Student Name: _____ J#: _____

CSC 641 Network Science, Fall 2018
Instructor: Dr. Natarajan Meghanathan
Exam 5 (Take Home)
Due: Submit Hardcopy in class on Thursday, Nov. 29th @ 7.30 PM

Max. Points: 100

Answer all questions in the space provided.
Use additional sheets, if needed. Staple all the sheets together.

1) (6 pts) Consider a regular ring lattice of degree 12 for every node. This regular graph is transformed to a small-world network by arbitrarily re-wiring the edges with probability β. Let the clustering coefficient of the small-world network generated out of this re-wiring be 0.3. **Determine the re-wiring probability β**.

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2) (12 pts) At time 300 units, you are given the degree distribution of the nodes that joined at the time units indicated as shown. Determine the number of links added per node introduction (m) and the network's dynamical exponent (β). Also, estimate the degree of a node that joined the network at time 40 units.

Node joining Time, t_i	**Degree at time t = 300**
5	29
15	16
30	11
45	9
60	7
75	6
100	5

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3) (13 pts) A node joined the network at time 20 units. You are given the degree of the node at various time units. Determine the number of links added per node introduction and the fitness (η) of the node. Under the BB model of evolution, assume the dynamical exponent value for a node is equal to the fitness of the node itself. Also, estimate the degree of the node at time 300 units.

Time Unit, *t*	**Degree at Time *t***
30	8
60	29
90	60
120	101
150	150
180	209
200	252
225	312

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4) (12 pts) Consider the BB model for evolution of scale-free networks.

- Let the parameter $\beta(\eta i)$ for any node i be equal to the fitness of node i, ηi. Consider two nodes A and B such that the fitness of node B is four times the fitness of node A.
- Node A joins the network at time 20 units and node B joins the network at time 150 units.
- If the degree of the nodes increase for every time unit (when a new node joins), what is the *minimum* value of the time unit starting from which the degree of node B would always be greater than the degree of node A?

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5) (7 pts) Consider a network modeled using the power-law, $P(K) = CK^{-\gamma}$. Determine the power-law exponent γ and the constant C if the network has approximately 15% of nodes with degree 4 and 5% of nodes with degree 6.

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6) (10 pts) Given the following adjacency list for the vertices, Use the **Kurtosis** measure to determine whether the Degree distribution could be classified to exhibit "scale-free" property.

0	1
0	2
0	3
0	4
0	5
0	6
0	7
1	2
1	3
1	4
1	5
1	8
1	9

2	3
2	8
3	4
3	5
3	6
3	9
4	6
4	7
4	8
6	7
6	9

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7) (12 pts) Consider the following degree distribution of the nodes and their fitness.

(a) Determine the probability with which each node is likely to get the first link with a newly joining node under the BB model.

(b) Let a new node join the network with 2 links under the BB model. Determine which nodes are likely to get connected to the new node.

ID	Degree	Fitness
1	5	2
2	2	4
3	5	8
4	3	5
5	3	3
6	2	5
7	2	4

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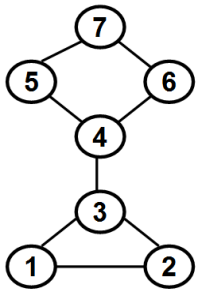
8) (10 pts) Let the network (shown on the right side) evolve to a small-world network under the "Enhanced Watts-Strogatz Model". Let the link 1 - 2 be the first link chosen for rewiring. Predict the vertex to which vertex 1 will be rewired to? Use q = 1



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9) (6 pts) Consider the enhanced WS model for small-world networks. Let there be a regular graph that is transformed to a small-world network. For every edge (u, v) selected for re-wiring, the probability that a node w of distance 3 hops to u is picked for re-wiring is 0.25 and the probability that a node w' of distance 5 hops to u is picked for re-wiring is 0.10. Find the value for the **parameter q** in the enhanced WS model.

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10) (12 pts) Given the probability degree distribution:

a) Draw a plot of the degree distribution and determine if the degree distribution follows a power-law or Poisson pattern?

b) Determine the parameters of the degree distribution you decided as listed below.

-- If the degree distribution follows Power Law, determine the Power Law Constant (C) and the Power Law Exponent (γ)

-- If the degree distribution follows Poisson Law, determine the randomness index, mean and standard deviation of node degree

K	P(K)
1	0.7780
2	0.1240
3	0.0423
4	0.0197
5	0.0109
6	0.0067
7	0.0045
8	0.0031