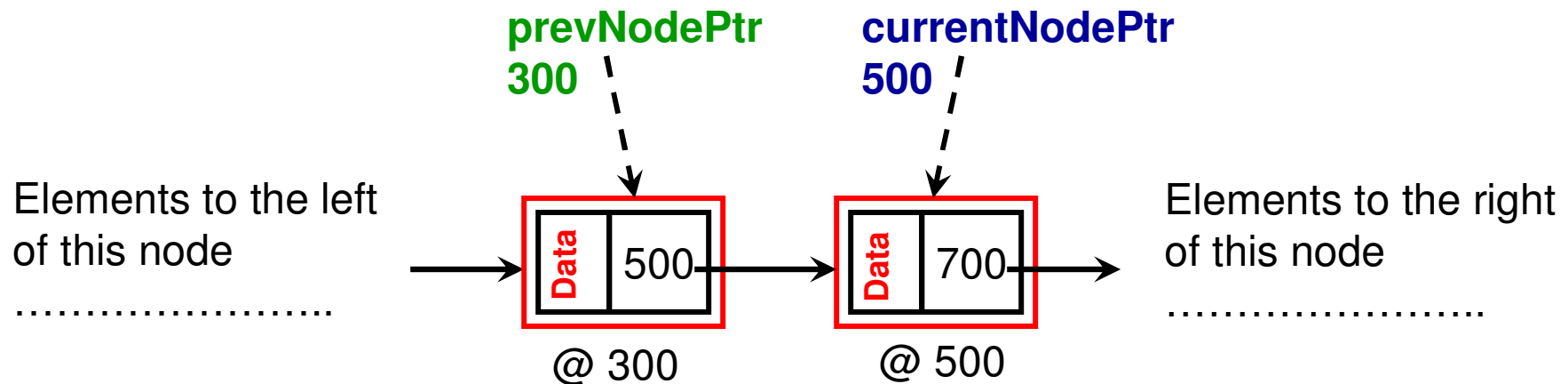
```
    return false;
```

```
}
```

Move the currentNode ptr from first node in the list to end of the list. When we come out of the 'while' loop, the prevNode ptr is the last node in the list and currentNode ptr points to null (0).

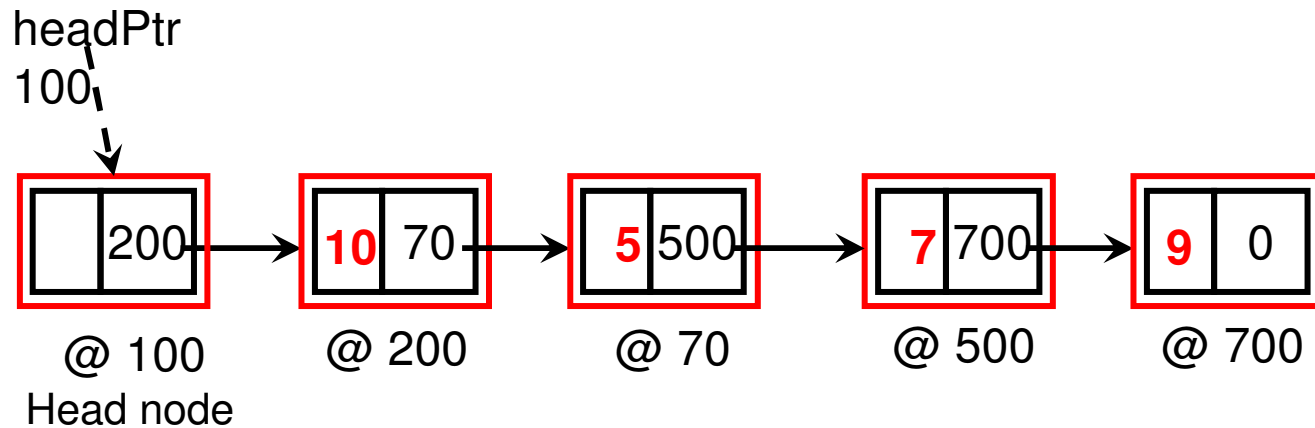
prevNodePtr and currentNodePtr

- As we traverse through the list, node by node, we will maintain two pointers: the prevNodePtr and currentNodePtr.
 - The currentNodePtr has the address for the node that is currently being visited/ processed.
 - The prevNodePtr has the address for the node that was just visited before the current node.
- We have reached the end of the list when currentNodePtr is 0 (i.e., does not point to any node).



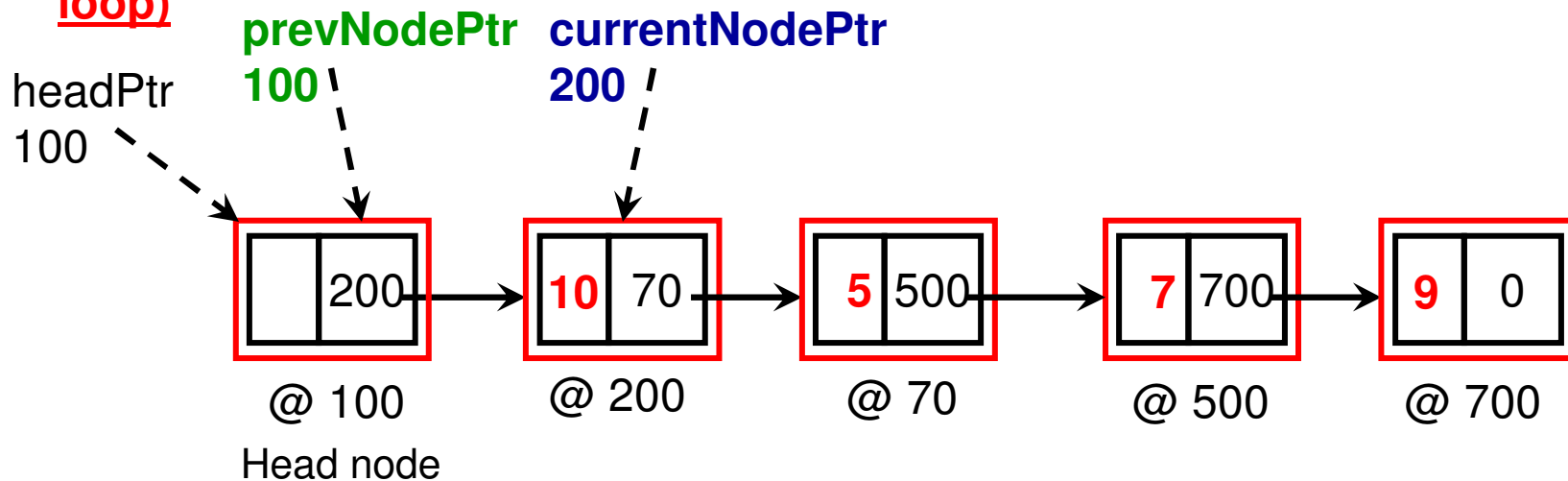
Example: Insertion at the End of the List (1)

Let the List be **10 5 7 9** and now we want to insert element '30' at the end.



Initialization of prevNodePtr and currentNodePtr (before the while loop)

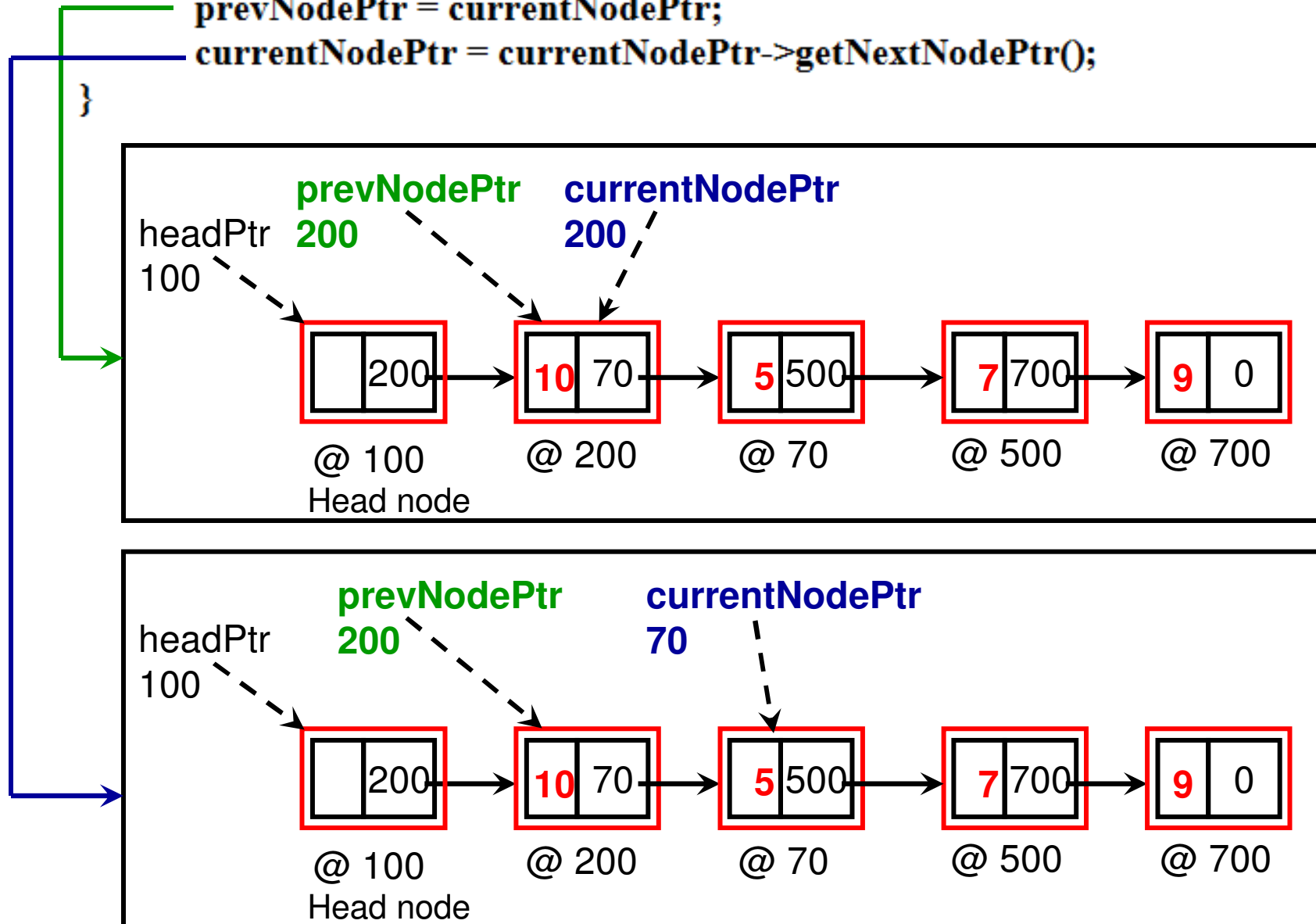
```
Node* currentNodePtr = headPtr->getNextNodePtr();  
Node* prevNodePtr = headPtr;
```



Inside the while loop

Example continued (2)

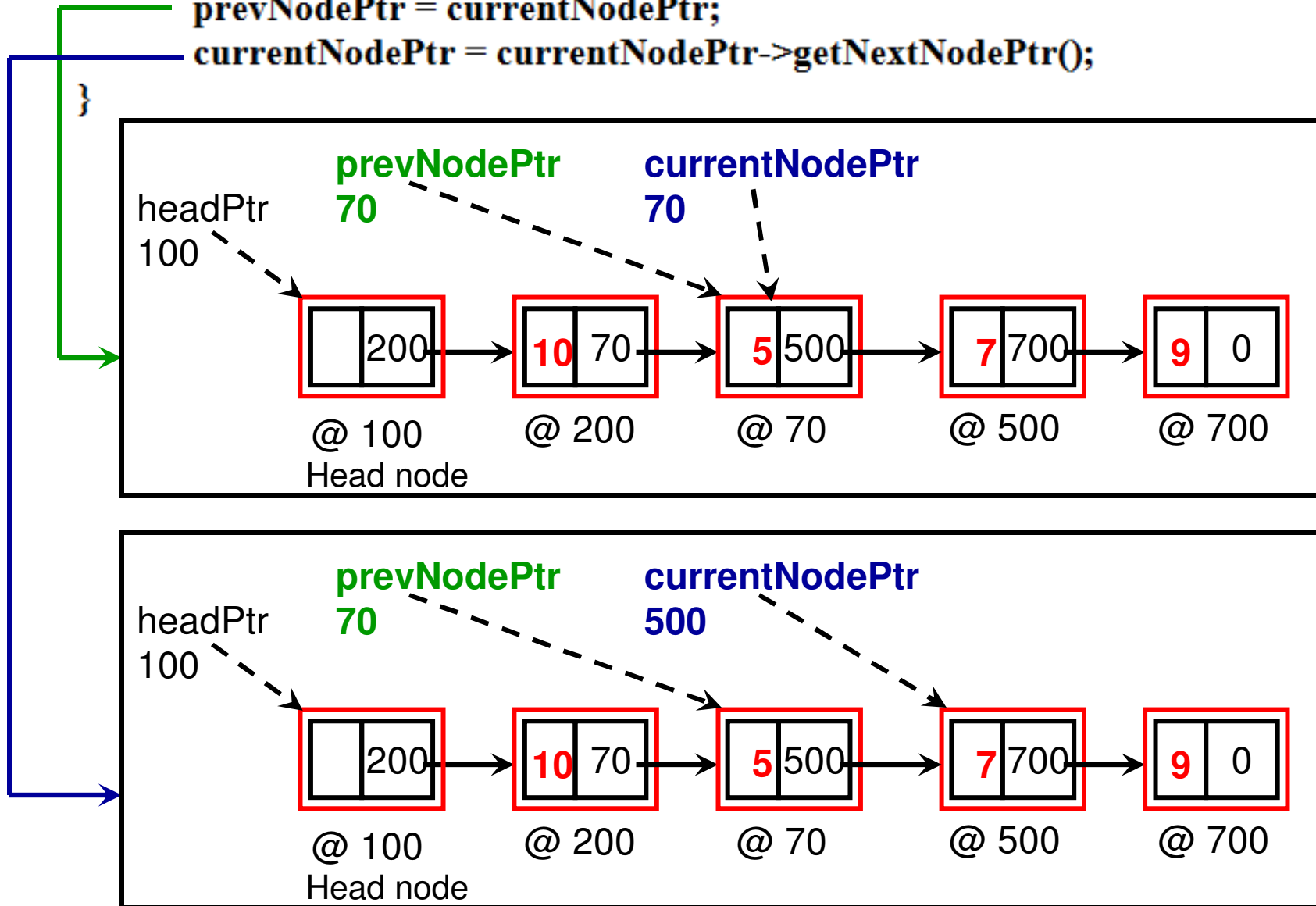
```
while (currentNodePtr != 0){  
    prevNodePtr = currentNodePtr;  
    currentNodePtr = currentNodePtr->getNextNodePtr();  
}
```



Inside the while loop

Example continued (3)

