## Reading List for Exam 3 (in-class, OPEN notes)

## All questions from Module 9 - Graphs

## Part I - To be tested on Wednesday, April 24th: 1 PM to 1.50 PM

- 1) Given a bipartite graph, run the Breadth First Search (BFS) algorithm on the graph: indicate the level numbers of the vertices and identify the tree edges and cross edges, using all of which determine the two partitions of the graph.
- 2) Given a graph, run the Depth First Search (DFS) algorithm on a given graph to identify the articulation points and bridge edges. Merely guessing and writing an answer will get you only ZERO points.
- 3) Run the Depth First Search (DFS) algorithm on a given directed graph.
- (a) Identify the different types of edges as part of DFS.
- (b) Determine the push and pop order of the vertices.
- (c) Determine the strongly connected component(s) of the graph
- (d) Determine the weakly connected component(s) of the graph

-----

## Part II - To be tested on Friday, April 26th: 1 PM to 1.50 PM

- 4) Given an undirected graph, run the Depth First Search (DFS) algorithm.
- (a) Draw the DFS tree with tree edges and back edges as well as show the push and pop orders of the vertices.
- (b) Use the results of (a) to assign directions to the edges such that the resulting directed graph has all the vertices in one strongly connected component.
- (c) Use the results of (a) to assign directions to the edges such that the resulting directed graph is a directed acyclic graph (DAG).
- 5) Run the Depth First Search algorithm on a given directed acyclic graph (DAG) and determine a topological sort of the vertices.
- 6) Given an undirected graph.
- (a) Determine the degree values of the vertices and the probability of observing a vertex with a certain degree.
- (b) Using (a), determine the average degree of the vertices and the number of edges in the graph.
- (c) Assign directions to the edges such that the resulting directed graph is a directed acyclic graph with a given topological sort order.
- (d) Without running DFS, what can you say about the strongly connected components of the directed graph obtained in (c)?