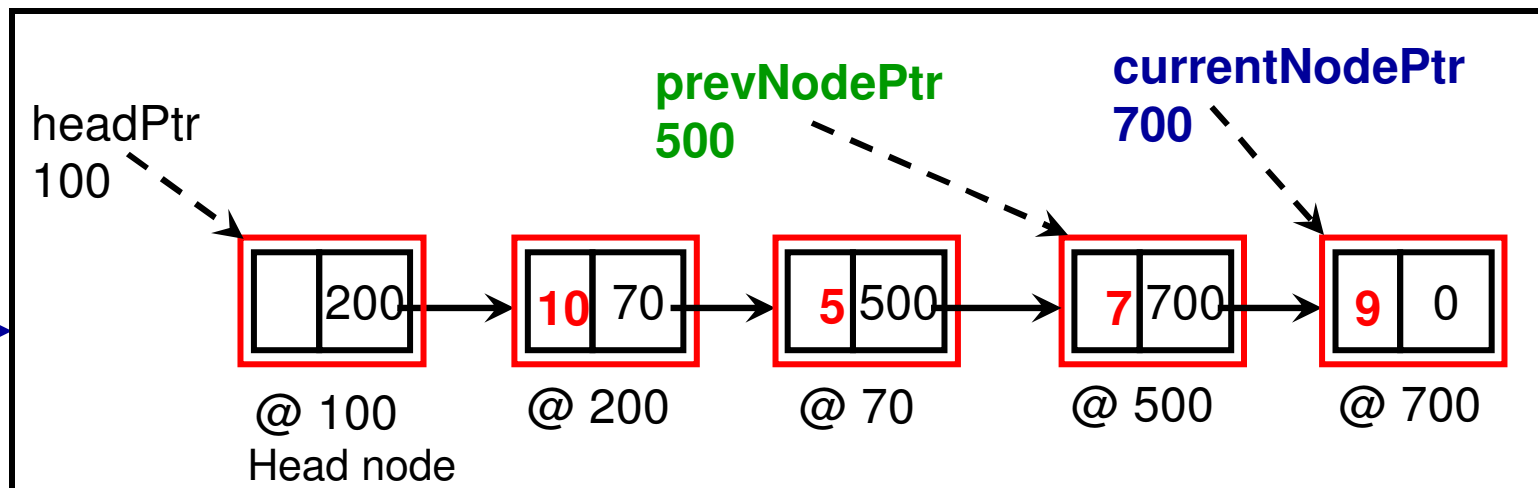
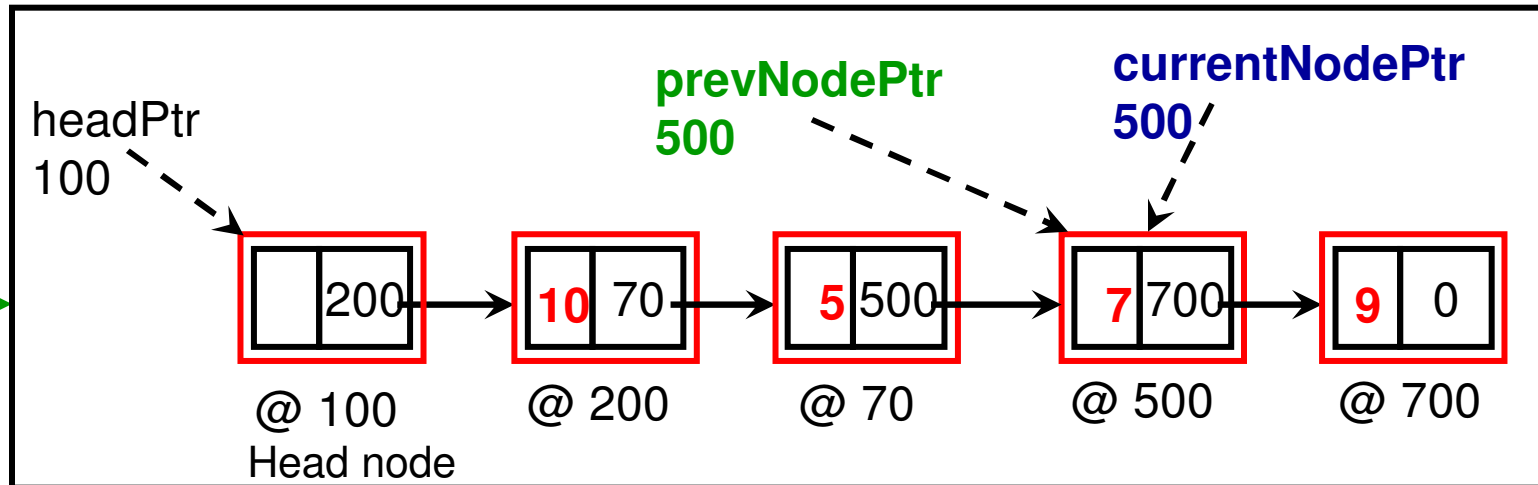
```
while (currentNodePtr != 0){  
    prevNodePtr = currentNodePtr;  
    currentNodePtr = currentNodePtr->getNextNodePtr();  
}
```



Inside the while loop

Example continued (4)

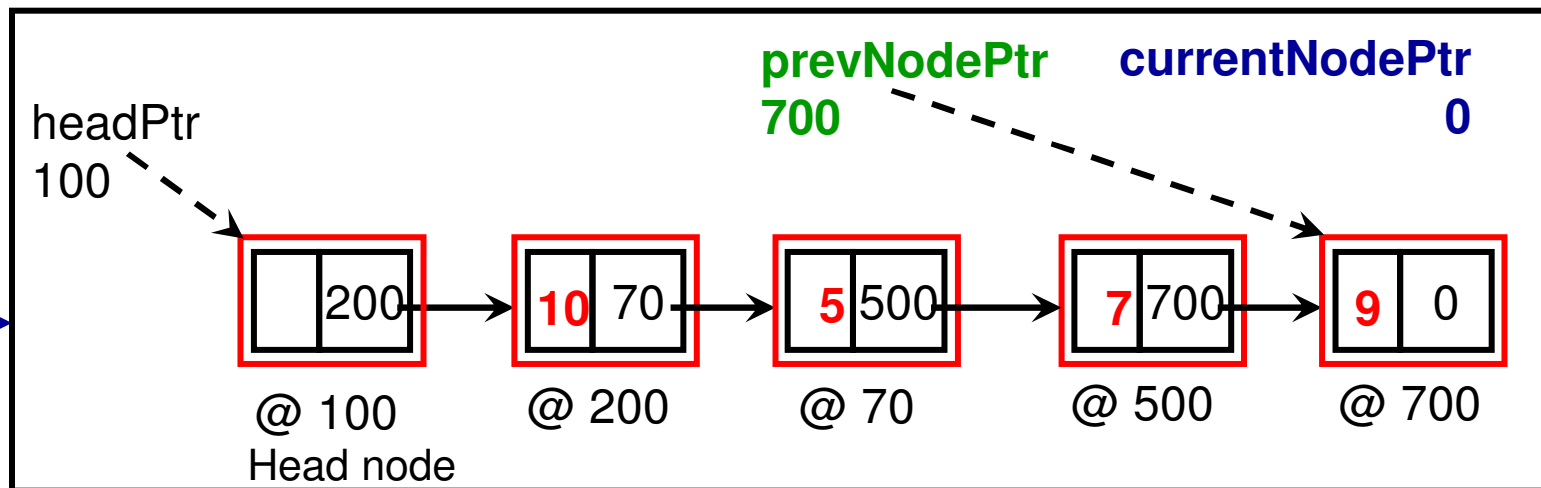
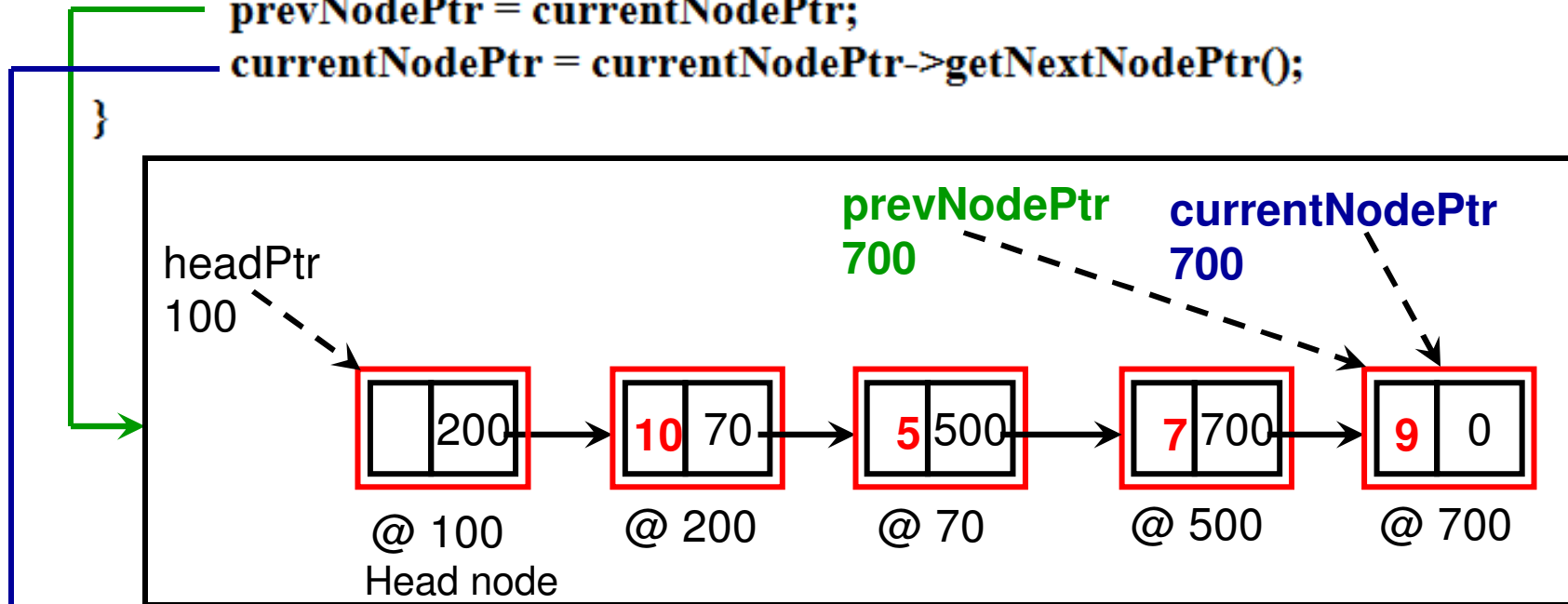
```
while (currentNodePtr != 0){  
    prevNodePtr = currentNodePtr;  
    currentNodePtr = currentNodePtr->getNextNodePtr();  
}
```



Inside the while loop

Example continued (5)

```
while (currentNodePtr != 0){  
    prevNodePtr = currentNodePtr;  
    currentNodePtr = currentNodePtr->getNextNodePtr();  
}
```

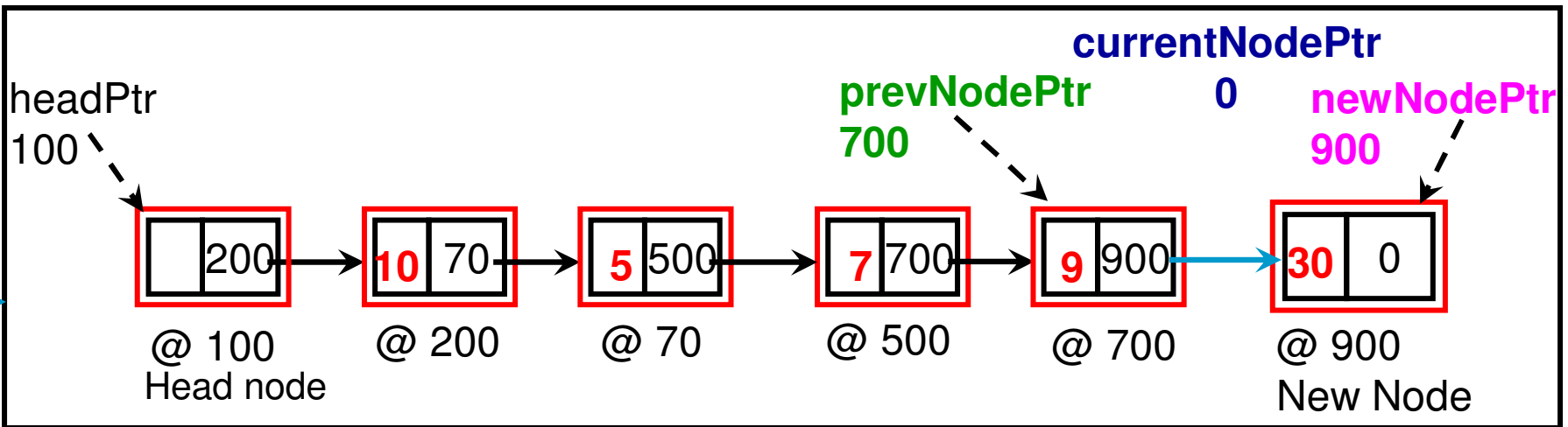
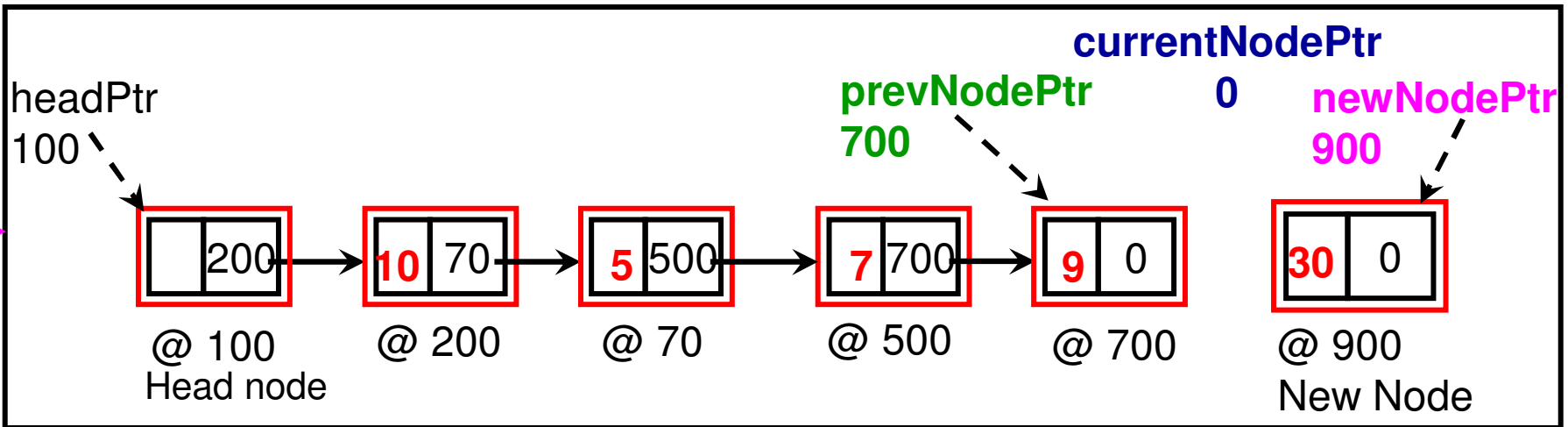


After the while loop

```
Node* newNodePtr = new Node();  
newNodePtr->setData(data);  
newNodePtr->setNextNodePtr(0);  
prevNodePtr->setNextNodePtr(newNodePtr);
```

Example continued (6)

Let '30' be the data to be inserted at the end of the Linked List



Class List (C++)

```
void insertAtIndex(int insertIndex, int data){
    Node* currentNodePtr = headPtr->getNextNodePtr();
    Node* prevNodePtr = headPtr;

    int index = 0;
    while (currentNodePtr != 0){
        if (index == insertIndex)
            break;

        prevNodePtr = currentNodePtr;
        currentNodePtr = currentNodePtr->getNextNodePtr();
        index++;
    }

    Node* newNodePtr = new Node();
    newNodePtr->setData(data);
    newNodePtr->setNextNodePtr(currentNodePtr);
    prevNodePtr->setNextNodePtr(newNodePtr);
}
```

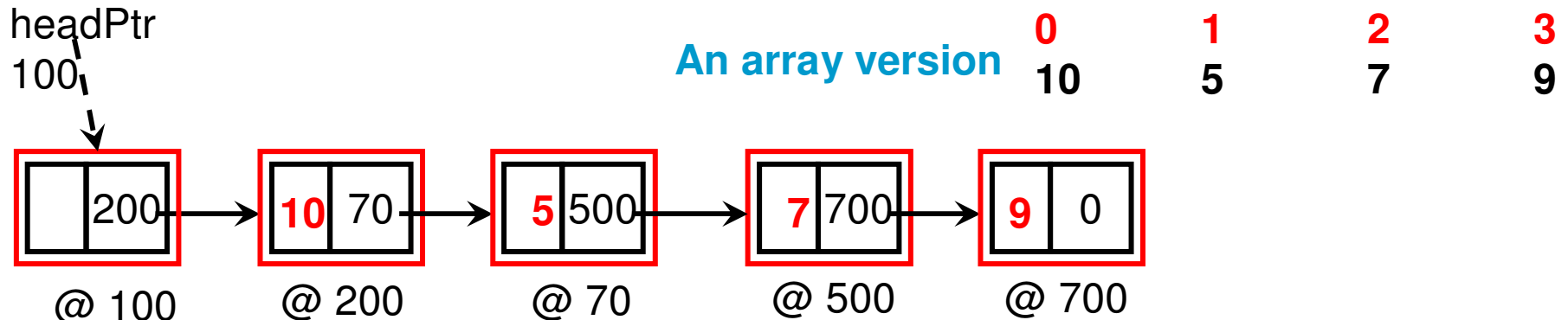
index refers to the node pointed by currentNodePtr at any time

During the beginning and end of the while loop, the value for 'index' corresponds to the Position of the currentNode ptr and prevNode ptr corresponds to index-1.

If index equals insertIndex, we break from the while loop and insert the new node at the index in between prevNode and currentNode.

Example: Insertion at *insertIndex* = 2 (1)

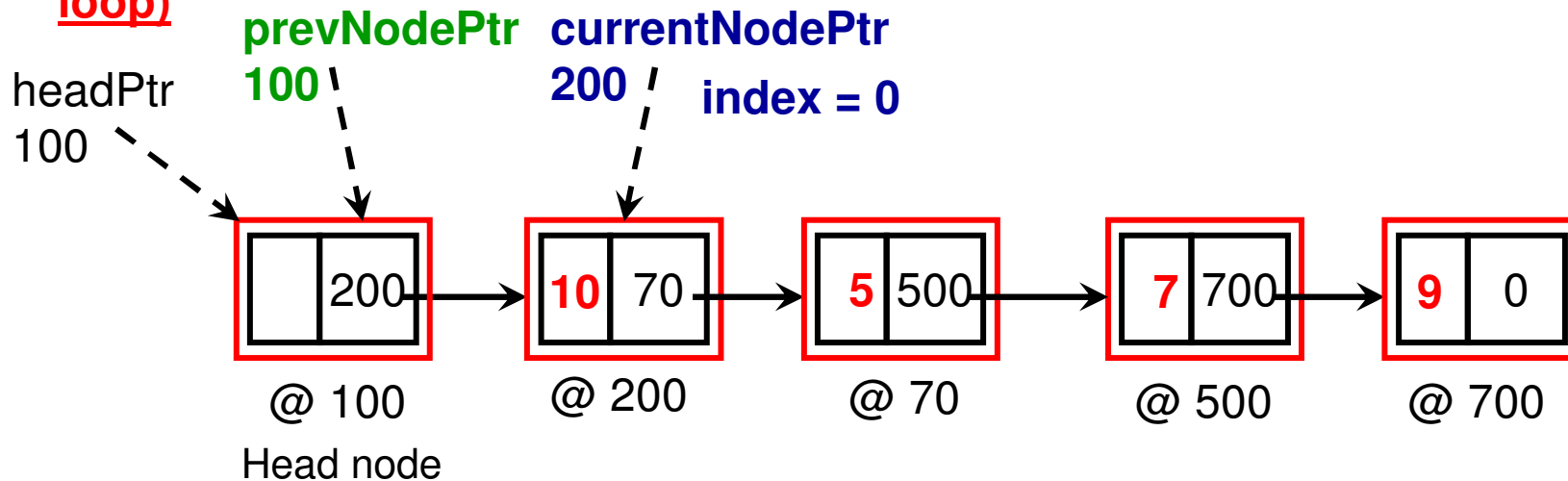
Let the List be **10 5 7 9** and let us say we want to insert element '30' at *insertIndex* = 2



Head node

Initialization of prevNodePtr and currentNodePtr (before the while loop)

```
Node* currentNodePtr = headPtr->getNextNodePtr();  
Node* prevNodePtr = headPtr;  
int index = 0;
```

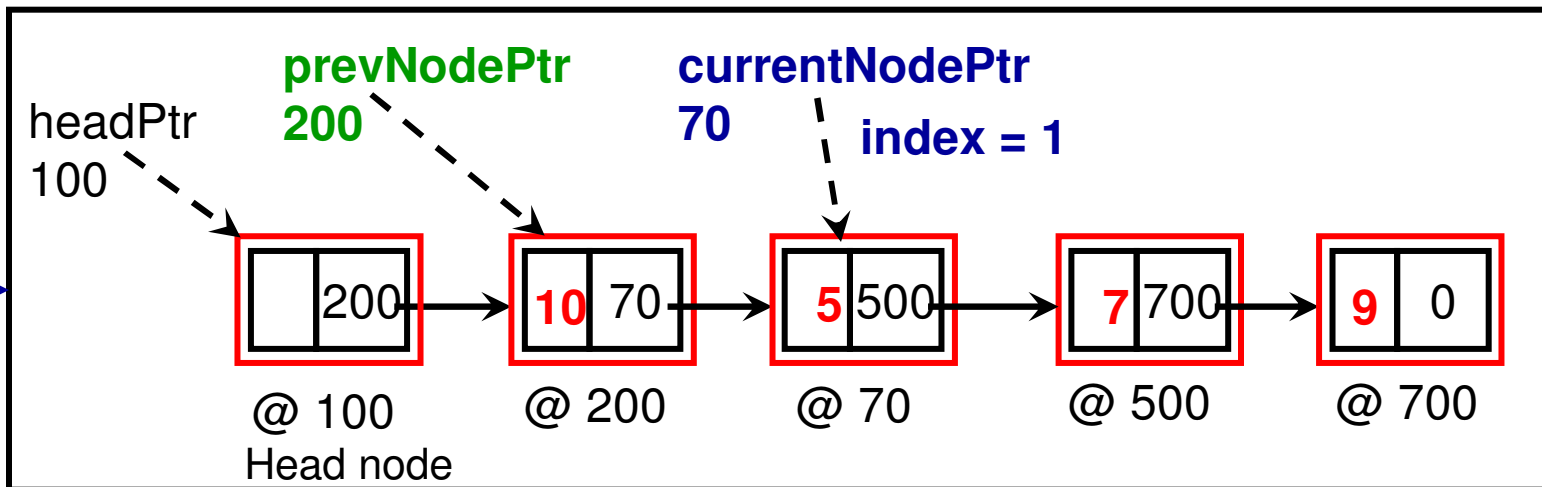
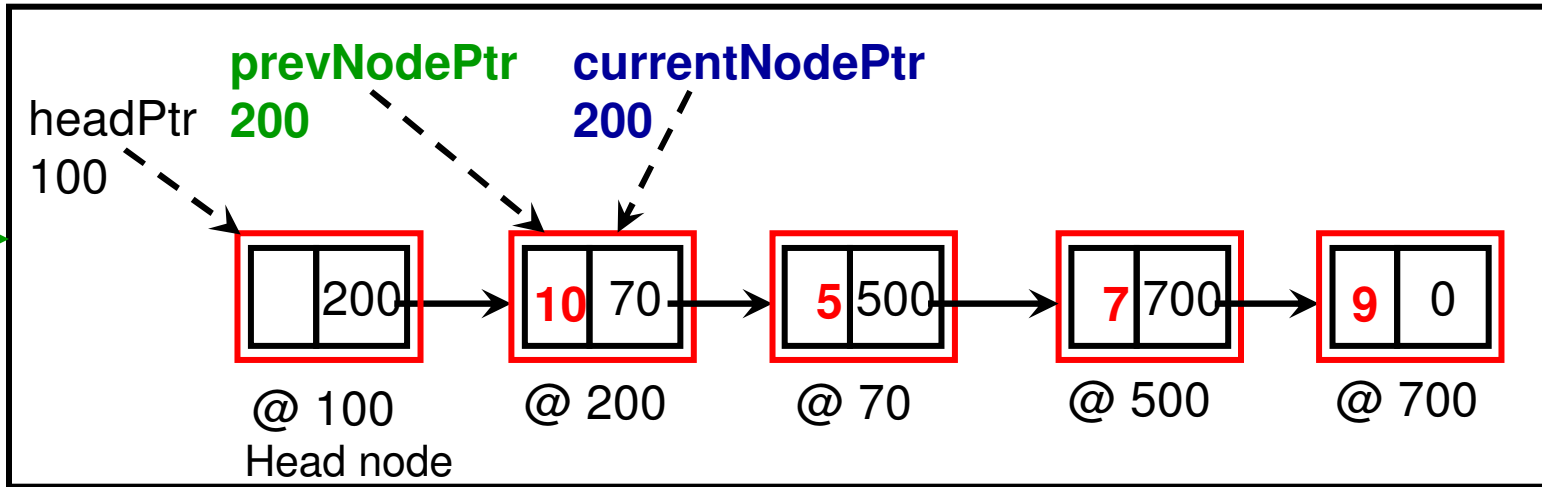


Inside the while loop

Example continued (2)

insertIndex = 2

```
prevNodePtr = currentNodePtr;  
currentNodePtr = currentNodePtr->getNextNodePtr();  
index++;
```

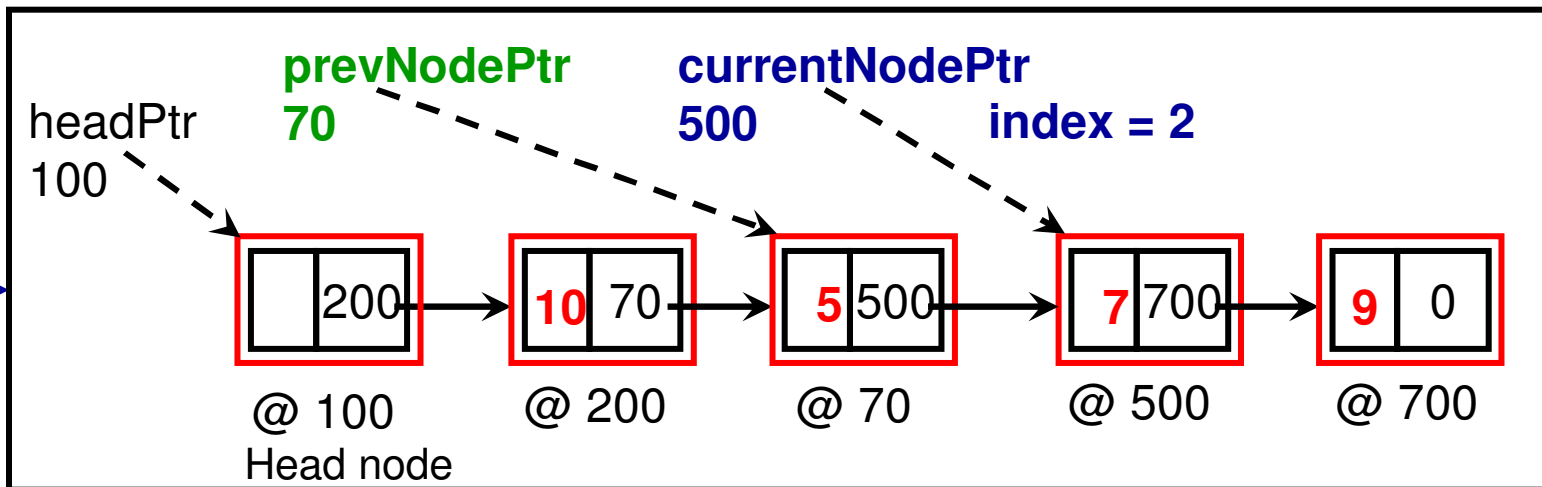
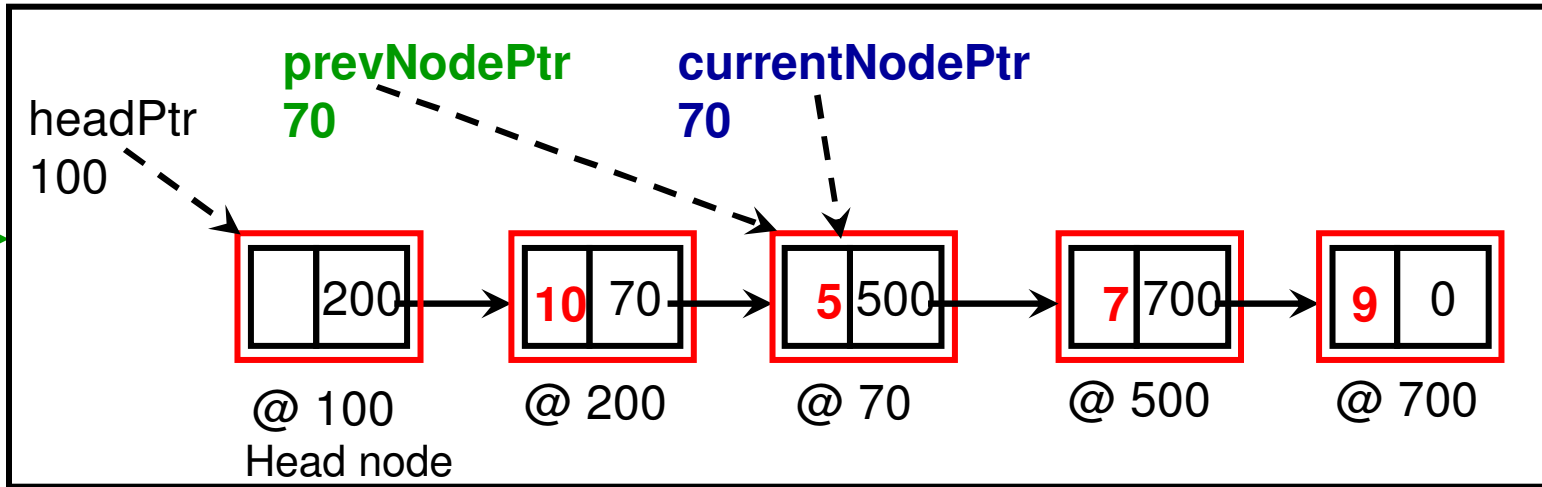


Inside the while loop

Example continued (3)

insertIndex = 2

```
prevNodePtr = currentNodePtr;  
currentNodePtr = currentNodePtr->getNextNodePtr();  
index++;
```

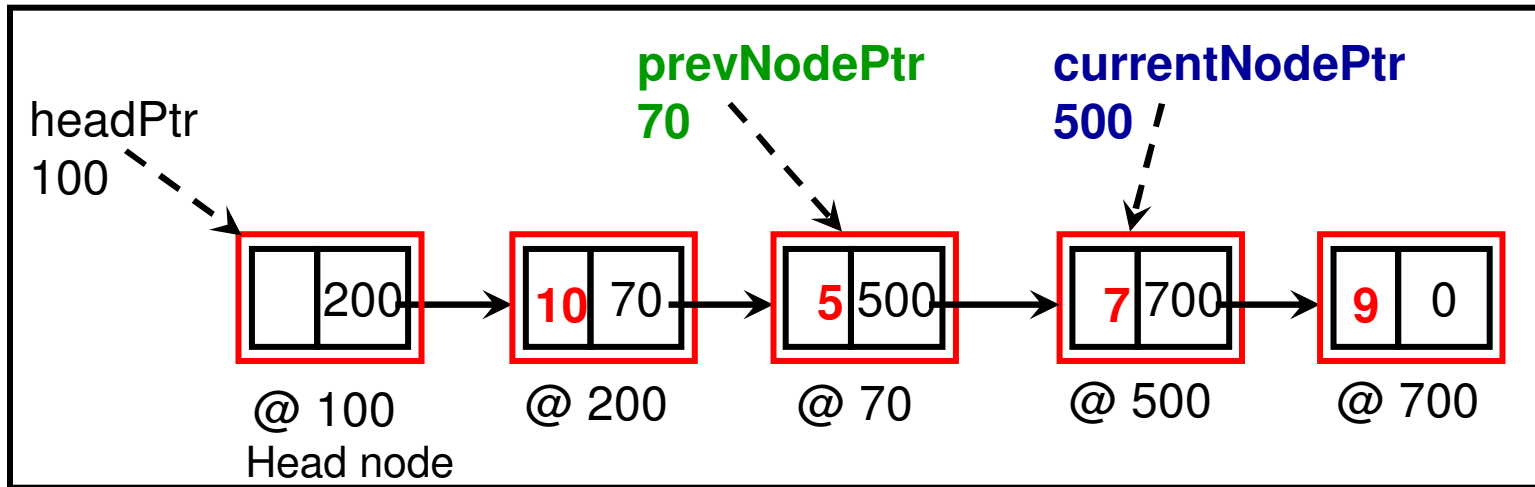


At the time of breaking from the while loop

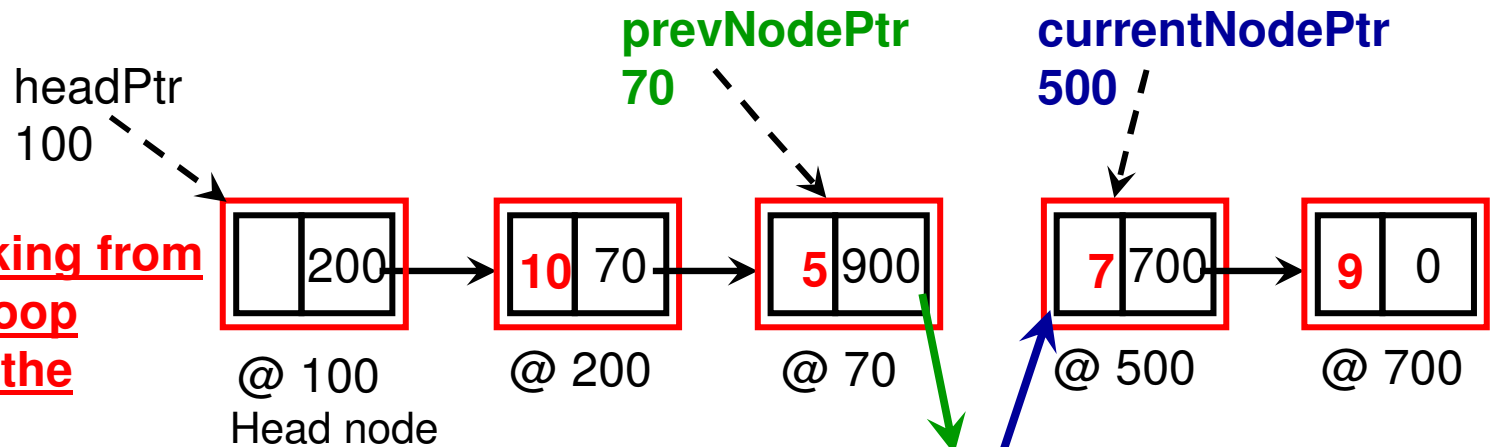
Example continued (3)

index = 2

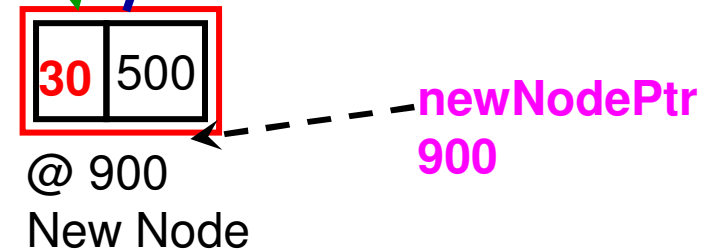
insertIndex = 2



After breaking from the while loop
Linking of the newNode



`newNode->setNextNodePtr(currentNode);`
`prevNode->setNextNodePtr(newNode);`



Class List (C++)

```
int read(int readIndex){  
    Node* currentNodePtr = headPtr->getNextNodePtr();  
    Node* prevNodePtr = headPtr;  
    int index = 0;  
  
    while (currentNodePtr != 0){  
        if (index == readIndex)  
            return currentNodePtr->getData();  
  
        prevNodePtr = currentNodePtr;  
        currentNodePtr = currentNodePtr->getNextNodePtr();  
  
        index++;  
        The 'index' value corresponds to the  
        Position of the currentNode ptr and  
        index-1 corresponds to prevNode ptr  
    }  
    return -1; // an invalid value indicating index is out of range  
}
```

Class List (C++)

```
void modifyElement(int modifyIndex, int data){
    Node* currentNodePtr = headPtr->getNextNodePtr();
    Node* prevNodePtr = headPtr;
    int index = 0;

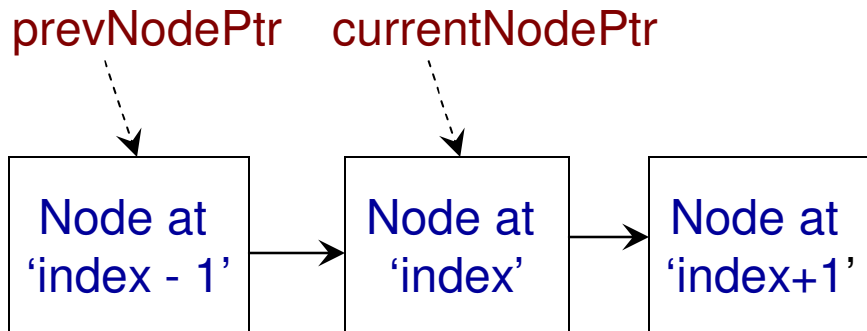
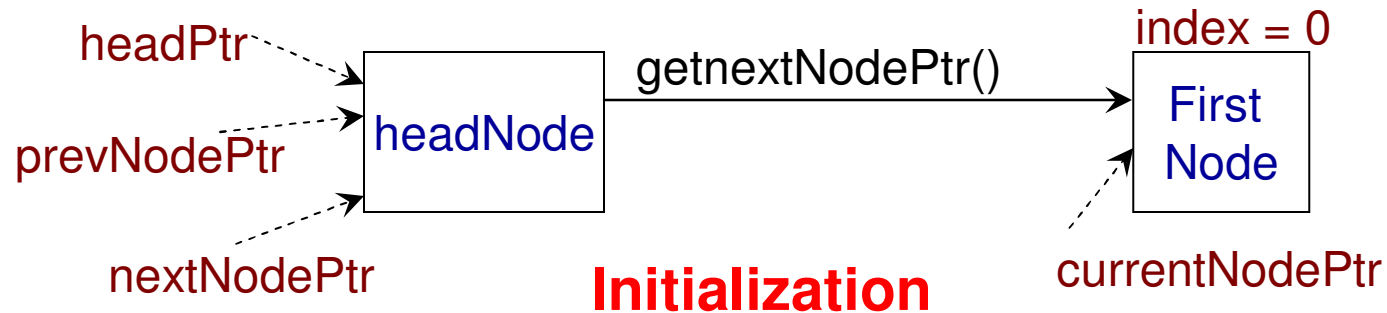
    while (currentNodePtr != 0){

        if (index == modifyIndex){
            currentNodePtr->setData(data);
            return;
        }

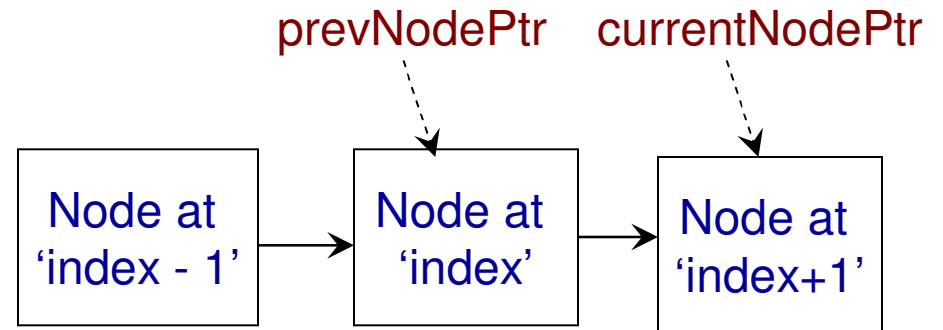
        prevNodePtr = currentNodePtr;
        currentNodePtr = currentNodePtr->getNextNodePtr();

        index++;
    }
}
```

Delete (deleteIndex) Function



At the beginning of an iteration inside the 'while' loop

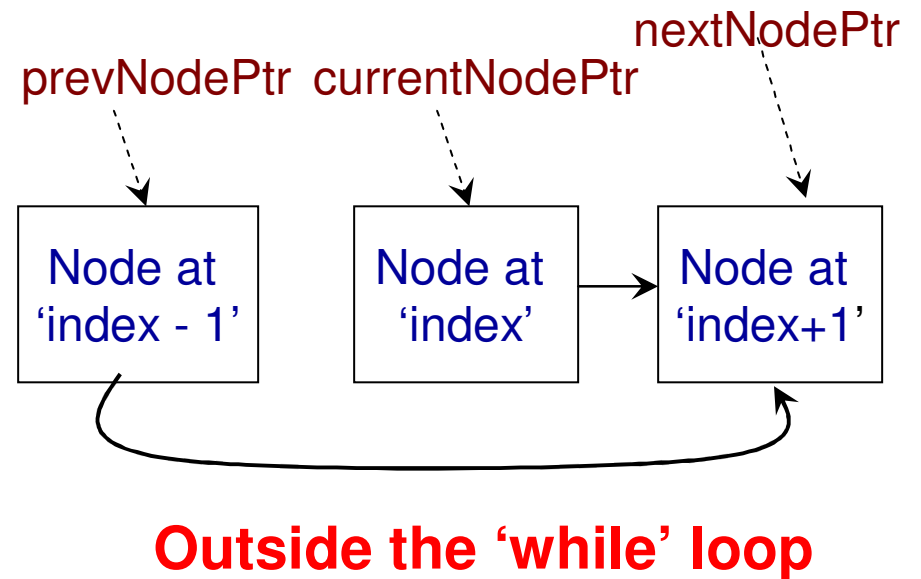
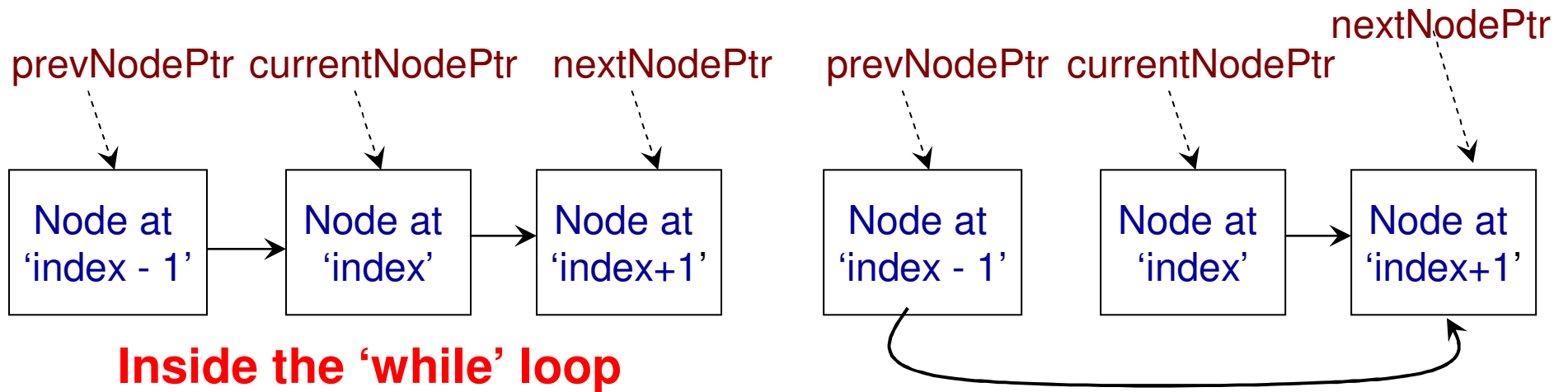


At the end of an iteration inside the 'while' loop

When index != deleteIndex

Delete (deleteIndex) Function

When $\text{index} == \text{deleteIndex}$



**currentNode at index = deleteIndex
is disconnected from the Linked List**

Class List (C++)

```
void deleteElement(int deleteIndex){
    Node* currentNodePtr = headPtr->getNextNodePtr();
    Node* prevNodePtr = headPtr;
    Node* nextNodePtr = headPtr;
    int index = 0;

    while (currentNodePtr != 0){

        if (index == deleteIndex){
            nextNodePtr = currentNodePtr->getNextNodePtr();
            break;
        }

        prevNodePtr = currentNodePtr;
        currentNodePtr = currentNodePtr->getNextNodePtr();

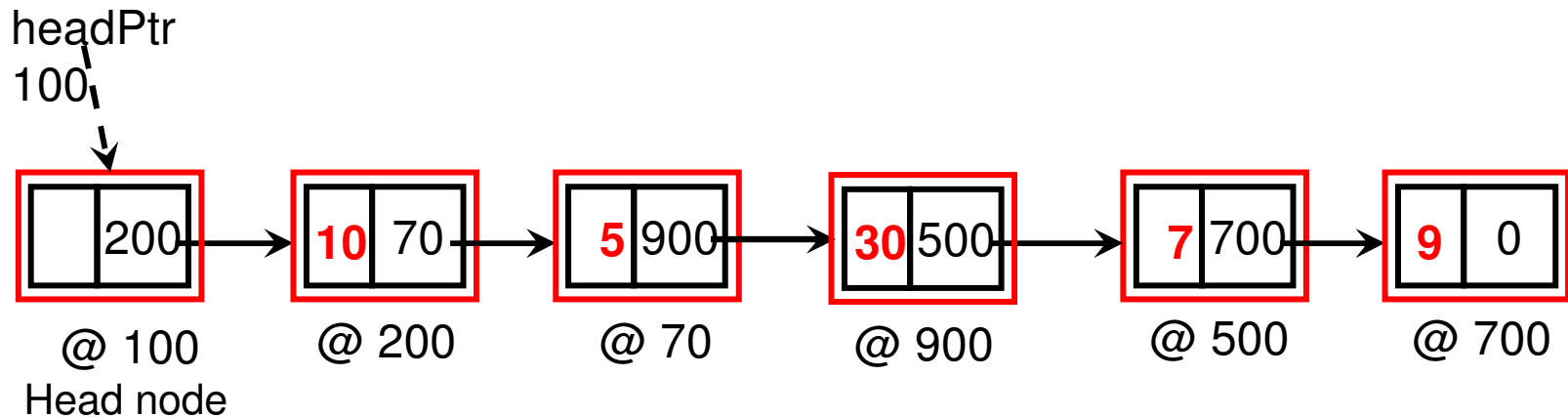
        index++;
    }

    prevNodePtr->setNextNodePtr(nextNodePtr);
}
```

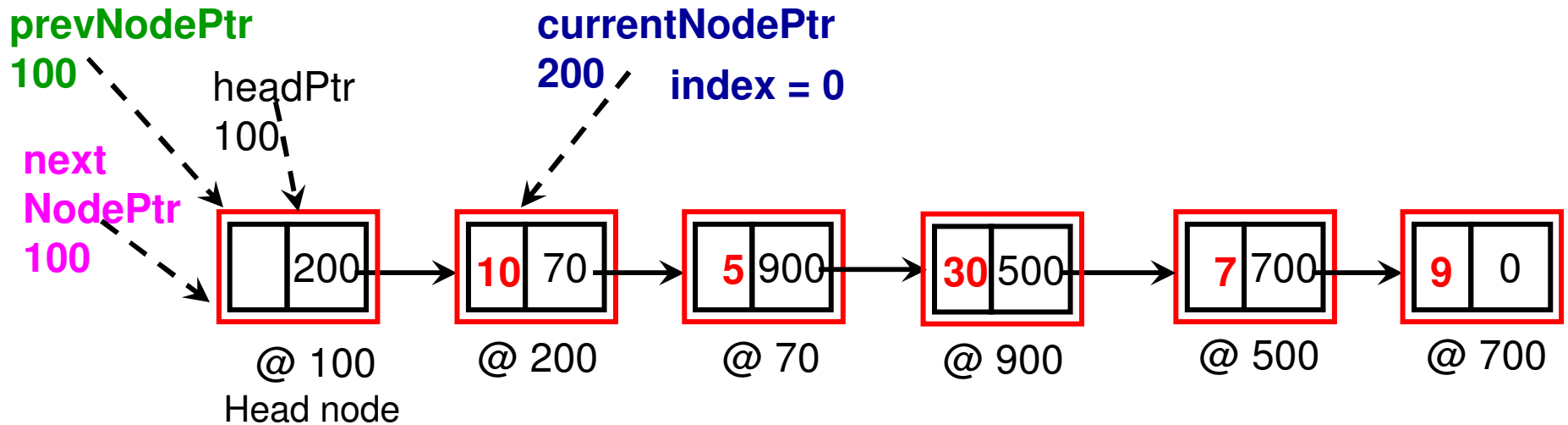
The next node for 'prevNode' ptr
is now 'next node' and not
'current node'

Example: Deletion at *deleteIndex* = 2

Let the List be **10 5 30 7 9** and now we want to delete '30' at *deleteIndex* = 2

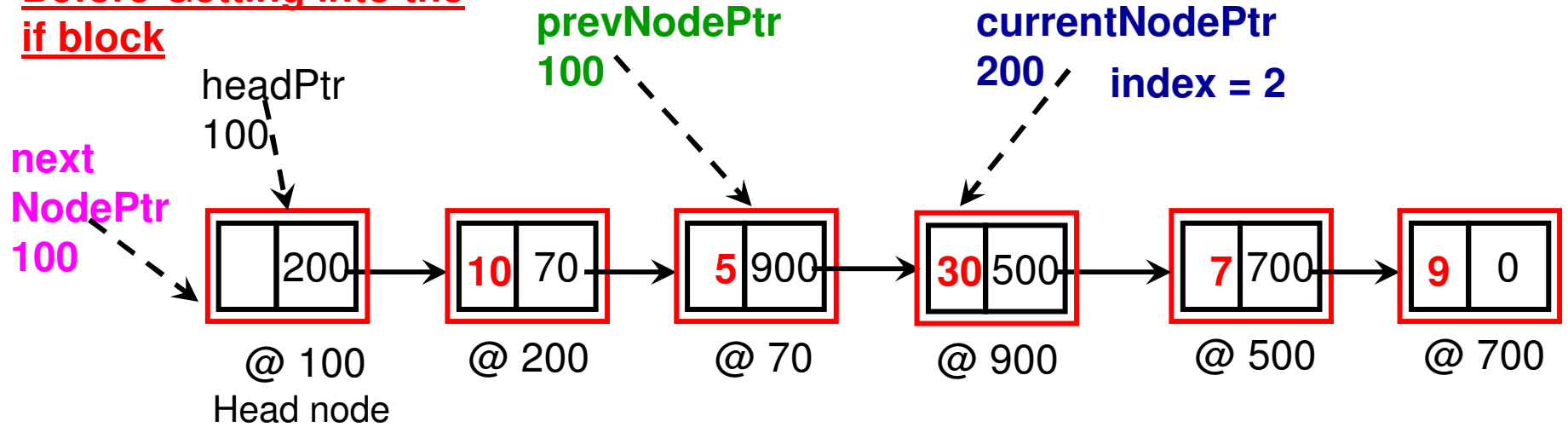


Initialization of the pointers

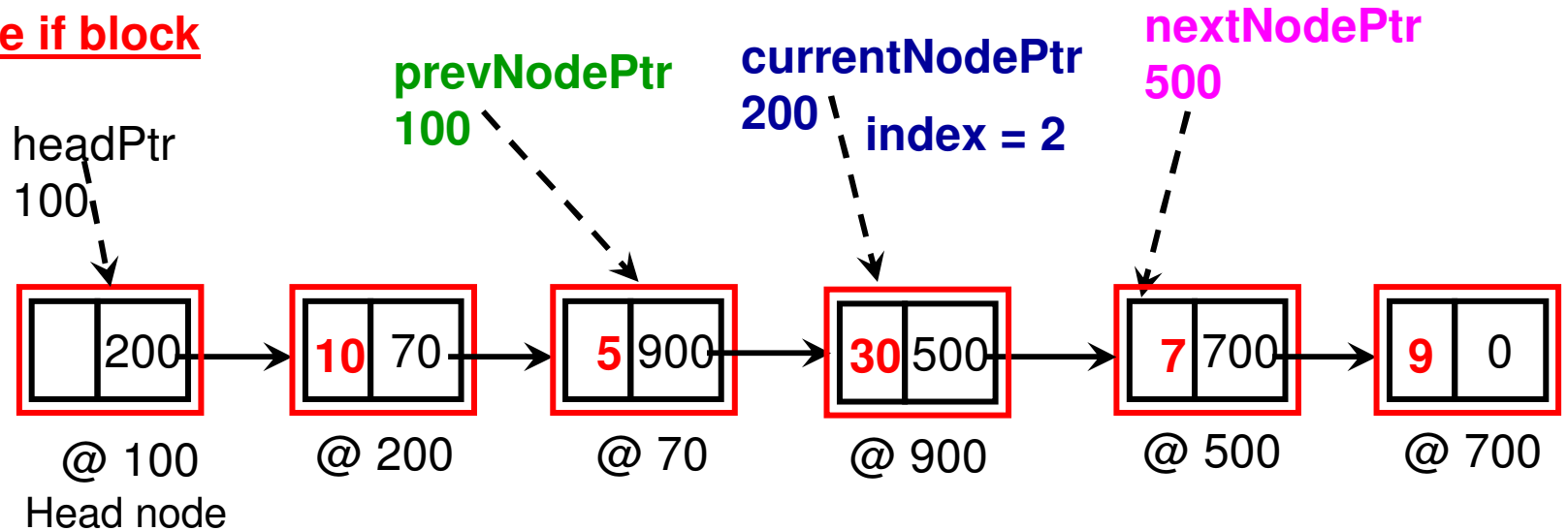


Example: Deletion at *deleteIndex* = 2

Before Getting into the if block

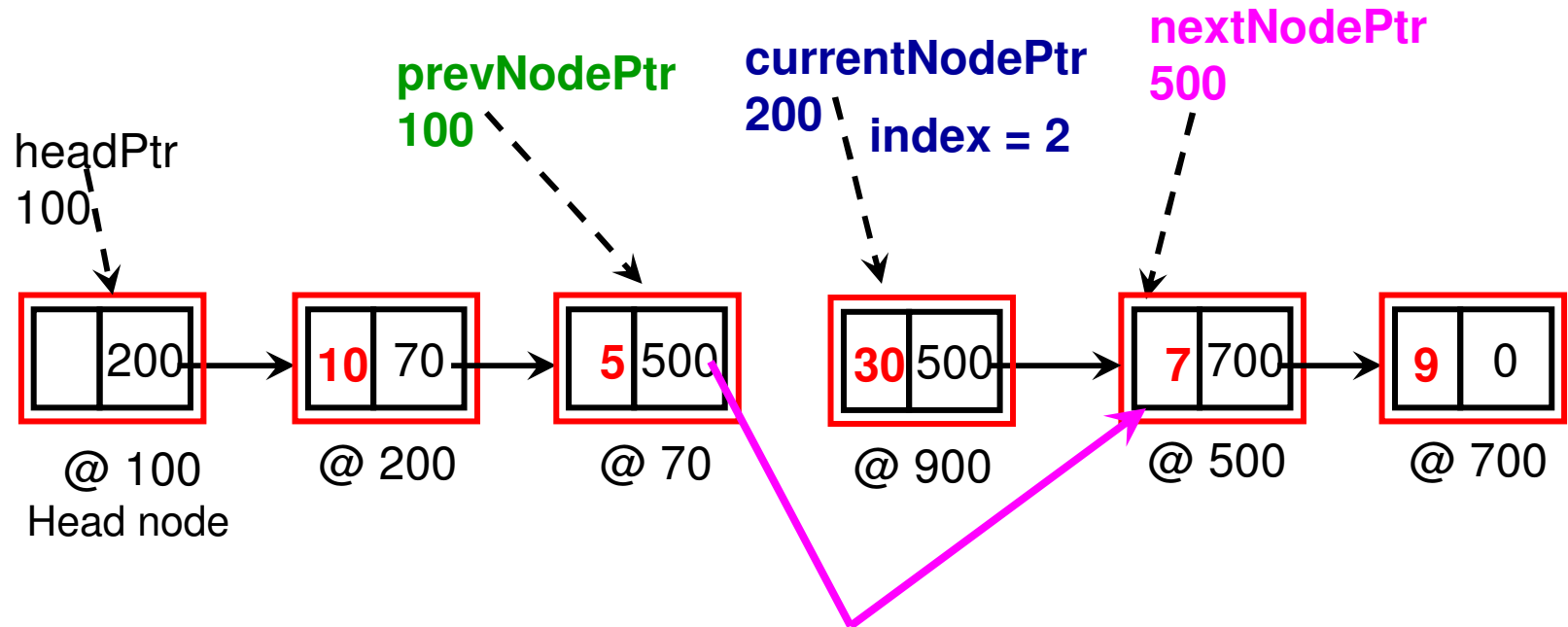


Inside the if block



Example: Deletion at *deleteIndex* = 2

After exiting from the 'while' loop



Delinking of Node at index = 2 (element '30' from the Linked List)

Iterative Print

```
void IterativePrint(){           Class List (C++)  
    Node* currentNodePtr = headPtr->getNextNodePtr();  
  
    while (currentNodePtr != 0){  
        cout << currentNodePtr->getData() << " ";  
        currentNodePtr = currentNodePtr->getNextNodePtr();  
    }  
  
    cout << endl;  
}
```

Linked List vs. Arrays: Time Complexity

	Array	Singly Linked List	Doubly Linked List
Read/Modify	$\Theta(1)$	$O(n)$	$O(n)$
Insert	$O(n)$	$O(n)$	$O(n)$
Delete	$O(n)$	$O(n)$	$O(n)$
isEmpty	$\Theta(1)$	$\Theta(1)$	$\Theta(1)$
Count	$\Theta(1)$	$O(n)$	$O(n)$

We typically use arrays if there are more frequent read/modify operations compared to Insert/Delete

We typically use Linked Lists if there are more frequent insert/delete operations compared to read/modify

Note: With arrays, Insert operations are more time consuming if need to be done at the smaller indices. With singly linked lists, insert operations are more time consuming if done towards the end of the list. A doubly linked list could be traversed either from the head or the tail, and hence if a priori information is know about the sequence of elements in the list, traversal could be initiated from the head or tail, and the traversal time could be lower than a singly linked list. Still $O(n)$ time though!

Recursion

- Recursion: A function calling itself.
- Recursions are represented using a recurrence relation (incl. a base or terminating condition)
- Example 1
- $\text{Factorial}(n) = n * \text{Factorial}(n-1)$ for $n > 0$
- $\text{Factorial}(n) = 1$ for $n = 0$

```
Factorial(n)
  if (n == 0)
    return 1;
  else
    return n * Factorial(n-1)
```

```
Factorial(0) = 1
Factorial(1) = 1 * Factorial(0)
Factorial(2) = 2 * Factorial(1)
Factorial(3) = 3 * Factorial(2)
Factorial(4) = 4 * Factorial(3)
Factorial(5) = 5 * Factorial(4)
```

```
int main(){
```

C++

Example (Code 4) to Illustrate Recursion and Random Number Generation

```
int arraySize;
```

```
cout << "Enter an array size: ";
```

```
cin >> arraySize;
```

```
int maxValue;
```

```
cout << "Enter the max. value of an element: ";
```

```
cin >> maxValue;
```

```
srand(time(NULL));
```

Initialize the random number generator with a seed that corresponds to the current system time

```
int array[arraySize];
```

```
for (int i = 0; i < arraySize; i++){  
    array[i] = rand() % maxValue;  
}
```

The random numbers are generated from 0 to maxValue – 1

```
cout << "IterativePrint: ";
```

```
IterativePrint(array, arraySize);
```

```
cout << "RecursivePrint: ";
```

```
RecursivePrint(array, arraySize, 0);
```

```
return 0;
```

```
}
```

Headers to be included

```
#include <iostream>
```

```
#include <stdlib.h> // random number
```

```
#include <time.h> // for time
```

```
using namespace std;
```

Code 4: C++

```
void IterativePrint(int* arrayPtr, int size){  
    for (int index = 0; index < size; index++){  
        cout << arrayPtr[index] << " ";  
  
    cout << endl;  
}
```

```
void RecursivePrint(int* arrayPtr, int size, int printIndex){  
    if (printIndex == size){  
        cout << endl;  
        return;  
    }  
    cout << arrayPtr[printIndex] << " "; Printing in the forward order  
  
    RecursivePrint(arrayPtr, size, printIndex+1);  
  
    cout << arrayPtr[printIndex] << " "; Printing in the reverse order  
}
```

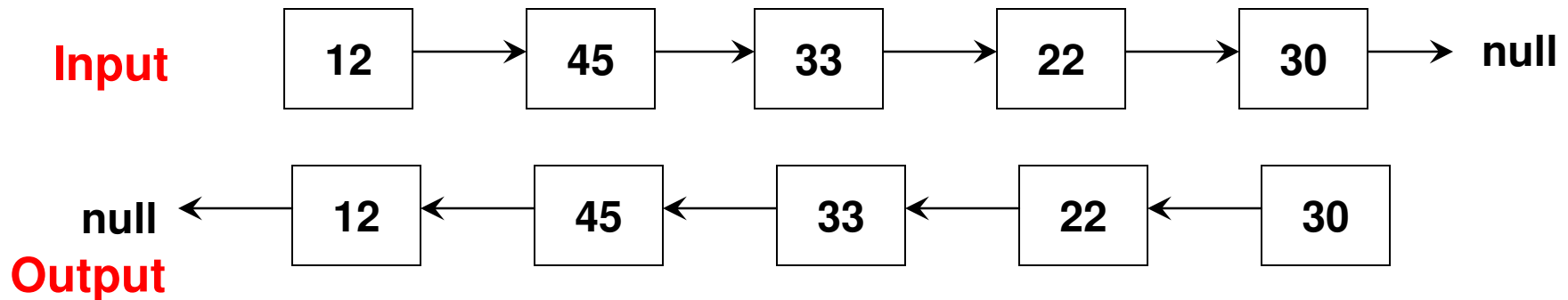
Recursion

Seq

	0	1	2	3
array	14	21	33	45
Seq	2	4	6	8
	14	21	33	45
	45	33	21	14
Seq	12	13	14	15

```
10 if (printIndex == arraySize){ // printIndex = 4
11     cout << endl; // 4 == 4
12     return;
13 }
8 cout << arrayPtr[3] << " "; // printIndex = 3
9 RecursivePrint(arrayPtr, arraySize = 4, printIndex + 1)
12 cout << arrayPtr[3] << " "; // printIndex = 3
6 cout << arrayPtr[2] << " "; // printIndex = 2
7 RecursivePrint(arrayPtr, arraySize = 4, printIndex + 1)
13 cout << arrayPtr[2] << " "; // printIndex = 2
4 cout << arrayPtr[1] << " "; // printIndex = 1
5 RecursivePrint(arrayPtr, arraySize = 4, printIndex + 1)
14 cout << arrayPtr[1] << " "; // printIndex = 1
2 cout << arrayPtr[0] << " "; // printIndex = 0
3 RecursivePrint(arrayPtr, arraySize = 4, printIndex + 1)
15 cout << arrayPtr[0] << " "; // printIndex = 0
@main
1 RecursivePrint(array, arraySize = 4, printIndex = 0)
```


Reversing a Linked List



Logic Maintain three pointers
currentNodePtr, nextNodePtr, prevNodePtr

Enter the loop if currentNodePtr is not null

After entering the loop,

Step 1: set nextNodePtr = currentNodePtr->getNextNodePtr()

Now that there is a pointer to the next node of currentNode, reverse the direction for the next node of currentNode

Step 2: currentNodePtr->setNextNodePtr(prevNodePtr)

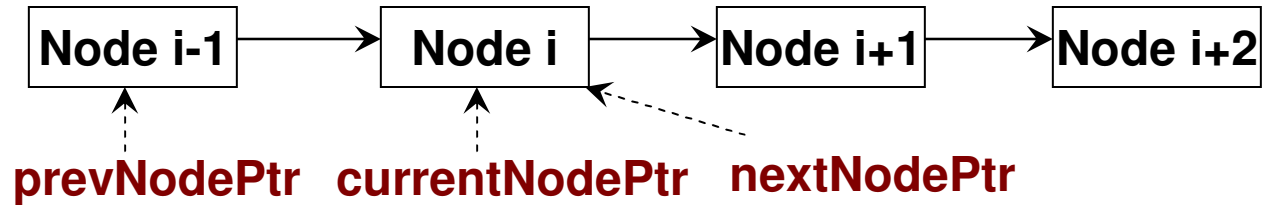
Now prepare for the next iteration,

Step 3: set prevNodePtr = currentNodePtr

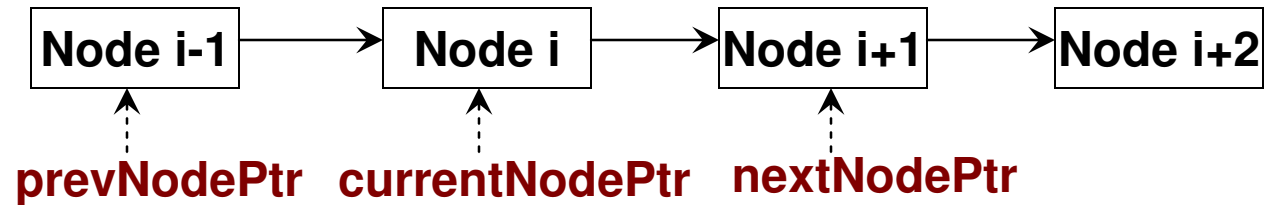
Step 4: set currentNodePtr = nextNodePtr

Reversing a Linked List (logic)

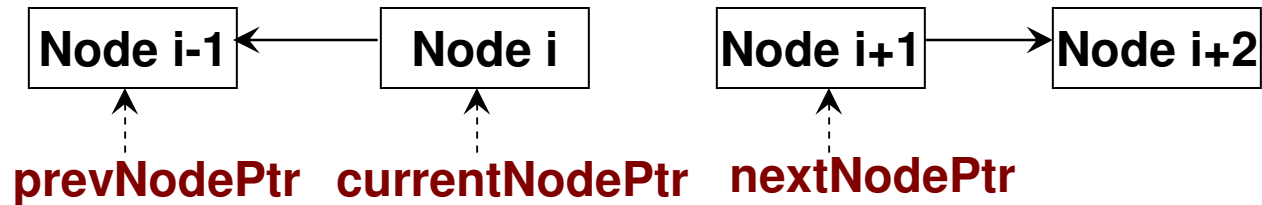
At the time of entering the loop:



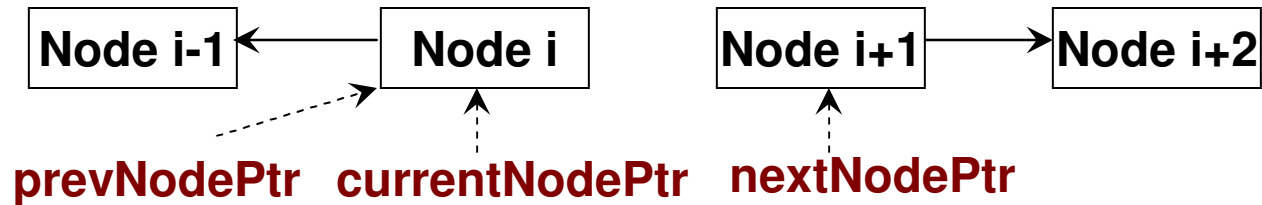
Step 1:



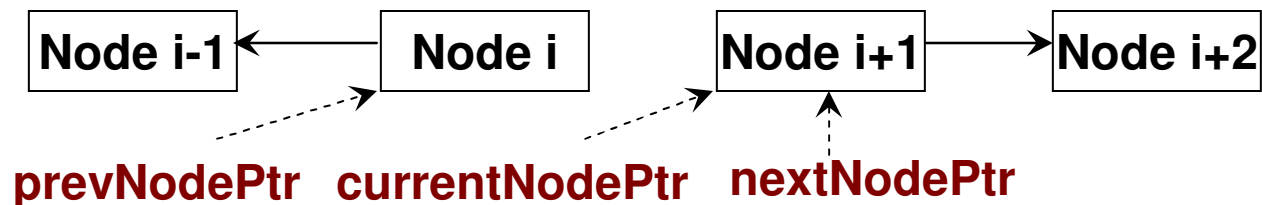
Step 2:



Step 3:



Step 4:



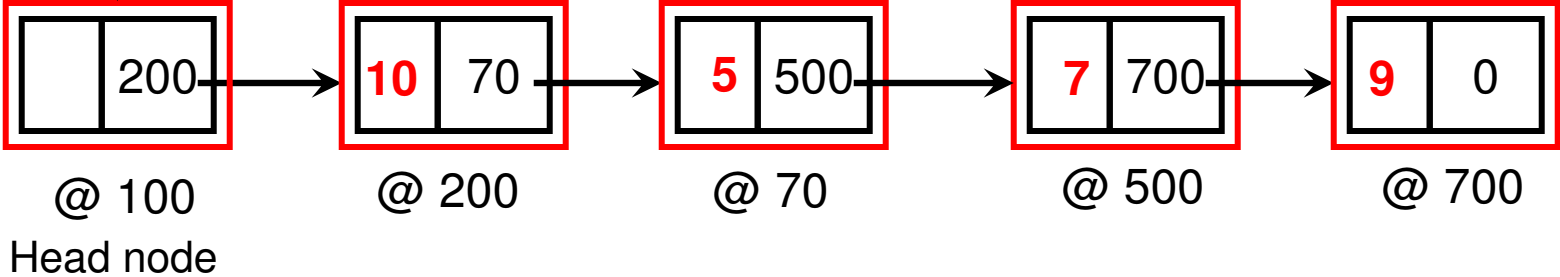
Reversing a Singly Linked List (Code 5): C++

```
void reverseList(){  
    Node* currentNodePtr = headPtr->getNextNodePtr();  
    Node* prevNodePtr = 0;  
    Node* nextNodePtr = currentNodePtr;  
  
    while (currentNodePtr != 0){  
        nextNodePtr = currentNodePtr->getNextNodePtr(); // Step 1  
        currentNodePtr->setNextNodePtr(prevNodePtr); // Step 2  
        prevNodePtr = currentNodePtr; // Step 3  
        currentNodePtr = nextNodePtr; // Step 4  
    }  
    headPtr->setNextNodePtr(prevNodePtr);  
}
```

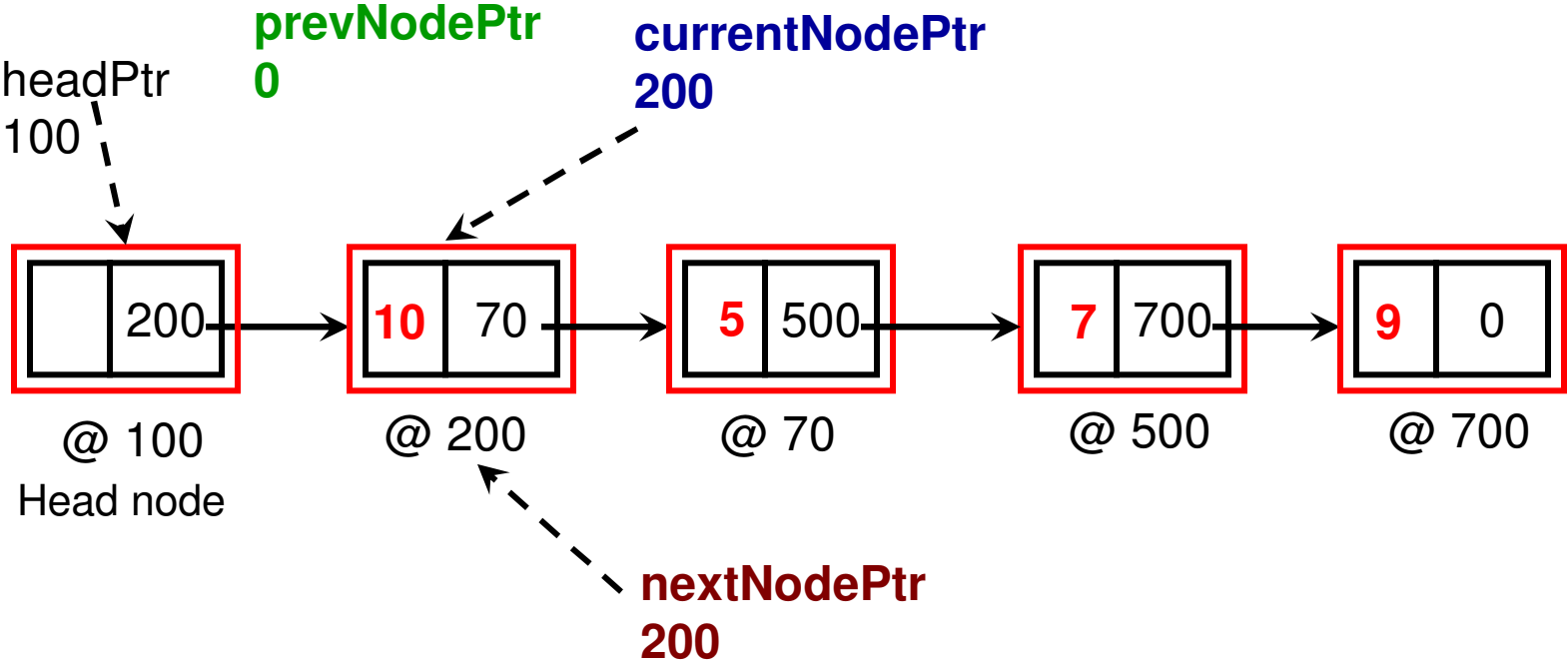
Example: Reversing a Singly Linked List

headPtr
100

Let the List be **10 5 7 9**
It needs to be reversed as **9 7 5 10**



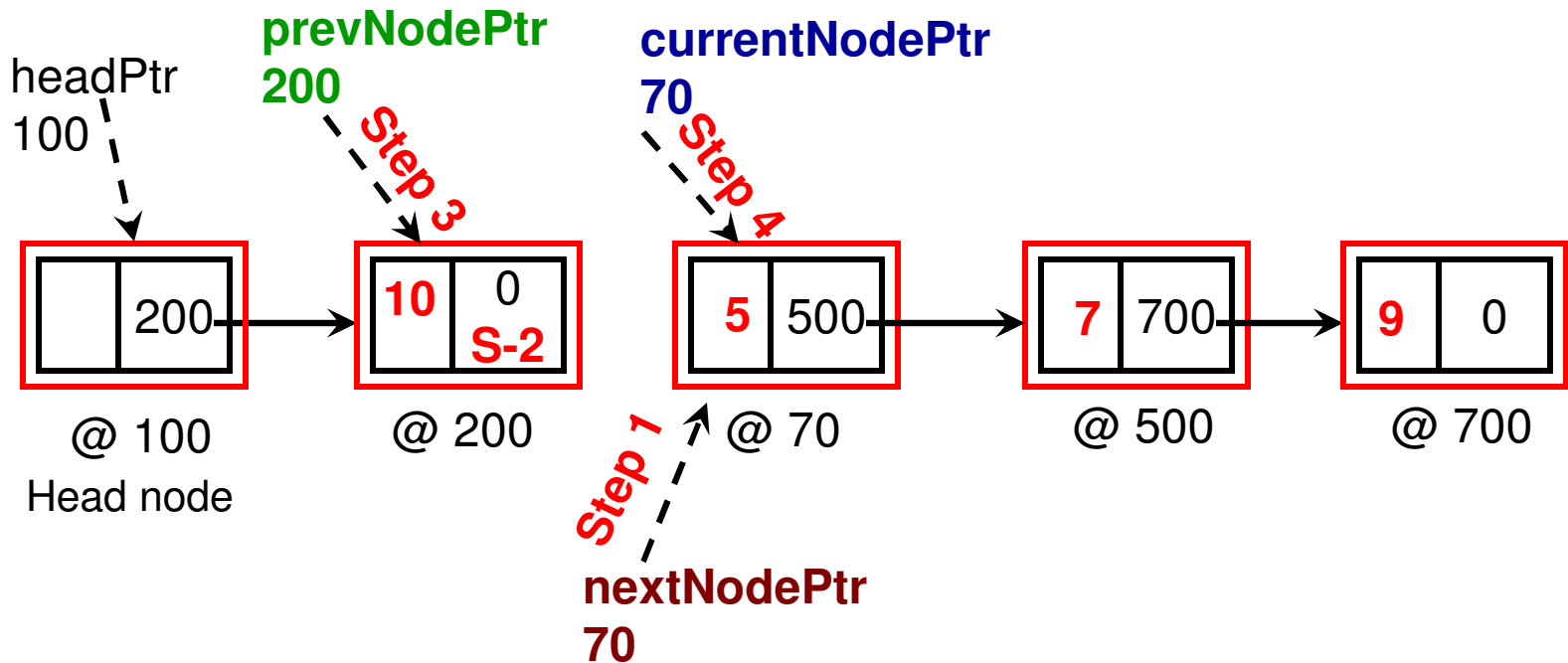
Initialization of the Pointers



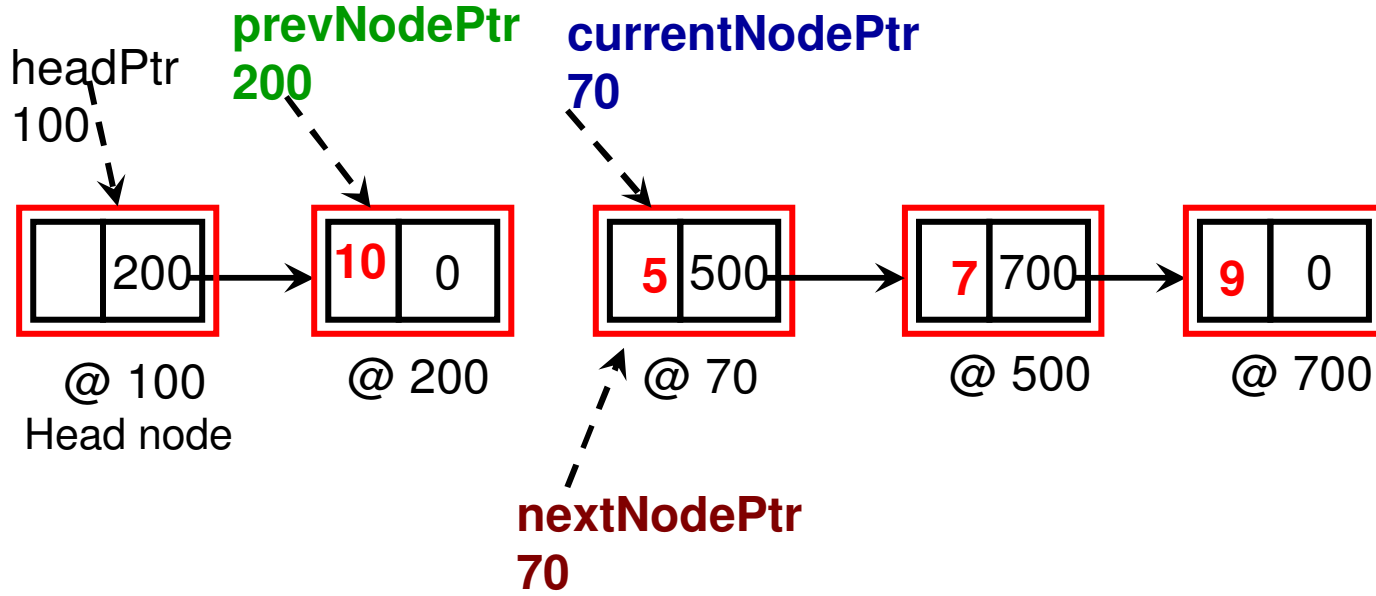
Example: Reversing a Singly Linked List

Inside the while loop (Iteration 1)

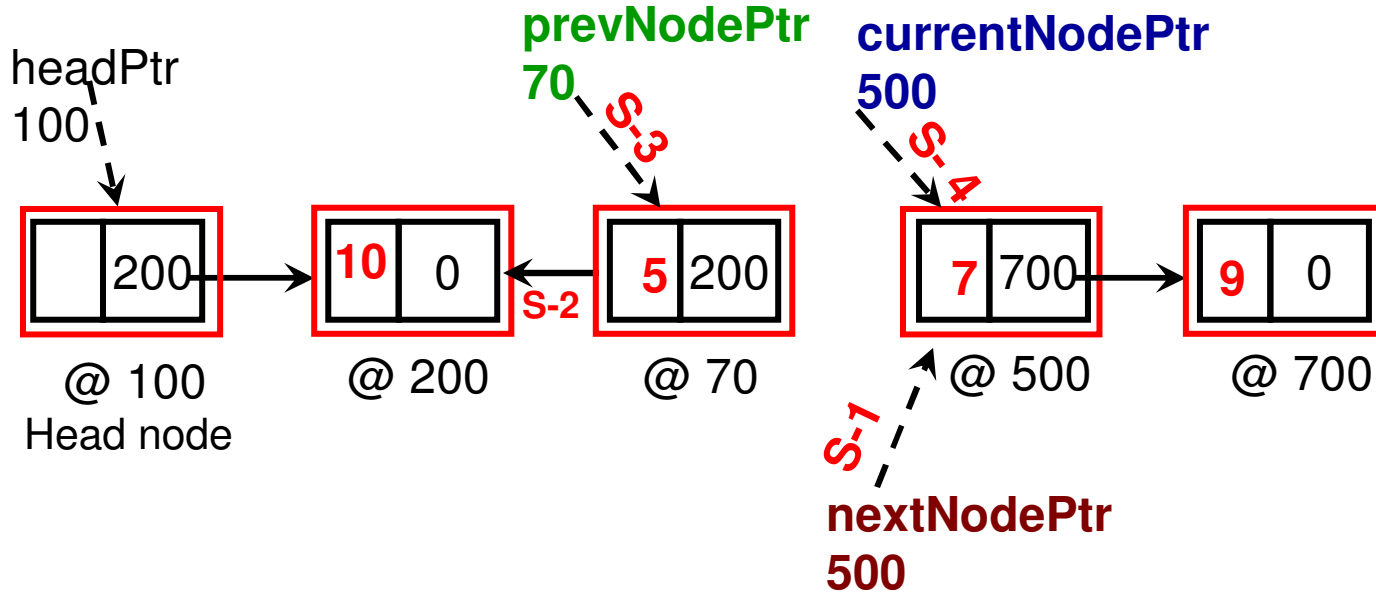
```
nextNodePtr = currentNodePtr->getNextNodePtr(); // Step 1
currentNodePtr->setNextNodePtr(prevNodePtr); // Step 2
prevNodePtr = currentNodePtr; // Step 3
currentNodePtr = nextNodePtr; // Step 4
```



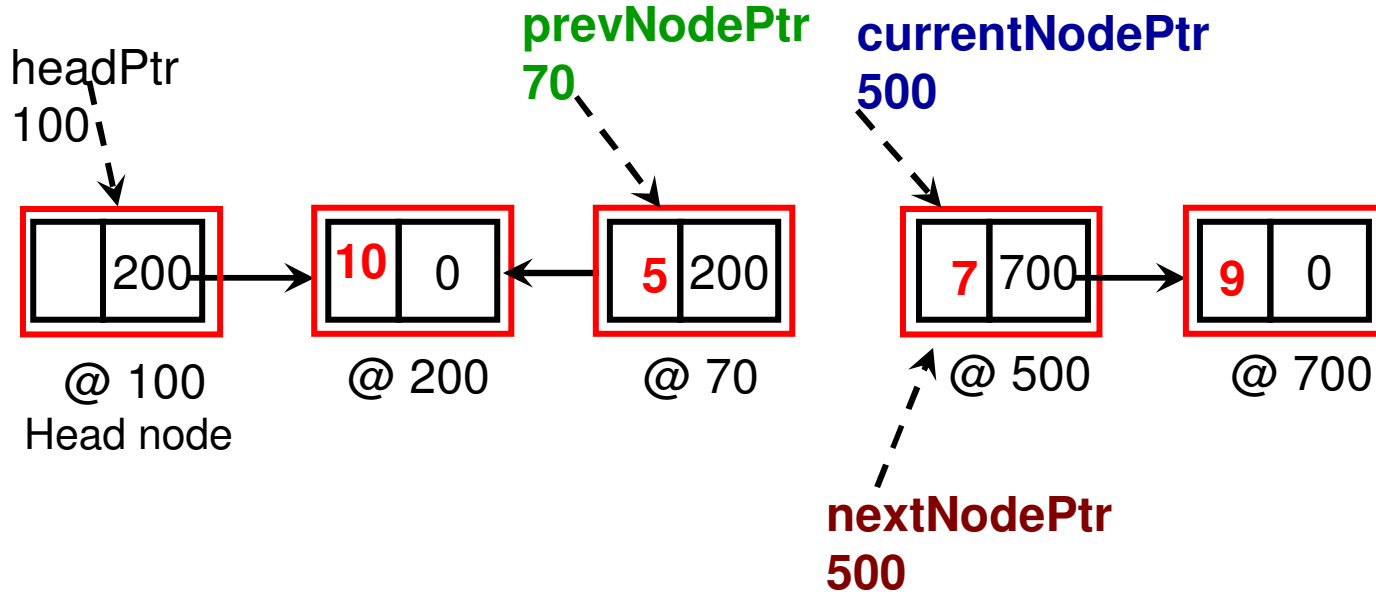
At the end of Iteration 1



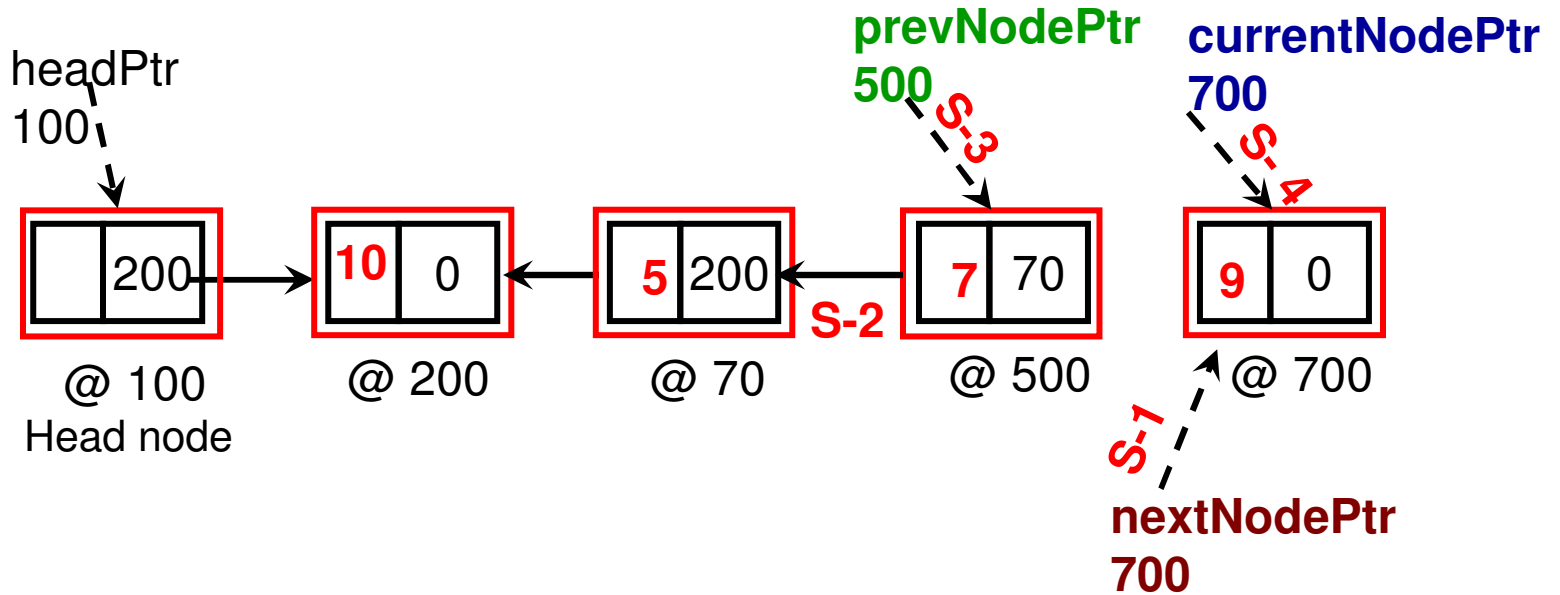
Iteration 2



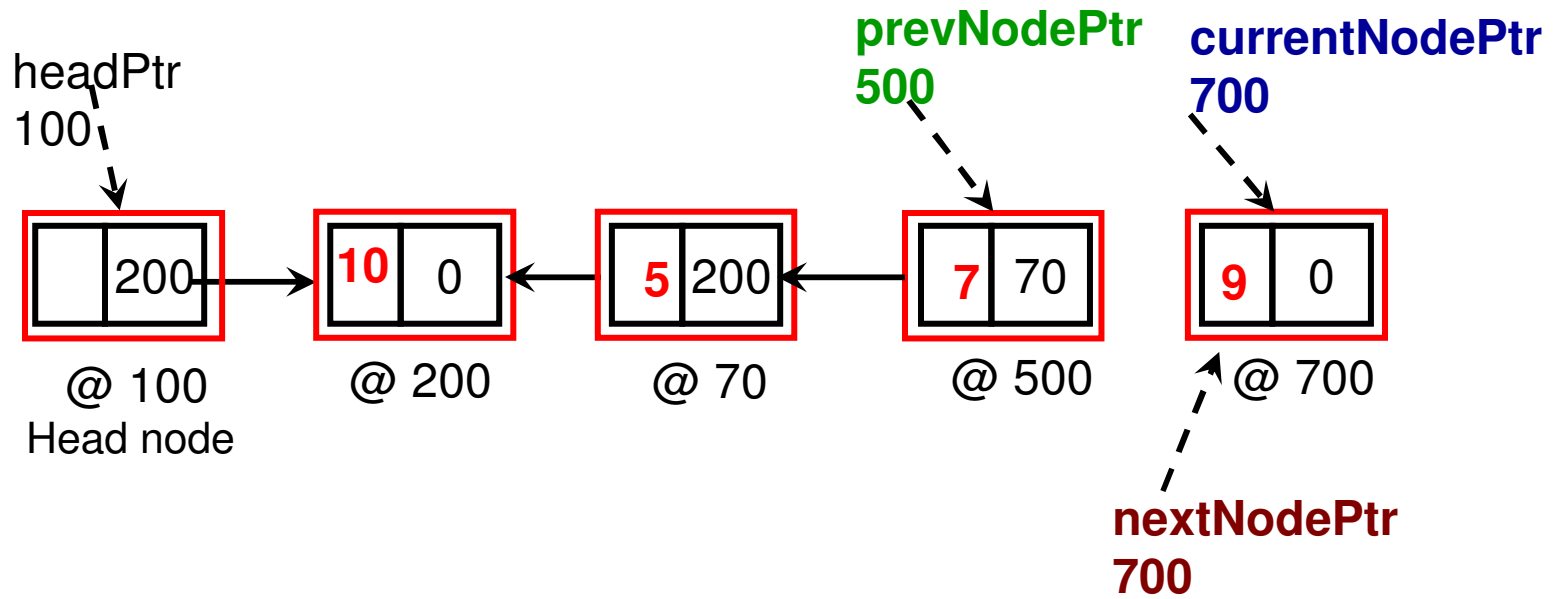
At the end of Iteration 2



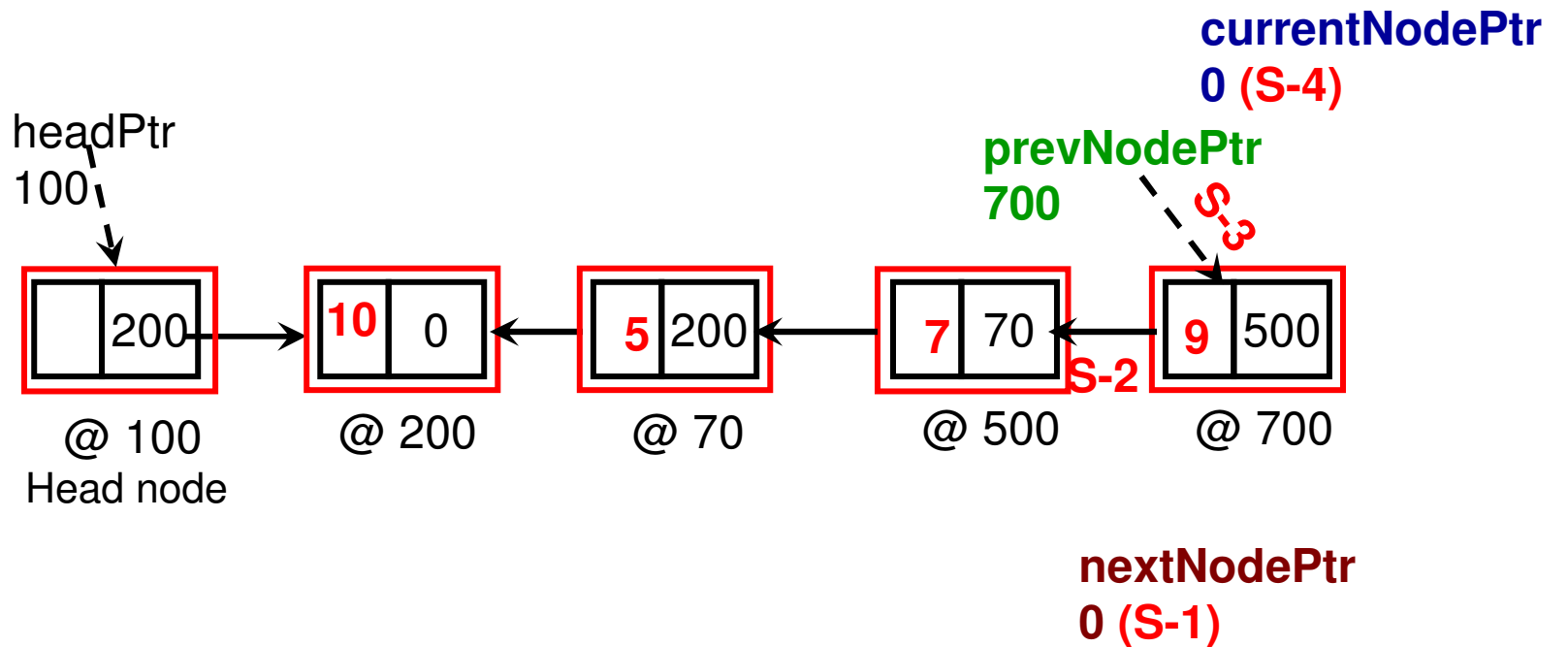
Iteration 3



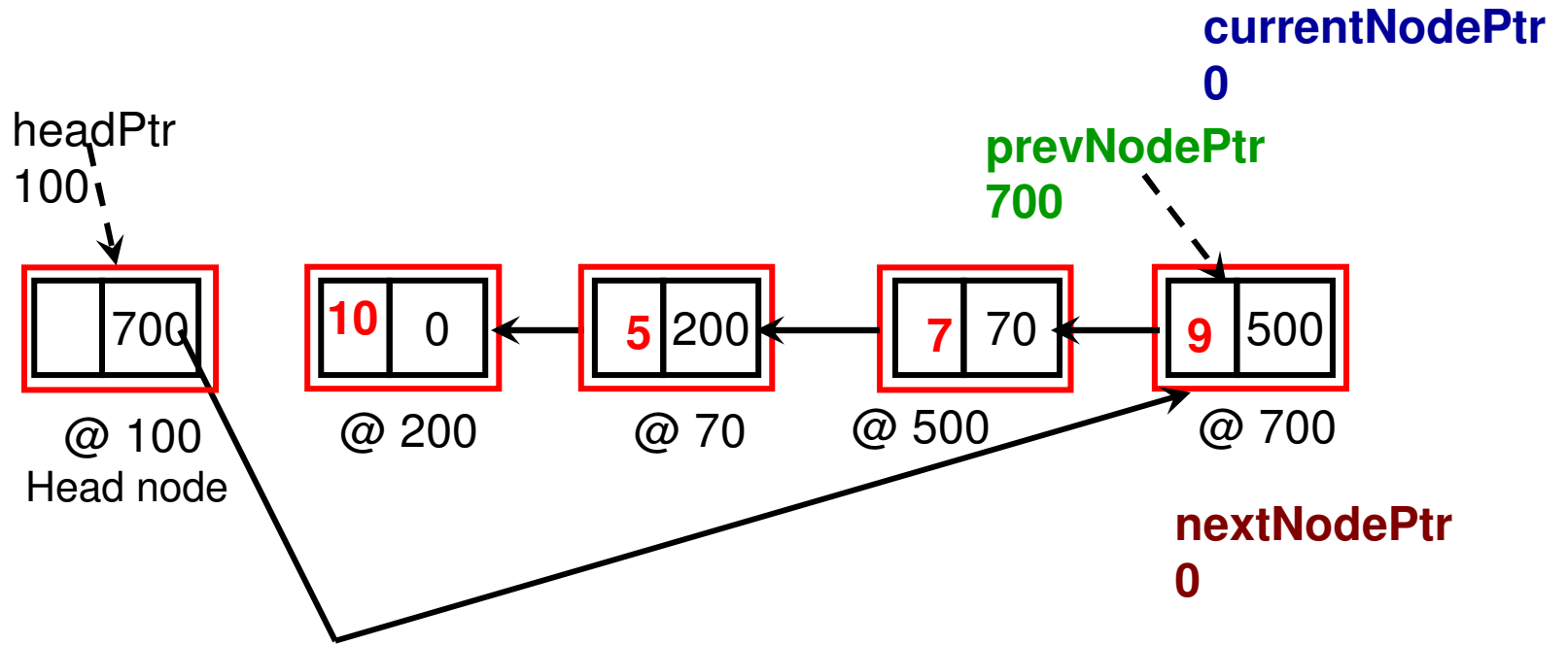
At the end of Iteration 3



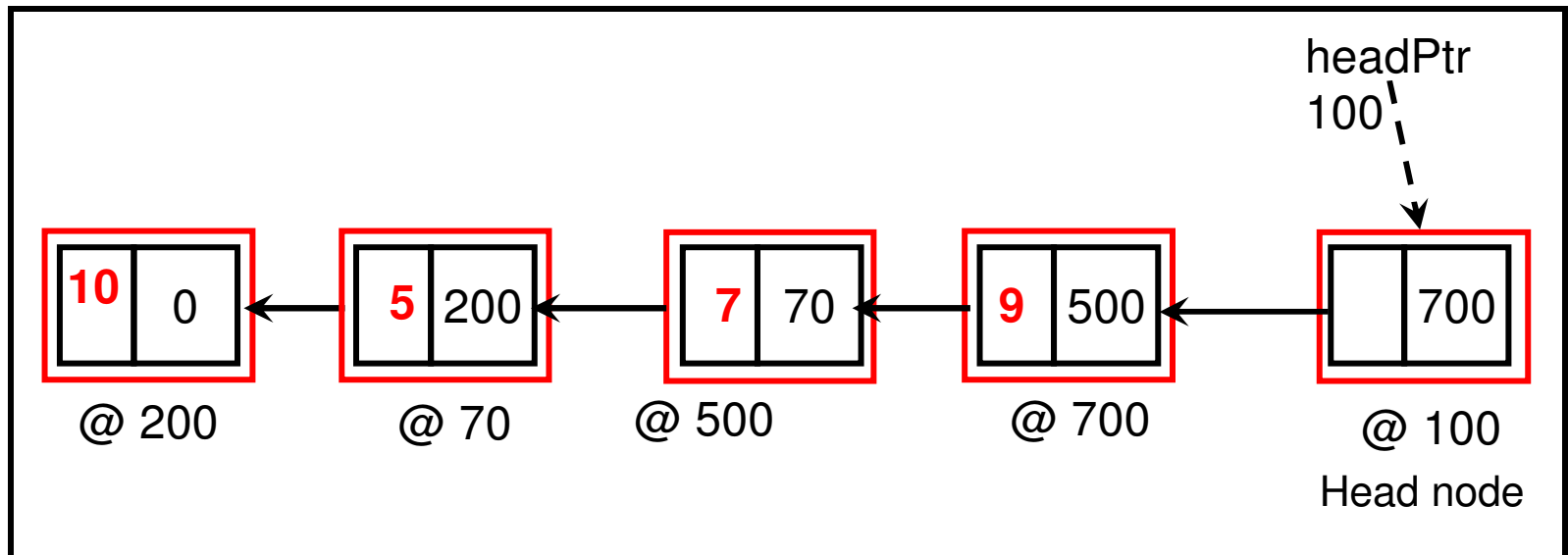
Iteration 4



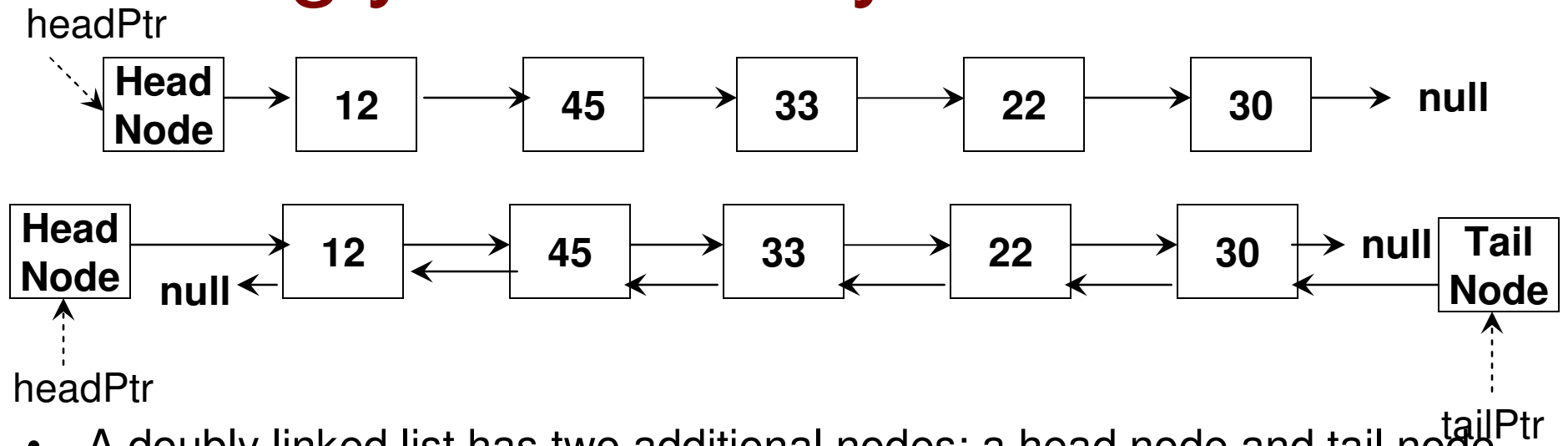
After coming out of the
'while' loop



Reversed Singly
Linked List



Singly vs. Doubly Linked List



- A doubly linked list has two additional nodes: a head node and tail node (a head ptr points to the head node whose next node is the first node in the list, and a tail ptr points to the tail node whose prev node is the last node in the list).
 - Note the next node for the last node in the list is null (so that the end of the list could be traced) as well as the prev node for the first node in the list is null (so that the beginning of the list could be traced).
- A doubly linked list could be traversed in either direction (from head to tail or from tail to head).
 - NextNodePtr values at the nodes are used to access in the forward direction (from head node to the last node)
 - PrevNodePtr values at the nodes are used to access in the reverse direction (from the tail node to the first node)

private:

```
int data;  
Node* nextNodePtr;
```

**Class
Node**

private:

```
int data;  
Node* nextNodePtr;  
Node* prevNodePtr;
```

public:

```
Node(){}
```

```
void setNextNodePtr(Node* nodePtr){  
    nextNodePtr = nodePtr;  
}
```

```
Node* getNextNodePtr(){  
    return nextNodePtr;  
}
```

**Singly
Linked List**

C++

public:

```
Node(){}
```

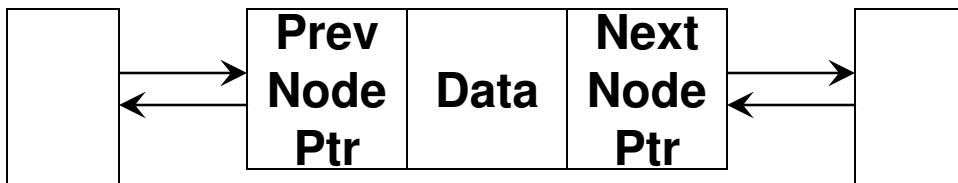
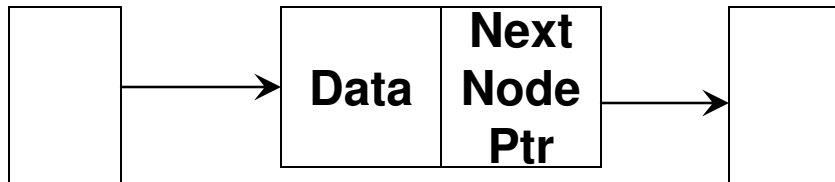
```
void setNextNodePtr(Node* nodePtr){  
    nextNodePtr = nodePtr;  
}
```

```
Node* getNextNodePtr(){  
    return nextNodePtr;  
}
```

**Doubly
Linked List**

```
void setPrevNodePtr(Node* nodePtr){  
    prevNodePtr = nodePtr;  
}
```

```
Node* getPrevNodePtr(){  
    return prevNodePtr;  
}
```



```

private:
    Node *headPtr; Singly
                    Linked List
public:
    List(){
        headPtr = new Node();
        headPtr->setNextNodePtr(0);
    }

    Node* getHeadPtr(){
        return headPtr;
    }

```

```

private:
    Node *headPtr; Doubly
    Node* tailPtr; Linked List
public:
    List(){
        headPtr = new Node();
        tailPtr = new Node();
        headPtr->setNextNodePtr(0);
        tailPtr->setPrevNodePtr(0);
    }

    Node* getHeadPtr(){
        return headPtr;
    }

    Node* getTailPtr(){
        return tailPtr;
    }

```